Short-range correlations and the nuclear EMC effect in deuterium and helium-3

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The EMC effect in deuterium and helium-3 is studied using a convolution formalism that allows isolating the impact of high-momentum nucleons in short-ranged correlated (SRC) pairs. We assume that the modification of the structure function of bound nucleons is given by a universal (i.e., nucleus independent) function of their virtuality, and find that the effect of such modifications is dominated by nucleons in SRC pairs. This SRC-dominance of nucleon modifications is observed despite the fact that the bulk of the nuclear inelastic scattering cross-section comes from interacting with low-momentum nucleons. These conclusions are found to be robust to model details including nucleon modification function parametrization, free nucleon structure function, and treatment of nucleon motion effects. While existing data cannot discriminate between such model details, we present predictions for measured, but not yet published, tritium EMC effect and tagged nucleon structure functions in deuterium that are sensitive to the neutron structure functions and bound nucleon modification functions.

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I. INTRODUCTION

Determining the underlying cause of the modification of the partonic structure of nucleons bound in atomic nuclei, known as the EMC effect [1-7], is an outstanding question in nuclear physics. Decades after its discovery, there is still no universally accepted explanation for the origin of the EMC effect [8-11], despite a large number of high-precision measurements in a wide variety of atomic nuclei.

Modern models of the EMC effect account for both "conventional" nuclear physics effects such as Fermi-motion and binding, as well as for the more "exotic" effects of nucleon modification [10–14], especially considering nucleon off-shellness [15,16]. The conventional nuclear physics effects are well understood and cannot reproduce experimental data alone, especially when including Drell-Yan data [11,17]. While required to reproduce experimental data, nucleon modification models are far less constrained and their microscopic origin is debated [11].

An observed correlation between the magnitude of the EMC effect and the relative abundance of short-range correlated (SRC) nucleon pairs in different nuclei [7,18–20] suggests that the EMC effect is driven by the modification of nucleons in SRC pairs. SRCs are pairs of strongly interacting nucleons at short distances. Nucleons in SRC pairs have large spatial overlap between their quark distributions and are highly off-shell ($E^2 \neq |\mathbf{p}|^2 + m^2$), which makes them prime candidates for structure modification.

Most recently, it has been demonstrated [7,21] that the EMC effect in nuclei from helium-3 (³He) to lead can be explained by a single effective universal modification function (UMF) of nucleons in SRC pairs. The UMF was constructed to be as model independent as possible. It is insensitive to the largely-unknown free-neutron structure function, F_2^n , and accounts for both conventional nuclear effects, such as the scheme dependence of the deuteron wave function, and nucleon motion effects, as well as more exotic nucleon modification effects.

Here we study the EMC effect using a convolution formalism that allows us to separate the mean field and short range correlation contributions of nucleon modification effects to the total UMF. We consider only light nuclei (the deuteron and ³He), for which exact nuclear wave functions are available, and nucleon modification effects can be isolated. The sensitivity of the convolution formalism to parametrization of the nucleon modification function F_2^n and the treatment of nucleon motion effects is studied.

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The convolution work described here is similar to the works of [22,23], although here we only focus on deuterium and helium-3 to make use of the exactly calculable nuclear dynamics that is available only for these systems. We further study a wide model phase space by considering different models of the free neutron structure function, nuclear motion dynamics, and bound nucleon modification functions.

We find that, as expected, the bulk of the structure-function comes from interactions with low-momentum nucleons. However, nucleon modification effects, which are required for a complete reproduction of the measured data, are dominated by nucleons in SRC pairs. We also find that existing data cannot discriminate between different F_2^n models or different parametrizations of bound nucleon modification functions. We predict new observables that can constrain these model inputs, including the tritium EMC effect, sensitive to F_2^n , and deuterium tagged nucleon structure functions, sensitive to bound nucleon modification functions. These predictions will soon be tested by data from the MARATHON [24], BAND [25], and LAD [26] Collaborations.

II. FORMALISM

A. F_2^A convolution approximation

In order to study the EMC effect in a framework that allows us to understand its dependence on nucleon momentum and off-shellness, we calculate the nuclear structure function $F_2^A(x_B)$, using the nuclear convolution model for lepton-nucleus DIS [8,27–30]:

$$\begin{split} F_{2}^{A}(x_{B}) &= \\ \frac{1}{A} \int_{x_{B}}^{A} \frac{d\alpha}{\alpha} \int_{-\infty}^{0} dv \Big[Z \tilde{\rho}_{p}^{A}(\alpha, v) F_{2}^{p}(\tilde{x}) + N \tilde{\rho}_{n}^{A}(\alpha, v) F_{2}^{n}(\tilde{x}) \Big] \\ &\times \Big(1 + v \ f^{\text{off}}(\tilde{x}) \Big) \\ &= \frac{1}{A} \int_{x_{B}}^{A} \frac{d\alpha}{\alpha} \int_{-\infty}^{0} dv \ F_{2}^{p}(\tilde{x}) \Big[Z \tilde{\rho}_{p}^{A}(\alpha, v) + N \tilde{\rho}_{n}^{A}(\alpha, v) \frac{F_{2}^{n}(\tilde{x})}{F_{2}^{p}(\tilde{x})} \Big] \\ &\times \Big(1 + v \ f^{\text{off}}(\tilde{x}) \Big), \end{split}$$

$$(1)$$

where $x_B = Q^2/(2m_N v)$, Q^2 is the four-momentum transfer squared, m_N is the nucleon mass, and v is the energy transfer (Fig. 1). $\tilde{x} = \frac{Q^2}{2p \cdot q}$ where q is the four-momentum of the virtual photon and p is the initial four-momentum of the struck off-shell nucleon. \tilde{x} reduces to $\frac{x_B}{\alpha} \frac{m_N A}{m_A}$ in the Bjorken limit with lightcone momentum fraction $\alpha = A(E + p_z)/m_A$ [see Appendices for finite energy corrections to Eq. (A1) at low Q^2]. Here z is opposite to the direction of the virtual photon, and $v = (E^2 - |\mathbf{p}|^2 - m_N^2)/m_N^2$ is the bound nucleon fractional virtuality. The functions $\tilde{p}_N^A(\alpha, v)$ are the nucleon (N = p or n) lightcone momentum and virtuality distributions in nucleus A, defined below. $F_2^p(\tilde{x})$ and $F_2^n(\tilde{x})$ are the free proton and neutron structure functions. We note that Eq. (A1) arises from a four-dimensional integral involving d^4p , where we perform a change of variables to α , v, and integrate over the remaining degrees of freedom [8]. For brevity we omit their explicit Q^2 dependencies but note that F_2^p , F_2^n , and F_2^A



FIG. 1. Reaction diagram for lepton-nuclear deep inelastic scattering in a factorized plane wave impulse approximation for (a) spectral function kinematics and (b) lightcone kinematics. Red lines represent off-shell nucleons. See text for details.

are always evaluated at the same Q^2 value. $f^{\text{off}}(\tilde{x})$ is a universal off-shell nucleon modification function, assumed here to be the same for neutrons and protons and for all nuclei. In Eq. (A1), we take the off-shell effect to be linear in v (i.e., $1 + v f^{\text{off}}(\tilde{x})$) as a first-order Taylor expansion in virtuality; see Ref. [31] for additional discussion.

B. Lightcone densities

In our convolution, traditional nuclear contributions to the EMC effect such as nucleon motion and binding are treated within the one-body lightcone momentum and virtuality distribution $\tilde{\rho}_N^A(\alpha, v)$. It describes the joint probability to find a nucleon (*n* or *p*) in a nucleus *A* with lightcone momentum fraction α and fractional virtuality *v*. Integrating over fractional virtuality defines the lightcone momentum distribution of a nucleon

$$\rho_N^A(\alpha) = \int_{-\infty}^0 dv \tilde{\rho}_N^A(\alpha, v), \qquad (2)$$

which is normalized herein according to the baryon sum rule:

$$\int_{0}^{A} \frac{d\alpha}{\alpha} \rho_{N}^{A}(\alpha) \equiv 1.$$
 (3)

To avoid producing an artificial EMC-like effect in nucleon-only models when used in Eq. (A1) [28], $\rho_N^A(\alpha)$ must also satisfy the momentum sum rule:

$$\frac{1}{A}\int_0^A \frac{d\alpha}{\alpha} \alpha \left(Z\rho_p^A(\alpha) + N\rho_n^A(\alpha) \right) = 1.$$
(4)

It is necessary to know the functional form of $\tilde{\rho}_N^A(\alpha, v)$ to proceed further. Although the nuclear wave functions for nuclei with A = 2 and A = 3 have been well computed, they do not suffice to unambiguously yield the lightcone momentum distributions and their dependence on virtuality. Handling this issue on a fundamental level would require a first-principles light-front calculation including the effects of off-mass-shell dependence. Such a calculation could be done by solving the relevant Bethe-Salpeter equation, but does not yet exist.

Therefore, we consider here two approximations to estimate $\tilde{\rho}(\alpha, \nu)$: a spectral-function (SF) approximation, where the momentum sum rule is violated if only nucleonic degrees of freedom are taken into account, and a generalized contact formalism lightcone (GCF-LC) approximation.

1. Spectral function approximation

The nuclear spectral function S(E, p) defines the probability for finding a nucleon in the nucleus with momentum p and nucleon energy E. Exactly calculable spectral functions are available for light nuclei and allow calculating the nuclear lightcone distributions as [32,33]

$$\tilde{\rho}_{N,SF}^{A}(\alpha, v) = \int dE d^{3} \mathbf{p} \ S_{N}^{A}(E, p) \cdot \frac{E + p_{z}}{E} \times \delta\left(\alpha - \frac{Ap^{+}}{P^{+}}\right) \delta\left(v - \frac{E^{2} - |\mathbf{p}|^{2} - m_{N}^{2}}{m_{N}^{2}}\right),$$
(5)

where $p = |\mathbf{p}|, p^+ \equiv E + p_z = m_A \alpha / A$ is the plus-component of the momentum of the struck nucleon, $P^+ = m_A$ is the pluscomponent of the momentum of the nucleus *A*, and m_A is the nucleus mass.

The flux factor $(E + p_z)$ is introduced to help satisfy the momentum sum rule [28]. The $\frac{1}{E}$ factor ensures SF-based lightcone distribution functions are appropriately normalized according to the Baryon sum rule [Eq. (3)]. However, this also changes the interpretation of $\rho(\alpha)$ from a simple probability density for finding a nucleon in a nucleus with lightcone momentum fraction α (see discussion in Refs. [28,32,33]).

For deuterium, considering a wave function calculated using the AV18 interaction, the momentum sum rule has a negligible violation (<0.1%). For ³He, using the AV18-based spectral function of Ref. [34], it is violated by $\leq 1\%$. This small violation is expected to produce an artificial EMC effect [28] that should result in a smaller nucleon modification effect required to explain the experimental data.

2. Generalized contact formalism lightcone approximation

To fully satisfy the ³He momentum sum rule, we examine an alternative approach for calculating $\tilde{\rho}_N^A(\alpha, v)$ using a scale-separation approximation where the lightcone density function is separated into a mean-field (single-nucleon) part and an SRC part [20,35–38]:

$$\tilde{\rho}^{A}_{N,GCF-LC}(\alpha, v) = \tilde{\rho}^{A}_{N,GCF,SRC}(\alpha, v) + \tilde{\rho}^{A}_{N,MF}(\alpha, v).$$
(6)

The SRC part of the lightcone density can be formulated by integrating over the lightcone SRC decay function [38,39], which describes the distribution of the momentum of the struck nucleon as well as its partner, here denoted the "spectator" nucleon:

$$\tilde{\rho}_{N,GCF,SRC}^{A}(\alpha, v) = \int d^{2}\mathbf{p}_{\perp} \frac{d\alpha_{s}}{\alpha_{s}} d^{2}\mathbf{p}_{s}^{\perp} \rho_{SRC}^{N}(\alpha, \mathbf{p}^{\perp}, \alpha_{s}, \mathbf{p}_{s}^{\perp}) \times \delta\left(v - \frac{p^{-}(m_{A}/A)\alpha - \mathbf{p}_{\perp}^{2} - m_{N}^{2}}{m_{N}^{2}}\right),$$
(7)

where

$$p^{-} = P^{-} - p_{s}^{-} - p_{A-2}^{-}$$

= $m_{A} - \frac{m_{N}^{2} + (\mathbf{p}_{s}^{\perp})^{2}}{(m_{A}/A)\alpha_{s}} - \frac{m_{A-2}^{2} + (\mathbf{p}_{CM}^{\perp})^{2}}{(m_{A}/A)(A - \alpha - \alpha_{s})}$ (8)

is the off-mass shell minus-component of the struck nucleon's momentum, α_s is the spectator nucleon lightcone fraction, \mathbf{p}_{\perp} and $\mathbf{p}_{s,\perp}$ are the transverse momentum of the struck nucleon and the spectator, respectively, and $\mathbf{p}_{CM}^{\perp} = \mathbf{p}_{\perp} + \mathbf{p}_{s,\perp}$. ρ_{SRC}^{N} is a two-body (i.e., pair) lightcone density given by a convolution of the pair center-of-mass and relative momentum densities. See Ref. [38] and Appendices for details.

The mean-field part of the lightcone density is taken from the spectral functions using a linearized approximation, similar to Eq. (5), but which manifestly preserves the baryon number and momentum sum rules:

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$$\tilde{\rho}_{N,MF}^{A}(\alpha, v) = \alpha \int_{0}^{m_{N}} dE \int_{0}^{p_{\text{cutoff}}} d^{3}\mathbf{p} S_{N}^{A}(E, p) \\ \times \delta\left(\alpha - 1 - \frac{Ap_{z}}{P^{+}}\right) \delta\left(v - \frac{E^{2} - |\mathbf{p}|^{2} - m_{N}^{2}}{m_{N}^{2}}\right).$$
(9)

The cutoff momentum, defined in the laboratory frame, $p_{\text{cutoff}} = 240 \text{ MeV}/c$ for ³He and was chosen such that the fraction of SRC pairs was equal to that extracted from *ab initio* many-body calculations (10.1% for neutrons and 5.9% for protons) [40,41].

We note that the exact momentum onset for SRC dominance is not exactly known, it is generally taken to be around the nuclear Fermi momentum. This is supported by both experimental SRC scaling onset observations at 275 ± 25 MeV/c [42] and calculations of infinite nuclear matter [43–45]. While light nuclei, such as helium-3, do not have a well defined Fermi momentum, our choice of a value slightly lower than the Fermi-momentum of medium nuclei is reasonable and as explained above also consistent with SRC probabilities (contact terms) extracted from ab-initio calculations [40,41].

We emphasize that the momentum sum rule for $\tilde{\rho}_{N,GCF-LC}^{A}(\alpha, v)$ is manifestly satisfied in this approximation and that the resulting GCF-LC density has a mean value of unity, in contrast to that obtained in the SF approximation (Fig. 2). We note that this is possible because the implementation of SRC center-of-mass motion in the LC decay function is performed on the lightfront (see Ref. [38] for full details).

III. STRUCTURE, FUNCTION, AND MODIFICATION MODELS

We compute Eq. (A1) using parametrizations of $f^{\text{off}}(\tilde{x})$, $F_2^p(\tilde{x})$, and $\frac{F_2^n(\tilde{x})}{F_2^p(\tilde{x})}$, and both $\tilde{\rho}_{N,SF}^A$ and $\tilde{\rho}_{N,GCF-LC}^A$. For the modification function $f^{\text{off}}(\tilde{x})$ we consider three models:

$$f_{\text{const}}^{\text{off}}(\tilde{x}) = C, \tag{10}$$

$$f_{\lim x}^{\text{off}}(\tilde{x}) = a + b \cdot \tilde{x} \tag{11}$$

$$f_{KP, CJ}^{\text{off}}(\tilde{x}) = C(x_0 - \tilde{x})(x_1 - \tilde{x})(1 + x_0 - \tilde{x})$$
 (12)

where $f_{\text{const}}^{\text{off}}$ assumes a virtuality-dependent modification model that is independent of \tilde{x} , and $f_{\ln x}^{\text{off}}$ is also linearly dependent on \tilde{x} . The free parameters of these parametrizations (*C*, *a*, and *b*) are determined by fitting Eq. (A1) to experimental data as detailed below.



FIG. 2. Lightcone momentum distributions $\rho(\alpha)$ for deuteron (a), protons (b), and neutrons (c) in ³He calculated using the spectral function (SF) and generalized contact formalism lightcone (GCF-LC) approximations. The discretization visible in the SF distributions (blue lines) is due to the discretization of the spectral function S(E, p) and integration of Eq. (5).

We also use modification functions determined by KP (f_{KP}^{off}) [22] and CJ (f_{CJ}^{off}) [46], who both chose to use a third order polynomial in \tilde{x} , albeit with different parameters. These are used here with their original parameters, extracted in Refs. [22,46]. $\frac{F_2^n(\tilde{x})}{F_2^p(\tilde{x})}$ was parametrized as

$$\frac{F_2^n(\tilde{x})}{F_2^p(\tilde{x})} \equiv R_{np}(\tilde{x}) = a_{np}(1-\tilde{x})^{b_{np}} + c_{np},$$
(13)

where $R_{np}(\tilde{x} \to 1) = c_{np}$. We fix the a_{np} , b_{np} , and c_{np} parameters by fitting Eq. (13) to one of two recent predictions by Segarra et al. [21] and by Arrington et al. [47], which represent two extreme models that capture the spread of current models [21] (see Fig. 3). We further assume that $R_{np}(\tilde{x})$ has negligible Q^2 dependence. We note that the original f_{KP}^{off} and f_{CJ}^{off} extractions were done using F_2^n/F_2^p that are respectively similar to the Segarra and Arrington models used herein.

 $F_2^p(x_B, Q^2)$ was taken from GD11-P [48]. As DIS data are typically given in the form of F_2^A/F_2^d ratios to minimize higher twist effects, the only explicit Q^2 dependence we assume is that of $F_2^p(x_B, Q^2)$, that is assumed to be negligible in the ratio F_{2}^{n}/F_{2}^{p} .

We estimated the parameters of $f_{\text{const}}^{\text{off}}$ and $f_{\text{lin }x}^{\text{off}}$ using a χ^2 -minimization inference from a simultaneous fit to both



FIG. 3. F_2^n/F_2^p parametrizations used in this work that span the current range of models [21]. See text for details.

 $F_2^{^{3}He}/F_2^d$ [6] and $F_2^d/(F_2^p + F_2^n)$ [49] data for $0.17 \leq x_B \leq 0.825$. While data for $F_2^{^{3}He}/F_2^d$ of [6] extends up to $x_B \sim$ 0.9, these high- x_B data are at low-invariant mass W. Requiring W > 1.4 GeV ($W^2 > 2$ GeV²) in the fitting procedure limited the data to $x_B \leq 0.825$. However, we extrapolate our predictions up to $x_B \sim 0.95$ for use by future measurements, such as MARATHON [24]. We neglect an explicit quasielastic contribution to our calculation when comparing to data, but this is a minimal contribution when requiring W > 1.4 GeV and restricting our analysis to $x_B \leq 0.825$. Resonance contributions to F_2^p and F_2^n were studied utilizing the Bosted-Christy parametrizations described in Ref. [50], see Appendices. Isoscalar corrections previously applied to $F_2^{^{3}He}/F_2^d$ data were removed and the quoted experimental normalization uncertainties of each data set were accounted for in the fit. In the calculation of each data point, F_2^p is evaluated at the Q^2 value of the data. We performed 16 inference trials for different model assumptions for $\tilde{\rho}(\alpha, v)$, F_2^n/F_2^p , and f^{off} (see Table I). For each trial, after minimization, 1σ confidence bands were produced from the parameter covariance matrix. When using f_{KP}^{off} and f_{CJ}^{off} , only the error due to renormalization was considered as their off-shell parameters are fixed in our trials.

IV. RESULTS

A. Inclusive data description

Figure 4 shows the resulting fit compared to the experimental data using SF densities (GCF-LC densities are shown in Appendices). We performed eight individual fits, switching between the two F_2^n/F_2^p models, constant-in- \tilde{x} or linear-in- \tilde{x} off-shell parametrizations, and using either SF or GCF-LC densities. We also show calculations using f_{KP}^{off} and f_{CI}^{off} . For completeness, Fig. 5 shows the inferred off-shell functions for $f_{\text{const}}^{\text{off}}$ and $f_{\text{lin}x}^{\text{off}}$ for the different convolution frameworks, along with f_{KP}^{off} [22] and f_{CJ}^{off} [46]. While f_{KP}^{off} and f_{CJ}^{off} demand zero-crossings in the off-shell function to preserve baryon charge and momentum sum rules, we do not consider this constraint as we restrict our study for x > 0.17.

From the χ^2 values in Table I and the similarity of the different models in Fig. 4, it is clear that the present ³He and ²H data cannot definitively discriminate between the different nucleon motion models (i.e., SF vs GCF-LC) or different neutron structure functions. The data can be adequately



FIG. 4. Convolution results after χ^2 -minimization procedure using the SF approximation. 1 σ confidence bands are displayed for each trial, and each band is shown with the renormalization inferred for ²H and ³He. The result of no off-shell modification (grey bands) are also shown with the renormalization preferred for that given fit. The data used in the minimization (²H data from [49] and ³He data of [6]) are shown as filled circles. Open circles denote data at W < 1.4 GeV, which were not used in the fit. [Top row, (a)–(d)] Results for $F_2^d/(F_2^p + F_2^n)$ with Segarra *et al.* F_2^n/F_2^p . [2nd row, (e)–(h)] Results for F_2^{3He}/F_2^d with Segarra *et al.* F_2^n/F_2^p . [3rd row, (i)–(l)] Results for $F_2^d/(F_2^p + F_2^n)$ with Arrington F_2^n/F_2^p . [Bottom row, (m)–(p)] Results for F_2^{3He}/F_2^d with Arrington F_2^n/F_2^p . In each row, results are shown for different off-shell functions used, in order from left to right: $f_{\text{const}}^{\text{off}}$ [(a),(e),(i),(m)], $f_{\text{lin}x}^{\text{off}}$ [(b),(f),(j),(n)], f_{CJ}^{off} [(c),(g),(k),(o)], f_{KP}^{off} [(d),(h),(l),(p)]. All curves are calculated and extrapolated with the same Q^2 as the data for ²H and ³He.

reproduced even with very different off-shell models. While accounting for nucleon modification improve the reproduction



FIG. 5. Off-shell functions $f^{\text{off}}(\tilde{x})$ resulting from χ^2 -minimization procedure with SF (a) and LC (b) approximations. The blue and red curves were minimization trials using a F_2^n/F_2^p fit to two recent predictions by Segarra *et al.* [21] (Seg.) and Arrington *et al.* [47] (Arr.), respectively. The two black lines are the off-shell functions as described in [22,46] and were taken as fixed for the minimization procedure, which is why they are identical for both convolution frameworks. 1 σ confidence bands are displayed for each trial.

of the data, in certain cases it can also be reproduced by a "no off-shell modification" calculation, i.e., with $f^{\text{off}} = 0$ (see Table I).

Table I and Fig. 4 show a significant systematic improvement for all minimizations when using the Segarra et al. F_2^n/F_2^p parametrization (blue curves), particularly for ³He. Using f_{KP}^{off} , the calculation does not describe the high- x_B ²H data. This is not unexpected as their off-shell function was not fit to BONUS data nor to high- x_B deuterium data (≥ 0.8) [22]. f_{KP}^{off} does describe the ³He EMC data markedly well due to the global nature of their analysis, which captures the general EMC trend in a wide range of nuclei. Similarly, when using f_{CI}^{off} , the calculation struggles as much as other models to accurately predict the ³He EMC ratio. However, we note that their global fit does not consider A > 2 nuclear DIS data. Again, the agreement improves with the use of the Segarra et al. F_2^n/F_2^p . The resulting off-shell functions from fits with the Segarra et al. F_2^n/F_2^p (blue curves) and Arrington (red curves) are independent of the nucleon motion model (SF or GCF-LC), see Fig. 5.

The GCF-LC framework does just as well at describing the ³He data and deuterium data (see Appendices), again, with improvement with the use of the Segarra *et al.* F_2^n/F_2^p . In the GCF-LC framework, the high- x_B ³He data not used in

TABLE I. Reduced χ^2 results of 20 trials with various model assumptions. $\tilde{\rho}(\alpha, v)$ refers to the approximation that was used for the lightcone virtuality and momentum distribution to calculate Eq. (A1). Similarly, f^{off} refers to the off-shell functional form used, including a no-modification assumption ($f^{\text{off}} = 0$). There is a systematic increase in χ^2 when using F_2^n/F_2^p of Arrington [47]. There is also an increase when using GCF-LC approximation to $\tilde{\rho}(\alpha, v)$. We note that when using the KP and CJ off-shell parametrization there are no free parameters fit to data and the quoted χ^2 values show the quality of their description of the data without any minimization procedure.

| $\tilde{\rho}(\alpha,\nu)$ | $F_2^n/F_2^p(\tilde{x})$ | $f^{\rm off}(\tilde{x})$ | χ_d^2 | $\chi^2_{^3He}$ | χ^2_{tot} /d.o.f. |
|----------------------------|--------------------------|--------------------------|------------|-----------------|------------------------|
| SF | Seg. | Constx | 7.4 | 12.4 | 19.8/31 = 0.63 |
| | | Linx | 7.7 | 7.7 | 15.4/30 = 0.51 |
| | | KP | 12.9 | 12.1 | 25/32 = 0.78 |
| | | CJ | 6.6 | 23.4 | 30/32 = 0.94 |
| | | No Mod. | 5.3 | 18.2 | 23.5/32 = 0.73 |
| | Arr. | Constx | 17.4 | 69.1 | 86.5/31 = 2.79 |
| | | Linx | 25.9 | 16.0 | 41.9/30 = 1.40 |
| | | KP | 12.1 | 21.4 | 33.5/32 = 1.05 |
| | | CJ | 6.7 | 111.9 | 118.6/32 = 3.71 |
| | | No Mod. | 5.2 | 98.2 | 103.4/32 = 3.23 |
| GCF-LC | Seg. | Constx | 8.4 | 19.2 | 27.6/31 = 0.89 |
| | | Linx | 7.2 | 16.4 | 23.6/30 = 0.79 |
| | | KP | 9.8 | 10.5 | 20.3/32 = 0.63 |
| | | CJ | 11.8 | 26.8 | 38.6/32 = 1.21 |
| | | No Mod. | 6.3 | 25.0 | 31.3/32 = 0.98 |
| | Arr. | Constx | 22.9 | 69.3 | 92.2/31 = 2.97 |
| | | Linx | 25.4 | 53.1 | 78.5/30 = 2.62 |
| | | KP | 8.7 | 64.5 | 73.2/32 = 2.29 |
| | | CJ | 12.9 | 110.8 | 123.7/32 = 3.87 |
| | | No Mod. | 6.2 | 106.2 | 112.4/32 = 3.51 |

the fitting procedure (due to having low W) is not as well described as in the SF framework. We also note that the f_{CI}^{off}

did not use ³He data as a constraint, and, therefore, struggles at describing the data, especially at high x_B .

B. SRC contribution to nucleon modification

In addition to being small in magnitude, the resulting off-shell function is dependent on the exact form of F_2^n/F_2^p . However, the contributions of mean-field nucleons and SRC nucleons to the structure function and off-shell modification are model independent.

Using the inferred parameters from the global fit as described above, we can now separate the contributions of the mean-field and SRC nucleons to the EMC effect. To this end we constructed $F_2^A = F_2^A(MF) + F_2^A(SRC)$ by splitting the integral in Eq. (A1) to contributions of Mean-Field and SRC nucleons. This separation is natural for the GCF-LC approach. For the SF based approach this is done by assigning all nucleons with momenta above a cutoff of 240 MeV/c as members of SRC pairs. Our findings are largely insensitive to the exact cutoff momentum we choose.

Figure 6 shows the ratio of the structure functions: $[F_2^{{}^{3}He}(SRC)]/[F_2^{{}^{3}He}(MF)]$ and $[F_2^d(MF)]/[F_2^d(SRC)]$ (LC calculations are similar and can be found in the Appendices). As expected, mean-field nucleons account for most of the structure function in Eq. (A1), except at very high x_B where nucleon motion effects are important and therefore the contribution of SRCs becomes significant. This is to be expected as SRC nucleons account for a small fraction of the nuclear wave function, especially in deuterium.

Next we explicitly examine the contribution of mean-field and SRC nucleons to the off-shell modification effect in the EMC. This is done by defining the off-shell decomposition as $F_2^A(\text{off-shell}) = F_2^A(\text{full}) - F_2^A(\text{no off-shell})$, where $F_2^A(\text{full})$ is calculated using Eq. (A1) and $F_2^A(\text{no off-shell})$ is calculated using the same equation but by setting $f^{\text{off}}(\tilde{x}) = 0$.



FIG. 6. Ratio of SRC contribution to MF contribution of the structure function using SF approximation. See text for details. [Top row, (a)–(d)] Ratio on F_2^d . [Bottom row, (e)–(h)] Ratio on $F_2^{^{3He}}$. In each row, results are shown for different off-shell functions used, in order from left to right: $f_{\text{const}}^{\text{off}}$ [(a),(e)], f_{cJ}^{off} [(c),(g)], f_{KP}^{off} [(d),(h)]. 1 σ confidence bands are displayed for each trial. Curves are shown with $Q^2 = 5 \text{ GeV}^2$.



FIG. 7. Decomposition of F_2^A (off-shell) for various model assumptions within the SF approximation. [Top row, (a)–(d)] Decomposition for $F_2^d/(F_2^p + F_2^n)$ with Segara *et al.* F_2^n/F_2^p . [2nd row, (e)–(h)] Decomposition for $F_2^{^{3He}}/F_2^d$ with Segara *et al.* F_2^n/F_2^p . [3rd row, (i)–(l)] Decomposition for $F_2^d/(F_2^p + F_2^n)$ with Arrington F_2^n/F_2^p . [Bottom row, (m)–(p)] Decomposition for $F_2^{^{3He}}/F_2^d$ with Arrington F_2^n/F_2^p . In each row, decompositions are shown for different off-shell functions used, in order from left to right: $f_{\text{const}}^{\text{off}}$ [(a),(e),(i),(m)], $f_{\text{lin}x}^{\text{off}}$ [(b),(f),(j),(n)], f_{CJ}^{off} [(c),(g),(k),(o)], f_{KP}^{off} [(d),(h),(1),(p)]. Solid black lines represent the full off-shell contribution. Dashed blue lines are the contribution due to SRC nucleons (>240 MeV/c in the SF assumption). Similarly, dotted red lines are the contribution due to MF nucleons (<240 MeV/c). 1σ confidence bands are displayed for each trial. Curves for GCF-LC approximation can be viewed in the Appendices. Curves are shown at $Q^2 = 5 \text{ GeV}^2$.

Figure 7 shows the decomposition of F_2^A (off-shell) into SRC and mean-field nucleons within the SF approach (LC calculations are qualitatively similar and can be found in the

Appendices). While high-momentum nucleons did not significantly contribute to the full convolution ratio in Fig. 6, these nucleons dominate the off-shell modification function



FIG. 8. Predictions of $\frac{F_2^{>H}}{F_2^d}$ using our convolution framework with the universal off-shell modification constrained from ²H and ³He data: [Top row, (a)–(d)] SF convolution, [Bottom row, (e)–(h)] GCF-LC convolution. In each row, results are shown for different off-shell functions used, in order from left to right: $f_{\text{const}}^{\text{off}}$ [(a),(e)], $f_{\text{lin}x}^{\text{off}}$ [(b),(f)], f_{CJ}^{off} [(c),(g)], f_{KP}^{off} [(d),(h)]. 1 σ confidence bands are displayed for each prediction. See text for details. All curves are shown for MARATHON kinematics, i.e., $Q^2 = 14 \cdot x_B$ [GeV²].



FIG. 9. [Top row, (a)–(c)] Predictions of the ratio of the bound proton structure function in deuterium to the free proton structure function as a function of α at a fixed $\tilde{x} = 0.6$. [Bottom row, (d)–(f)] Predictions of the double ratio of bound-to-free proton structure function for $\tilde{x} = 0.6$ to $\tilde{x} = 0.3$. 1 σ confidence bands are displayed for each prediction. In the bottom panels, predictions for models with $f_{\text{const}}^{\text{off}}$ yield a double ratio of 1, as the modification is constant in \tilde{x} . See text for details. Curves are shown at $Q^2 = 5 \text{ GeV}^2$ and for $\mathbf{p}_{\mathbf{T}} = \mathbf{0}$. In (c) and (f), finely dotted lines use f_{KP}^{off} and dashed-dotted lines use f_{CI}^{off} .

(i.e., the dashed blue lines track the solid black lines closely, especially at high x_B) in all models even though the off-shell behavior is different for each model.

This holds true even in deuterium at high x_B , although at $x_B \sim 0.6$, the mean-field and SRC contributions are closer to 1:1. This is still surprising given the high-momenta fraction of the nuclear momentum-distribution is only $O(\sim 4\%)$ [51]. Adding to this surprise is the feature that a significant contribution to the wave function comes from np separations larger than the range of the nuclear forces [52].

Furthermore, in the results shown here using the SF approach, the momentum sum rule is violated by ~1%. While small, this violation still induces an artificial EMC effect, thereby reducing the strength of the actual off-shell contribution to the structure function (i.e., the absolute *y* scale of Fig. 7). Alternatively, in the LC approach, the sum rules are manifestly satisfied, and the extracted off-shell contribution is much larger for the models of $F_2^n/F_2^p|_{Seg.}$ by a factor of about 1.5 – 3 (see Appendices).

Our findings are robust to the exact underlying off-shell function used in Eq. (A1), even though $f^{\text{off}}(\tilde{x})$ (Fig. 5) varies

dramatically among the models. Therefore, the results shown in Fig. 7 contradict the recent claims of Ref. [53], where the SRC UMF was analyzed without proper separating its contributions from nucleon motion and modification effects. For completeness we note that the UMF extracted by Ref. [7,21] is reproduced with the convolution framework used here for ³He, see Appendices.

V. PREDICTING FORTHCOMING OBSERVABLES

While existing data cannot constrain F_2^n/F_2^p , here we show predictions F_2^{3H}/F_2^d , which was recently measured by the MARATHON collaboration [24], and should be sensitive to F_2^n . Figure 8 shows the convolution prediction for F_2^{3H}/F_2^d obtained using the constrained off-shell modification function and assuming isospin symmetry in the lightcone distributions. The different F_2^n/F_2^p parametrizations, which are both consistent with $F_2^{^{3H}}/F_2^d$ data, predict very different $F_2^{^{3H}}/F_2^d$ at high x_B that MARATHON can test. Still, as seen in Fig. 8, there are predictions of $F_2^{^{3H}}/F_2^d$, which overlap for very



FIG. 10. Comparison of $\tilde{\rho}_{p,n}^{2H}(\alpha, v)$ for the (a) GCF-LC formalism and (b) SF formalism. Due to isospin symmetry, the distributions are identical for proton and neutron.



FIG. 11. Comparison of $\tilde{\rho}_{p,n}^{^{3}He}(\alpha, v)$ for the (a), (c) GCF-LC formalism and (b), (d), SF formalism. Proton distributions are shown above [(a),(b)] and neutron distributions are shown below [(c),(d)].

different F_2^n/F_2^p and f^{off} behaviors. In particular, taking the f_{KP}^{off} with $F_2^n/F_2^p|_{\text{Seg.}}$ (blue dotted) and f_{CJ}^{off} with $F_2^n/F_2^p|_{\text{Arr.}}$ (red dash-dotted), yield overlapping predictions. This indicates a combined analysis of nuclear DIS data with forthcoming data by MARATHON will be needed to disentangle F_2^n/F_2^p and f^{off} , similar to efforts Ref. [22] has performed in the past.

While the MARATHON results will be very sensitive to F_2^n/F_2^p , they will be less sensitive to the exact nature of the off-shell modification function (f^{off}). This can however be tested in a new set of tagged deep inelastic scattering measurements off deuterium [25,26,54], which will study the dependence of the bound nucleon structure function on α , see Fig. 9:

$$F_2^{p*}(\tilde{x},\alpha) = F_2^p(\tilde{x})[1 + \langle v \rangle \mid_{\alpha} f^{\text{off}}(\tilde{x})], \qquad (14)$$

where $\langle v \rangle |_{\alpha}$ is the average fractional virtuality for the given α , see Figs. 10 and 11 for the phase space of the lightcone densities.

By taking a ratio of the bound-to-free proton structure function, one can access the off-shell modification function, and can examine the differences of the off-shell contribution at high \tilde{x} and low \tilde{x} , see Fig 9. The predictions here are similar to those made by Ref. [54] and will be directly tested by the LAD [26] and BAND [25] Collaborations. The latter already completed 50% data taking and results are anticipated soon. While predictions here are made for $\mathbf{p_T} = \mathbf{0}$, experiments will have some finite acceptance in $\mathbf{p_T}$. As seen in Fig 9, there are significant uncertainties due to uncertainties in F_2^n/F_2^p (red vs blue curves). However, after precise measurements on F_2^n/F_2^p by the MARATHON Collaboration [24], these uncertainties will be greatly reduced.

VI. SUMMARY

We present an extensive study of nucleon modification effects in nuclei using a convolution formalism and measurements of the EMC effect in deuterium and ³He. We examine a range of off-shell modification functions, free-neutron structure function models, and different treatments of nucleon motion effects. In all cases we find that nucleons in SRC pairs are the dominant contribution to nucleon modification effects in deuterium and ³He.

With upcoming precise measurements of 3 H, our study can be extended to test the isospin dependence of the universal off-shell modification function and the ability to use nuclear DIS data to constrain the free neutron structure function. We stress that an isospin-dependent EMC effect, in the sense of a different average modification for protons and neutrons, as, e.g., suggested by Refs. [11,12,55,56], can be obtained in all models discussed in this paper if the proton and neutron lightcone densities have different average virtualities. In addition we make predictions for new measurements of the bound nucleon structure function. These measurements will allow us to further constrain the elements of our model.

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FIG. 12. Labels for subplots signify fit results using model assumptions described in χ^2 -minimization procedure. (Top): fit quality to $F_2^d/(F_2^p + F_2^n)$ data. (Bottom): fit quality to $F_2^{^{3He}}/F_2^d$ data.

APPENDIX A: x²-MINIMIZATION PROCEDURE

We calculate $F_2^A(x_B)$ for ³He and ²H in a nuclear convolution approximation:

$$F_2^A(x_B, Q^2) = \int_{x_B}^A \frac{d\alpha}{\alpha} \int_{-\infty}^0 dv F_2^p(\tilde{x}, Q^2)$$
$$\times \left[Z \tilde{\rho}_p^A(\alpha, v) + N \tilde{\rho}_n^A(\alpha, v) \frac{F_2^n}{F_2^p}(\tilde{x}) \right] (1 + v f^{\text{off}}(\tilde{x})), \quad (A1)$$

and form the EMC ratios of $F_2^{^{3}He}/F_2^d$ to compare to [6] and $F_2^d/(F_2^p + F_2^n)$ to compare to [49] in order to infer parameters of interest (see below Sec. D on low Q^2 , high- x_B sensitivity for definition of \tilde{x} and discussion of finite- Q^2 effects). In particular, we would like to investigate the nucleon off-shell modification function $f^{\text{off}}(\tilde{x})$, which we assume to be the

same for neutrons and protons, as well as the same across all nuclei. The nucleon off-shell modification is assumed to be linear in virtuality $v = \frac{E^2 - p^2 - m_N^2}{m_N^2}$ (hence the [1 + vf] form). We consider three models:

$$f_{\text{const}}^{\text{out}}(\tilde{x}) = a_{\text{const}},$$

$$f_{\text{lin}\,x_B}^{\text{off}}(\tilde{x}) = a_{\text{lin}\,x_B} + b_{\text{lin}\,x_B} \cdot \tilde{x}$$

$$f_{KP,\,CJ}^{\text{off}}(\tilde{x}) = C(\tilde{x} - x_0)(\tilde{x} - x_1)(1 + x_0 - \tilde{x})$$

To perform the parameter inference, we first construct the structure function ratios [following Eq. (A1)] for each kinematic point $i(x_B, Q^2)$ in the data sets considered, i.e., $\frac{F_2^{3He}}{F_2^d}|_{i,theo}$ and $\frac{F_2^d}{F_2^{p}+F_2^n}|_{i,theo}$ using initial guesses on the parameters of interest. We also allow for a floating renormalization of the



FIG. 13. Equivalent figure as Fig. 4 in the main text, but for the lightcone convolution approximation. Convolution results after χ^2 -minimization procedure. 1 σ confidence bands are displayed for each trial, and each band is shown with the renormalization inferred for ²H and ³He. The result of no off-shell modification (grey bands) are also shown with the renormalization preferred for that given fit. The data used in the minimization (²H data from [49] and ³He data of [6]) are shown as filled circles. Open circles denote data at W < 1.4 GeV, which were not used in the fit. [Top row, (a)–(d)] results for $F_2^{d}/(F_2^p + F_2^n)$ with Segarra *et al.* F_2^n/F_2^p . [2nd row, (e)–(h)] Results for F_2^{3He}/F_2^d with Segarra *et al.* F_2^n/F_2^p . [3rd row, (i)–(l)] Results for $F_2^{d}/(F_2^p + F_2^n)$ with Arrington F_2^n/F_2^p . [Bottom row, (m)–(p)] Results for F_2^{3He}/F_2^d with Arrington F_2^n/F_2^p . In each row, results are shown for different off-shell functions used, in order from left to right: $f_{\text{const}}^{\text{off}}$ [(d),(h),(l),(p)]. All curves are calculated and extrapolated with the same Q^2 as the data for ²H and ³He.

data sets, N_B for [49] and N_S for [6]. We then calculate a χ^2 for the current parameter assumptions $(f^{\text{off}}(\tilde{x}), N_B, N_S)$:

$$\chi^{2} = \sum_{i \in {}^{2}H} \left(\frac{N_{B} \cdot \frac{F_{2}^{d}}{F_{2}^{p} + F_{2}^{n}}|_{i,theo} - \frac{F_{2}^{d}}{F_{2}^{p} + F_{2}^{n}}|_{i,meas}}{\sigma_{i}} \right)^{2} + \sum_{i \in {}^{3}He} \left(\frac{N_{S} \cdot \frac{F_{2}^{3}He}{F_{2}^{d}}|_{i,theo} - \frac{F_{2}^{3}He}{F_{2}^{d}}|_{i,meas}}{\sigma_{i}} \right)^{2}$$

$$+\left(\frac{N_B-1}{\sigma_{\text{norm},B}}\right)^2 + \left(\frac{N_S-1}{\sigma_{\text{norm},S}}\right)^2,\tag{A2}$$

and minimize χ^2 to infer our parameters utilizing Minuit2 MIGRAD algorithm. $F_2^p(\tilde{x}, Q^2)$ carries the only Q^2 dependence we assume in Eq. (A1). We calculated F_2^p using the GD11-P parameterization [48]. We also performed a study utilizing the Bosted-Christy [50] parameterizations of F_2^p, F_2^n to investigate resonance contributions (see below). $\tilde{\rho}_{p,n}^A(\alpha, v)$ are the lightcone distributions for protons and neutrons in a given nucleus A. The minimization procedure was performed



FIG. 14. Ratio of full (finite- Q^2) convolution integral to Bjorken-limit convolution integral. In blue, ratio of $F_2^{d}|_{\text{finite}}$ to $F_2^{d}|_{\text{Bjorken-limit}}$ is shown. In orange, double ratio of $[F_2^{^{3He}}|_{\text{finite}}/F_2^{d}|_{\text{finite}}]$ to $[F_2^{^{3He}}|_{\text{Bjorken-limit}}/F_2^{d}|_{\text{Bjorken-limit}}]$ is shown. (a) Spectral function convolution approximation. (b) Lightcone convolution approximation. To interpolate over a wide range of x_B values, a parameterization of the $Q^2(x_B)$ reach of each experiments (Deuterium and Helium-3 separately) was utilized.



FIG. 15. [Top, (a)–(d)] Convolution results using the finiteenergy expression of Eq. (D2) for \tilde{x} (Low-Q Convolution) and Bjorken frame of Eq. (D3) for \tilde{x} (High-Q Convolution) for deuterium and Helium-3. [Bottom, (e),(f)] The ratio of structure functions $F_2^A(x_B)$ calculated with Eq. (D2) to that calculated with Eq. (D3). While at high x_B , the ratio starts to diverge above 2%, we only consider data up to $x_B \sim 0.8$.

two times: using a spectral function approximation to $\tilde{\rho}(\alpha, v)$ and using the lightcone formalism (see main text for details).

 F_2^n/F_2^p is parameterized as $F_2^n/F_2^p(\tilde{x}) = a_{np}(1-\tilde{x})^{b_{np}} + c_{np}$, where there is no explicit Q^2 considered, except for the study with the Bosted-Christy parameterizations (see below). We fit this parameterization to two recent predictions by Segarra [21] and Arrington [47], and then perform the χ^2 minimization using each F_2^n/F_2^p prediction. We do not allow parameter variation of F_2^n/F_2^p in the minimization procedure with the two data sets considered. However, by taking two extreme predictions of F_2^n/F_2^p , we can study the sensitivity our results have to the exact nature of F_2^n/F_2^p . In the case of using $f_{KP,CJ}^{off}(\tilde{x})$, we fixed the parameters

In the case of using $f_{KP,CJ}^{\text{off}}(\tilde{x})$, we fixed the parameters of the off-shell function to those found in a minimization by [22] (f_{KP}^{off}) and by [46] (f_{CJ}^{off}) . We note that while the same off-shell parameterization is used by both groups, Ref. [22] considered a wide range of nuclear DIS data sets and [46] used DIS data only on the proton and deuterium to infer their off-shell function.



FIG. 16. The ratio of EMC ratios calculated with Eq. (E1) to that calculated with Eq. (D3). (a) The ratio of $(F_2^d/(F_2^n + F_2^p))|_{\text{Eq.E1}}/(F_2^d/(F_2^n + F_2^p))|_{\text{Eq.D3}}$ and (b) the ratio of $(F_2^{3He}/F_2^d)|_{\text{Eq.E1}}/(F_2^{3He}/F_2^d)|_{\text{Eq.D3}}$.

Sixteen minimization trials were presented in the main text for the various model assumptions:

(a) SF with $F_2^n/F_2^p|_{\text{Seg. with }} f_{\text{const}}^{\text{off}}$ (b) SF with $F_2^n/F_2^p|_{\text{Arr. with }} f_{\text{const}}^{\text{off}}$ (c) SF with $F_2^n/F_2^p|_{\text{Seg. with }} f_{\text{iin } x_B}^{\text{off}}$ (d) SF with $F_2^n/F_2^p|_{\text{Arr. with }} f_{\text{iin } x_B}^{\text{off}}$ (e) SF with $F_2^n/F_2^p|_{\text{Seg. with }} f_{KP}^{\text{off}}$ (f) SF with $F_2^n/F_2^p|_{\text{Arr. with }} f_{CJ}^{\text{off}}$ (g) SF with $F_2^n/F_2^p|_{\text{Arr. with }} f_{CJ}^{\text{off}}$ (i) GCF-LC with $F_2^n/F_2^p|_{\text{Arr. with }} f_{\text{const}}^{\text{off}}$ (j) GCF-LC with $F_2^n/F_2^p|_{\text{Seg. with }} f_{\text{const}}^{\text{off}}$ (k) GCF-LC with $F_2^n/F_2^p|_{\text{Seg. with }} f_{\text{iin } x_B}^{\text{off}}$ (l) GCF-LC with $F_2^n/F_2^p|_{\text{Seg. with }} f_{\text{iin } x_B}^{\text{off}}$ (n) GCF-LC with $F_2^n/F_2^p|_{\text{Arr. with }} f_{\text{iin } x_B}^{\text{off}}$ (n) GCF-LC with $F_2^n/F_2^p|_{\text{Seg. with }} f_{KP}^{\text{off}}$ (o) GCF-LC with $F_2^n/F_2^p|_{\text{Arr. with }} f_{KP}^{\text{off}}$ (o) GCF-LC with $F_2^n/F_2^p|_{\text{Arr. with }} f_{CJ}^{\text{off}}$ (p) GCF-LC with $F_2^n/F_2^p|_{\text{Arr. with }} f_{CJ}^{\text{off}}$



FIG. 17. Convolution results for ³He shown as the universal modification function as described in [21], which was unable to decompose nucleon off-shell and motion effects. All curves are calculated and extrapolated with the same Q^2 as the data for ³He. (a) Uses the spectral function approach, and (b) uses the lightcone approach to the convolution.



FIG. 18. Minimization results and analysis conclusions utilizing the Bosted-Christy parameterizations of F_2^p and F_2^n (solid lines) compared to a minimization trial with F_2^n/F_2^p from Segara [21] (shaded bands). Both trials used an off-shell function that was constant in x, f_{const}^{off} , and the spectral function approximation to the convolution. As was found when using F_2^n/F_2^p from Arrington [47], the resulting off-shell function extracted depends on the underlying neutron structure assumed. However, universal features still emerge, such as the MF dominance to the full structure function, and the SRC dominance of the off-shell effect. (a) Off-shell function extracted from minimization trial. (b) Calculation of $F_2^d/(F_2^p + F_2^n)$ with resulting parameters compared to BONUS data. (c) Calculation of $F_2^{^{3He}}/F_2^d$ with resulting parameters compared to Seely data. (d) SRC/MF fraction of $F_2^{^d}$. (e) SRC/MF fraction of $F_2^{^{3He}}$. (f) off-shell contributions to F_2^d . (g) Off-shell contributions to $F_2^{^{3He}}$.

where SF is a minimization trial that approximates $\tilde{\rho}(\alpha, v)$ with a spectral function, GCF-LC is a minimization trial that uses the lightcone formalism for $\tilde{\rho}(\alpha, v)$, $F_2^n/F_2^p|_{\text{Seg.}}$ is a minimization trial that uses F_2^n/F_2^p fitted to [21], and $F_2^n/F_2^p|_{\text{Arr.}}$ uses a fit to [47]. We performed and present additional iterations to investigate finite- Q^2 effects (see below).

APPENDIX B: SF AND GCF-LC COMPARISON

The distributions $\tilde{\rho}(\alpha, v)/\alpha$ of lightcone fraction and virtuality as shown below for deuterium in Fig. 10 and helium-3 in Fig. 11, using both the GCF lightcone formalism (GCF-LC) and the spectral function formalism (SF). We note that



FIG. 19. Decomposition of EMC ratios (Top: deuterium, Bottom: helium-3) for MF (red finely dotted lines) and SRC (blue dashed lines) nucleons, compared to the full (black solid lines) convolution. See section on radio decomposition for details on calculations. In all curves we see that MF dominates the ratio and the SRC contribution is only $\mathcal{O}(\sim 10\%)$. Labels for subplots signify fit results using model assumptions described in χ^2 -minimization procedure.

the largest deviations between these models occurs at large virtuality, in the SRC-dominated region. The SF model has increased probability of low- α nucleons relative to the GCF-LC model. In both formalisms, a momentum cutoff was placed at p = 1 GeV/c due to the expectation that assumptions would break down beyond this region. The hard cuts seen at large -v are the result of this cutoff, which is expressed differently in the GCF-LC model and the SF model.

Figure 2 shows the distribution $\tilde{\rho}(\alpha)/\alpha$ of the lightcone fraction for all nucleons (integrated over *v*), for deuterium and both protons and neutrons in helium-3. While the GCF-LC formalism produces lightcone fraction distributions that are symmetric around $\alpha = 1$, this symmetry is not manifest in

the SF formalism, resulting in the small momentum sum-rule violation mentioned in the main text.

APPENDIX C: QUALITY OF MODEL EXTRACTION

Each minimization trial is shown individually with the data used here with the resulting reduced χ^2 in Fig. 12, and see Fig. 13 for equivalent Fig. 4 but using the GCF-LC approach.

APPENDIX D: LOW Q^2 , HIGH- x_B SENSITIVITY

In Eq. (1) of the main text and here, the Bjorken-limit was already invoked $(Q^2, q \rightarrow \infty, x \text{ fixed})$. The full convolution



FIG. 20. Equivalent figure as Fig. 6 in the main text, but for the lightcone convolution approximation. Ratio of SRC contribution to MF contribution of the structure function. [Top row: (a)–(d)] Ratio on F_2^d . [Bottom row: (e)–(h)] Ratio on $F_2^{^3He}$. In each row, results are shown for different off-shell functions used, in order from left to right: $f_{\text{const}}^{\text{off}}$ [(a),(e)], $f_{\text{lin},x}^{\text{off}}$ [(b),(f)], f_{CJ}^{off} [(c),(g)], f_{KP}^{off} [(d),(h)]. 1 σ confidence bands are displayed for each trial. Curves are shown with $Q^2 = 5 \text{ GeV}^2$.

formula, as defined in [57] Eqs. (17) and (37), may be utilized to investigate finite- Q^2 effects. In order to study the size of these effects, we performed the convolution integral twice, once using the full formula including finite- Q^2 effects following Ref. [57], and once using the approximation of Eq. (1) with $\tilde{x} = \frac{x_B}{\alpha} \frac{Am_N}{m_A}$. We did this for both the spectral function and the lightcone convolution approximations. Although the data used in this analysis is at low-to-moderate Q^2 , we find that our calculations are relatively insensitive to finite- Q^2 effects ($\sim 1 - 2\%$), especially considering that we utilize structure function ratios, which suppress these effects (see Fig. 14).

Another way to estimate the effects of finite Q^2 is the definition of \tilde{x} used in the convolution. Defining $q = (v, 0, 0, -|\mathbf{q}|)$, we may express the momenta of the virtual photon and the struck nucleon in the frame:

$$q = (q_{-} = (q_{0} - q_{3}), q_{+} = (q_{0} + q_{3}), \mathbf{q_{t}} = 0)$$

$$p = (p_{-} = (p_{0} - p_{3})/m_{N}, p_{+} = (p_{0} + p_{3})/m_{N}, \mathbf{p_{t}}), (D1)$$

where in this frame, $q_0 = v$, $q_3 = |\mathbf{q}|$. Defining \tilde{x} :

$$\tilde{x} = \frac{Q^2}{2(q \cdot p)} = \frac{Q^2}{2([q_+ \cdot p_-]/2 + [q_- \cdot p_+]/2 - \mathbf{q_t} \cdot \mathbf{p_t})}$$
$$= \frac{Q^2}{[q_+ \cdot p_-] + [q_- \cdot p_+]}.$$
(D2)

In the Bjorken frame, $\frac{q_+}{q_-} \to 0$ such that $\tilde{x} \to Q^2/(q_- \cdot p_+)$. With fixed $x_B = Q^2/(2m_N \nu), x_B \to Q^2/m_N q_-$:

$$\tilde{x} = \frac{Q^2}{q_- \cdot p_+} = \frac{x_B}{p_+} m_N = \frac{x_B}{\alpha} \frac{Am_N}{m_A},$$
 (D3)

where $\alpha = Ap_+/m_A$. With this, we have arrived at the expression used in Eq. (1) in the main text. As the data considered in our fit is at finite- Q^2 , we may also directly use Eq. (D2) for \tilde{x} . We repeated our minimization procedures and no significant

difference was seen in the ratios $F_2^d/(F_2^p + F_2^n)$, $F_2^{^{3}He}/F_2^d$ (see Fig. 15).

APPENDIX E: TAGGED KINEMATICS

When considering deuterium, in PWIA, we can write $\tilde{x} = Q^2/(2q \cdot p)$ using the kinematics of the spectator nucleon to ensure that as $\tilde{x} \to 1$, $\tilde{W} \to m_N^2$. Given that the initial deuterium nucleus is at rest $(p_d = (m_d, \mathbf{0}))$ and the spectator nucleon is on-shell after the interaction:

$$\tilde{x}_{\text{tagged}} = \frac{Q^2}{2[\nu(m_d - E_r) + \mathbf{p}_r \cdot \mathbf{q}]},\tag{E1}$$

where $\mathbf{p}_r = -\mathbf{p}$ and $E_r = \sqrt{m_N^2 + |\mathbf{p}|^2}$. For the case of ³He, there are two-body breakup (2bbu) and three-body breakup (3bbu) channels that the resulting A - 1 system can exist in. Defining a similar definition of Eq. (E1), we can then look at the impact of this on the ratios $F_2^d/(F_2^p + F_2^n)$ and F_2^{3He}/F_2^d , see Fig. 16. In deuterium, the effect is on the order of ~2% at $x_B \sim 0.7$. When calculating $F_2^{^{3He}}$, it is a slightly larger effect, however it is not much larger than F_2^d , which is why the ratio of $(F_2^{^{3He}}/F_2^d)|_{\text{Eq.6}}/(F_2^{^{3He}}/F_2^d)|_{\text{Eq.5}}$ is small.

APPENDIX F: UNIVERSAL FUNCTION PREDICTION

We note that the UMF extracted by Ref. [7,21] is reproduced with the convolution framework used here for ³He, see Fig. 17.

APPENDIX G: LOW-W RESONANCE CONTRIBUTIONS

As the data considered in this analysis is at relatively low W, particularly at high x_B , we also investigated the contributions due to resonance effects in the underlying free structure functions F_2^p and F_2^n . By using the Bosted-Christy param-



FIG. 21. Decomposition of off-shell contribution to ratio (Top: deuterium, Bottom: helium-3) for MF (red finely dotted lines) and SRC (blue dashed lines) nucleons, compared to the full (black solid lines) convolution. See section on off-shell decomposition for details on calculations. In most all curves we see that now SRC dominates the contribution at high x_B and the MF contribution is small. Labels for subplots signify fit results using model assumptions described in the section on χ^2 -minimization procedure.

eterizations of F_2^p and F_2^n [50], resonance contributions to our convolution calculation of F_2^d and $F_2^{^3He}$ are considered. Furthermore, by utilizing these parameterizations, we allow for the separate Q^2 dependence of F_2^n and F_2^p in the ratio $F_2^n(\tilde{x}, Q^2)/F_2^n(\tilde{x}, Q^2)$ (in the main text it is assumed the Q^2 dependence in the ratio is negligible).

We repeated our entire analysis to infer the off-shell function with the Bosted-Christy parameterizations of $F_2^p(\tilde{x}, Q^2)$ and $F_2^n(\tilde{x}, Q^2)$ here. To investigate the sensitivity to resonance contributions, we only consider an off-shell function that is constant in *x*, $f_{\text{const}}^{\text{off}}$ and only consider the spectral function approximation to the convolution integral. We find a good description of the data, $\chi^2/\text{dof} = 25.5/31 \approx 0.82$ [compared to iteration (a) where we achieved a $\chi^2/\text{dof} = 19.8/31 \approx 0.63$]. Comparing to iteration (a), where we used the same off-shell functional form and spectral function approximation, we find consistent results for all of our findings in the main text, see Fig. 18. While the off-shell function is slightly reduced in magnitude, we find still that (1) the SRC/MF contribution to the structure function is small and (2) SRC nucleons play a large role in the off-shell contribution to the structure function.

APPENDIX H: CONVOLUTION DECOMPOSITION

1. Ratio decomposition

In calculating Eq. (A1), we would like to understand the contribution of low- and high-momentum nucle-



FIG. 22. Ratio of of-fshell contribution in Helium-3 to the structure function in the GCF-LC framework to SF framework. The ratio is always larger than one, signifying that the off-shell effect is larger in the GCF-LC framework than SF framework, as expected due to the momentum sum rule violation in the SF framework. All blue lines use $F_2^n/F_2^p|_{\text{Seg.}}$ [(a),(b),(e),(g)], whereas red lines use $F_2^n/F_2^p|_{\text{Arr.}}$ [(c),(d),(f),(h)]. The off-shell functional form utilized is written in each subfigure.

ons to the full nuclear structure function. In the GCF-LC formalism, $\tilde{\rho}(\alpha, v)$ is already factorized into meanfield/low-momentum (MF) and short-range-correlation/highmomentum (SRC) contributions, see Ref. [38]. In the SF approximation, we simply choose integral bounds of the spectral function for the momentum range of interest (we



FIG. 23. Equivalent figure as Fig. 7 in the main text, but for the lightcone convolution approximation. Decomposition of F_2^A (off-shell) for various model assumptions. [Top row, (a)–(d)] Decomposition for $F_2^d/(F_2^p + F_2^n)$ with Segara *et al.* F_2^n/F_2^p . [2nd row, (e)–(h)] Decomposition for $F_2^{^3He}/F_2^d$ with Segara *et al.* F_2^n/F_2^p . [3rd row, (i)–(l)] Decomposition for $F_2^d/(F_2^p + F_2^n)$ with Arrington F_2^n/F_2^p . [Bottom row, (m)–(p)] Decomposition for $F_2^{^{3He}}/F_2^d$ with Arrington F_2^n/F_2^p . In each row, decompositions are shown for different off-shell functions used, in order from left to right: $f_{\text{const}}^{\text{off}}$ [(a),(e),(i),(m)], $f_{\text{in } x}^{\text{off}}$ [(b),(f),(j),(n)], f_{CJ}^{off} [(c),(g),(k),(o)], f_{KP}^{off} [(d),(h),(l),(p)]. Solid black lines represent the full off-shell contribution. Dashed blue lines are the contribution due to SRC nucleons (>240 MeV/c in the SF assumption). Similarly, dotted red lines are the contribution due to MF nucleons (<240 MeV/c). 1 σ confidence bands are displayed for each trial. Curves are shown at $Q^2 = 5 \text{ GeV}^2$.

chose 240 MeV/c):

$$\tilde{\rho}_{N,SF}^{SRC,A}(\alpha, v) = \int_{|\mathbf{p}|=240 \text{MeV/c}}^{\infty} dE d^3 \mathbf{p} \ S_N^A(E, p)$$
$$\times \cdot \frac{E + p_z}{E} \cdot \frac{m_A}{m_N A} \,\delta\left(\frac{m_N \alpha}{m_A} - \frac{p^+}{P^+}\right)$$
$$\times \delta\left(v - \frac{E^2 - |\mathbf{p}|^2 - m_N^2}{m_N^2}\right),$$

and similarly, a $\tilde{\rho}_{N,SF}^{MF,A}(\alpha, v)$ is defined by integrating from 0 - 240 MeV/c. Substituting in $\tilde{\rho}_{N}^{SRC,A}(\alpha, v)$ into Eq. (A1), we can calculate $F_{2}^{SRC,A}$, the contribution to F_{2}^{A} by SRC nucleons. We note that $F_{2}^{MF,A} + F_{2}^{SRC,A} = F_{2}^{A}$. Figure 19 shows the individual contributions to F_{2}^{A} by MF and SRC nucleons (in the main text, the ratio of SRC/MF was taken, and see Fig. 20 for equivalent Fig. 6 but using the GCF-LC approach).

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2. Off-shell decomposition

We would also like to understand the role of high momentum nucleons in the of-fshell effect $f^{\text{off}}(\tilde{x})$ and how that contributes to the overall structure function. We can estimate the of-fshell contribution to the structure function by taking F_2^A (off-shell) = F_2^A (full) – F_2^A (no-offshell), where we calculate F_2^A (full) by usual means of Eq. (A1) and F_2^A (no-offshell) is calculated by setting $f^{off}(\tilde{x}) = 0$ in Eq. (A1). We then can look again at the contributions due to MF and SRC nucleons to F_2^A (off-shell). Figure 21 shows the individual contributions to $\overline{F_2^A}$ (off-shell) by MF and SRC nucleons (in the main text, only a select few curves were shown). As was noted in the main text, in the SF framework, there is a slight momentum sum rule violation in helium-3, which induces an artificial off-shell effect. In Fig. 22, we look at the ratio of the off-shell effect in helium-3 using the GCF-LC approach and the SF approach. The GCF-LC framework requires a larger off-shell effect, as expected due to manifestly satisfying the momentum sum rule. See Fig. 23 for equivalent Fig. 7 but for the GCF-LC approach.

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