ANALYTICAL DESIGN OF A WAVEGUIDE IRIS/STUB TUNING COUPLER TO AN OVERCOUPLED SUPERCONDUCTING CAVITY

Haipeng Wang*

TJNAF, Newport News, VA 23606, USA

Abstract

The high RF power test of a superconducting cavity without beam loading requires a variable coupling scheme. For a fixed power coupler and a finite source power, one needs to increase the external Q . A 3-stub tuner placed between the doorknob transition and an iris plate inside of WR975 waveguide has been developed for the SNS cryomodule test facility (CMTF). This paper describes the theoretical analysis, calculation by equivalent circuits and the coupling scale related to the stub tuning and the iris size. A copper model bench measurement and a 3D computer simulation proved the principle and some of the parameters. A factor of 100 over $Q_{\text{ext}}=7 \times 10^5$ has been achieved when implemented in the cryomodule test.

INTRODUCTION

The external quality factor $Q_{s,\text{ext}}$ of the fundamental power coupler (FPC) to a superconducting cavity is normally designed much lower than the cavity's intrinsic quality factor Q_s in order to match the input power to the beam load. For example, $Q_{s,\text{ext}}=10^5 \sim 10^7$, $Q_s=10^9 \sim 10^{10}$. That means the coupling co-efficient $\beta_s=Q_s/Q_{s,\text{ext}}$ from FPC to cavity is always heavily over-coupled $\beta_s \gg 1$. A common high power type FPC was also designed in a fixed coupling in order to handle a high power and save cost. When the cavity cryomodule is under the final high power test without a beam loading, most of forward power is going to reflect back and to dump into the klystron's circulator. Using a finite klystron power to achieve a high gradient field in the cavity, one needs to increase the equivalent external Q ($Q_{\text{eq},\text{ext}}$) by 1~3 order of magnitude, up to the maximum level of microphonics. A simple and common solution is to use a 3-stub tuner on the input power waveguide. Normally this tuning mechanism can only change $Q_{\text{eq},\text{ext}}$ about 1 order. By adding an iris plate upstream to klystron, like in the Figures 1& 2, from the following analysis, one can get 2 orders higher. Combining the 3-stub tuning capability, the coupling of $\beta_{\text{eq}}=Q_s/Q_{\text{eq},\text{ext}}$ can be variable. Here we define loaded $Q_{\text{sl}}=Q_s/(1+\beta_{\text{eq}})$. This mechanism is very attractive for an energy recovery recirculating linac (ERL). When the beam energy is returned to the cavity, the beam loading is gone. A higher external Q will save more klystron power from its circulator. Using a variable coupling, a same cavity can be used for both beam acceleration and storage. It can also help in helium

processing to bring more power to the cavity for destroying the field emitters. In the CMTF, using a 3-stub tuner only was the usual case for small Q external changes.

Figure 1: Iris/stub tuner design layout for SNS cryomodule tests.

Figure 2: An iris plate installed next to the stub tuner for a 15kW CW klystron system at TJNAF.

EQUIVALENT CIRCUIT ANALYSIS

The waveguide section between the iris plate and the superconducting (sc) cavity detuning short can be treated as a low- Q coupling resonator. The power coupling from klystron to the sc cavity will be two-stage impedance transforming (see Figure 3). The sc cavity loaded Q can be deduced as [1]:

Figure 3: Resonator coupling equivalent circuit.

* email: haipeng@jlab.org.

$$Q_{SL} = \frac{Q_s(1 + \beta_g) - Q_s\delta_s + Q_c - Q_c\delta_c}{1 + \beta_g + \beta_s - Q_s\delta_s Q_c\delta_c} \quad (1)$$

Here

$$\omega_c^2 = \frac{1}{L_c C_c} \quad \omega_s^2 = \frac{1}{L_s C_s} \quad Q_c = \frac{\omega L_c}{R_c} \quad Q_s = \frac{\omega L_s}{R_s} \quad (2)$$

$$\beta_g = \frac{\omega^2 M_g^2}{R_c R_g} \quad \beta_s = \frac{\omega^2 M_s^2}{R_c R_s} \quad \delta_c = 1 - \frac{\omega_c^2}{\omega^2} \quad \delta_s = 1 - \frac{\omega_s^2}{\omega^2} \quad (3)$$

Using the fact that mostly $Q_s \gg Q_c \gg Q_s\delta_s \gg Q_c\delta_c$, (1) can be simplified as:

$$\frac{Q_{eq,ext}}{Q_{s,ext}} = \frac{\beta_s}{\beta_{eq}} = \frac{1 + \beta_g}{1 - \frac{Q_s\delta_s Q_c\delta_c}{\beta_s}} = \frac{1 + Q_c/Q_{c,ext}}{1 - Q_{s,ext}\delta_s Q_c\delta_c} \quad (4)$$

We define the Q_c is the coupling cavity intrinsic Q. $Q_{c,ext}$ is the iris coupling external Q to the coupling cavity. The relative frequency detuning for sc cavity δ_s is normally limited by the static tuner and microphonics' level. However, stub tuning can change the relative frequency of coupling cavity δ_c , so as to change the $Q_{eq,ext}/Q_{s,ext}$. Note that this detuning requires $Q_{s,ext}\delta_s Q_c\delta_c < 1$. That means stub frequency detuning for the resonance coupling condition has to be:

$$\Delta f_c < \frac{f^2}{4Q_{s,ext}Q_c\Delta f_s} \quad (5)$$

Here f is the klystron operating frequency. For example, for a SNS medium beta cavity, $Q_{s,ext} = 7.3 \times 10^5$, $f = 805$ MHz, assumed $\Delta f_s = 10$ Hz, $Q_c = 1 \times 10^3$. Δf_c must be less than 22 MHz. The Q_c determines the sensitivity of stub tuning. If the Q_c can be made high enough, a fast tuner can be used to compensate the Lorenz force detuning and microphonics noise. From Equation (4), we can see that this iris/stub tuning coupler can only increase equivalent external Q or $Q_{eq,ext} > Q_{s,ext}$.

People worry about the power loss of coupling cavity P_c relative to the power loss in the sc cavity P_s . It can be found out [1] that it mainly depends on the sc cavity's microphonics' level. Figure 3 shows this calculation.

$$\frac{P_c}{P_s} = \frac{Q_{s,ext}}{Q_s} \left(1 + 4Q_s^2 \frac{\Delta f_s^2}{f^2} \right) \quad (6)$$

Figure 3. Power loss ratio in the coupling cavity.

The $Q_{c,ext}$ in Equation (4) depends on the iris hole's size, position and thickness. From the analytical calculation of next section, the external Q enhancement factor can be plotted as the function of iris diameter (Figure 4).

Figure 4: Analytical calculation verse one measured data.

IRIS COUPLING CALCULATION

The iris hole coupling to a rectangular waveguide $Q_{c,ext}$ can be done by a 3D computer simulation like MAFIA or Analyst (Omega3). The first approach I took is the analytical solution. The susceptance of an iris inside of waveguide is [2]:

$$\frac{B}{Y_0} = \frac{\lambda_g}{a} \left[\frac{\pi b}{24d j_1^2} - 1 + A_1 - \left(\frac{a}{\lambda} \right)^2 A_2 \right] \quad (7)$$

With an iris thickness (Figure 5) correction:

$$\frac{B_a}{Y_0} = \frac{B}{2Y_0} + \frac{|Y_0'|}{Y_0} \tanh \frac{\pi}{|\lambda_g'|} \quad \frac{B_b}{Y_0} = \frac{|Y_0'|}{Y_0} \csc h \frac{2\pi}{|\lambda_g'|} \quad (8)$$

Here Y_0 is the shunt conductance of waveguide. The j_1 , A_1 , A_2 , and Y_0' , λ_g' are all the functions of d/a , see Ref. [2] for detail.

Q external of an iris coupling to a TE₁₀x rectangular cavity can be deduced from Ref. [3] by the circuit transformation of Figure 6:

$$Q_{ext} = \left(\frac{B}{Y_0} \right)^2 \left[\frac{\pi}{2} \frac{1}{1 - (\lambda/2a)^2} + \frac{Y_0}{B} \right] \quad (9)$$

With an iris thickness correction:

$$Q_{c,ext} = \left(\frac{B_a}{Y_0} \right)^2 \frac{\pi}{2} \frac{1}{1 - \left(\frac{\lambda}{2a} \right)^2} \left(\frac{B_a + 2B_b}{B_b} \right)^2 \quad (10)$$

There is another formula from Collin [4] for the case of without iris thickness:

$$Q_{c,ext} = \frac{9}{4\pi} \frac{b^2 c (a^2 + c^2) \lambda}{d^6 \sqrt{1 - (\lambda/2c)^2}} \quad (11)$$

Here a , b and c is waveguide width, height and length respectively. The d is the iris hole diameter.

In Figure 7, I compare two analytical methods, MIT's Equations (7)~(10) and Collin's Equation (11), with a

Analyst 3D simulation [5]. The simulation used Balleyguier's method [6]. The simulation has confirmed

Figure 5: Iris without (top) and with (bottom) thickness simulation inside of a TE₁₀ rectangular waveguide.

Figure 6: Equivalent circuit transformation from an iris-coupled to a short-circuit waveguide cavity.

that the detail of meshing around the iris hole is important. The thickness of the iris has also a significant susceptance contributed to the $Q_{c,ext}$'s calculation.

Figure 7: Q external calculation for an iris hole coupling to a TE₁₀x rectangular waveguide resonator.

IRIS POSITION DETERMINATION

The position of the iris plate along the waveguide has to be at the voltage minima of standing wave (SW) when the cavity/coupling system is on resonance. So the iris inductance will be effectively at the maximum SW current position. Also the coupling waveguide will be in the TE_{01n} mode resonant frequency when the waveguide length $c=n\lambda_g/2$. For a waveguide coupling to a normal conducting cavity, like a copper or a room temperature niobium cavity, the “detuned short” position is also the voltage minimum position in resonance. It can be explained by the voltage reflection coefficient, because of $\beta \ll 1$:

$$\Gamma(\omega) = \frac{\beta - 1 - iQ_0\delta}{\beta + 1 + iQ_0\delta} \quad \delta = \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \quad (12)$$

When the cavity changes from normal conducting state to superconducting state, the coupling coefficient changes from $\beta \ll 1$ to $\beta \gg 1$. The voltage minimum position at resonance will be changed by $\lambda_g/4$ (90°). It is important to incorporate this change in the design. For the SNS medium beta cavity coupling, the iris position was determined by a computer 3D simulation, then by a bench measurement on a model. Using a slot-line waveguide (or a hole array on the centerline) coupled to a copper cavity, I measured the SW profile. From the plot in Figure 8, I got that the distance from the door-knob center to the first V_{min} is 52.6cm. The HFSS simulation from Y. Kang is 52.7cm [7]. Both of them are for the copper cavity. The iris position in the actual design was pulled back by $3/4\lambda_g$.

Figure 8: SW profile measured on WR975 waveguide.

SUMMARY

The combination of iris plate and 3-stub tuner can be used as a variable coupler. It increases the equivalent external Q of an over-coupled superconducting cavity by two orders of higher. More measurement needs to be done to verify this analysis when the CMTF is available for this study.

I would like to thank R. Sundelin, L. Phillips, C. Reece, and J. Delayen, I. Campisi and Y. Kang of ORNL for the fruitful discussions during the course of this work.

REFERENCE

- [1] I. Ben-Zvi, SUNYLAC Internal Report, April 1980.
- [2] Waveguide Handbook, edited by N. Marcuvitz, MIT Radiation Lab, 1986 edition, p238~240, p327, p408~409.
- [3] Principle of Microwave Circuits, edited by C. Montgomery, R. Dicke, E. Purcell, MIT Radiation Lab, series 1948, p231~234.
- [4] Field Theory of Guided Waves, second edition, R. Collin, p523~531.
- [5] Private communication with J. DeFords of STAR, Inc.
- [6] P. Balleyguier, LINAC98 proceedings, MO4037.
- [7] Private communication with Y. Kang of ORNL.