

Dark decay of the top quark

Kyoungchul Kong,¹ Hye-Sung Lee,^{2,3} and Myeonghun Park⁴

¹*Department of Physics and Astronomy, University of Kansas, Lawrence, Kansas 66045, USA*

²*Department of Physics, College of William and Mary, Williamsburg, Virginia 23187, USA*

³*Theory Center, Jefferson Lab, Newport News, Virginia 23606, USA*

⁴*Kavli IPMU (WPI), The University of Tokyo, Kashiwa, 277-8583, Japan*

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We suggest top quark decays as a venue to search for light dark force carriers. The top quark is the heaviest particle in the standard model whose decays are relatively poorly measured, allowing sufficient room for exotic decay modes from new physics. A very light (GeV scale) dark gauge boson (Z') is a recently highlighted hypothetical particle that can address some astrophysical anomalies as well as the 3.6σ deviation in the muon $g-2$ measurement. We present and study a possible scenario that top quark decays as $t \rightarrow bW + Z'$ s. This is the same as the dominant top quark decay ($t \rightarrow bW$) accompanied by one or multiple dark force carriers. The Z' can be easily boosted, and it can decay into highly collimated leptons (lepton-jet) with large branching ratio. We discuss the implications for the Large Hadron Collider experiments including the analysis based on the lepton-jets.

I. INTRODUCTION

With a recent discovery of a new scalar particle [1, 2], which is consistent with the standard model (SM) Higgs boson, the understanding of the SM is near completion except for precision studies. With this, the interest toward new physics beyond the SM soars. One definite evidence of new physics is the existence of dark sectors such as dark energy and dark matter [3].

Dark force was introduced as a newcomer to dark sector [4]. It is a hypothetical interaction among the dark matters that can address various astrophysical anomalies such as positron excess. Positron excess has been observed at numerous experiments including PAMELA [5] and AMS [6]. A very light (roughly, GeV scale) dark force carrier (which we call Z') is supposed to couple to dark matter strongly, but extremely weakly to the SM particles. It is expected to be light because such a light force carrier can provide the the required enhancement (via the so-called Sommerfeld effect) of the present time dark matter annihilation at the Galactic center while satisfying the dark matter relic density constraints [4]. Through a simple kinematics, it can also naturally explain why antiproton excess has not been observed. In addition, such a gauge boson with small mass and very weak coupling can address the 3.6σ deviation in the muon anomalous magnetic moment [3] through a one-loop correction of Z' [7, 8]. (For more motivations and details about the light dark force carriers, see Ref. [9].)

With such appealing motivations, there are active searches for light dark force carriers. A dark force carrier is roughly of GeV scale, and can be searched for both at the low energy and high energy experiments. The major search schemes are based on bremsstrahlung at fixed target experiments or meson decays [10]. Collider signatures for certain supersymmetric models [11] and the decay of the Higgs bosons into the Z' [12–14] have been studied as well.

In this paper, we present a novel channel to produce and search for the dark force carrier using top quark de-

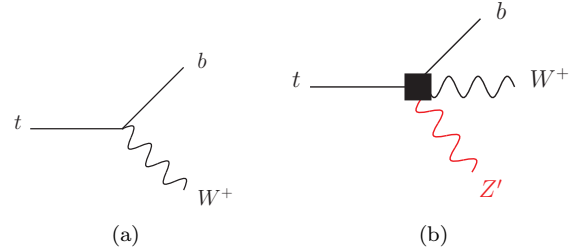


FIG. 1: (a) Dominant top quark decay mode ($t \rightarrow bW$). (b) The top quark decay into dark force carriers ($t \rightarrow bW + Z'$ s) is the same to the dominant top quark plus one or multiple Z' s. A very light Z' can be easily boosted and, it can decay into highly collimated jets or leptons (lepton-jet).

cays. We show that the top quark decays into dark force carriers are possible and it can be searched for at the Large Hadron Collider (LHC) with excellent discovery potential.

II. TOP TO Z' PRODUCTION

The top quark is the heaviest elementary particle in the SM, quite possibly heavier than new particles in many models beyond the SM. (For a short review about the top quark, see a review article in Ref. [3].) Because of its large mass, its lifetime ($\tau_t \approx 0.5 \times 10^{-24}$ sec) is very short. Since it is shorter than the QCD scale ($\Lambda_{\text{QCD}} \sim 10^{-23}$ sec), top quark decays before forming any hadrons, unlike other quarks [15]. For this reason, top quark decays have been considered as an ideal probe of new physics even before its discovery at Tevatron in 1995 [16, 17].

Although top quark mass is precisely measured ($m_t = 173.1$ GeV with 0.5% level uncertainty), its decay width is not [3]:

$$\Gamma_t = 2.0 \pm 0.5 \text{ GeV}. \quad (1)$$

While it is in a reasonable agreement with the SM prediction ($\Gamma_t^{\text{SM}} \simeq 1.3$ GeV with theoretical error better than 1% [3]), quite a large uncertainty (25%) indicates a lack of precise knowledge about top quark properties. While the exact values are process dependent, typical experimental errors related to top quark decays are of $\mathcal{O}(10\%)$ [3], leaving plenty room for new decay modes originating from new physics beyond the SM. (Later, in our illustration, we will take the top quark decay branching ratio into light Z' 's not more than 0.1%–1% although it could be much greater in principle.) With these observations, we view the top quark decay as an ideal window to look for a dark force carrier.

In the SM, nearly 100% of top quark decay is the on-shell $t \rightarrow bW$ decay. Possible scenarios to search for Z' in connection to the top quark decay include

- (i) $t \rightarrow bH^+ \rightarrow bW + Z'$
(through $H^\pm W^\mp Z'$ coupling),
- (ii) $t \rightarrow bH^+ \rightarrow bW + h \rightarrow bW + Z'Z'$
(with a light non-SM Higgs boson h),
- (iii) $t \rightarrow bW^* \rightarrow bW + Z'$
(through $Z'WW$ coupling),
- (iv) $t \rightarrow bW^* \rightarrow bW + h \rightarrow bW + Z'Z'$
(through hWW coupling).

There can be also Z' radiation off from top not being a decay product. For a relatively heavy Z' , $m_{Z'} \gtrsim 1$ GeV, the radiation cross sections are negligibly small though. While the off-shell processes are worth investigating as they may prevail in different situations (for example, when a charged Higgs is absent), we will focus on the on-shell decays in this paper.

There may be also other ways the t can decay into Z' 's without producing bW such as $t \rightarrow qZ'$ (with $q = u, c$) through the W loop. Nevertheless, it is interesting to observe that there are abundant ways the t can decay into Z' 's with bW , the decay products of the dominant top quark decay. (See Fig. 1.)

Throughout this paper, we will assume $m_W \lesssim m_{H^\pm} \lesssim m_t$, and study the on-shell decays (i) and (ii). Whether (i) or (ii) dominates depends on the masses of the Higgs bosons, especially whether the non-SM Higgs h is light enough so that the charged Higgs can decay into it dominantly or not.

III. INGREDIENTS OF DARK FORCE MODELS

A. Dark force carrier

While the final particles in the aforementioned modes are the same up to the number of Z' 's, some of the modes are model dependent, and it is worth describing some aspects of the models.

The minimum ingredients of extra particles to extend the SM to the dark sector are, besides the dark matter itself, the Z' (dark force carrier) and an additional Higgs to give a mass to the Z' . As the Z' should be massive in order to decay into the leptons so that it can explain the

astrophysical anomalies, we need some extended Higgs sector to give a mass to the Z' . (We do not consider other possible ways to provide a mass such as the Stueckelberg mechanism [18].)

Z' is typically taken as a gauge boson of a new gauge symmetry, dark $U(1)$, under which the SM particles do not have charges. Although Z' does not couple to the SM particles directly, it can couple through the mixing of the Z' with the SM gauge bosons via the gauge kinetic mixing parametrized by ε [19]

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} + \frac{1}{2}\frac{\varepsilon}{\cos\theta_W}B_{\mu\nu}Z'^{\mu\nu} - \frac{1}{4}Z'_{\mu\nu}Z'^{\mu\nu}. \quad (2)$$

The exact coupling, however, depends on the details of model, especially on how the Z' gets a mass. For example, it depends on whether the extra Higgs is a $SU(2)_L$ singlet or doublet [12].

Depending on the Higgs sector, the Z' may couple both to the electromagnetic current (J_{em}) and the weak neutral current (J_{NC}). The interaction Lagrangian of the Z' with the SM fermions is given by

$$\mathcal{L}_{\text{dark } Z} = -(\varepsilon e J_{em}^\mu + \varepsilon_Z g_Z J_{NC}^\mu) Z'_\mu \quad (3)$$

$$= \bar{f}(g_V \gamma^\mu - g_A \gamma^\mu \gamma^5) f Z'_\mu \quad (4)$$

with

$$g_V = -\varepsilon e Q_f - \varepsilon_Z g_Z \left(\frac{1}{2} T_{3f} - Q_f \sin^2 \theta_W \right), \quad (5)$$

$$g_A = -\varepsilon_Z g_Z \left(\frac{1}{2} T_{3f} \right), \quad (6)$$

where Q_f and T_{3f} are the electric charge and isospin, respectively. Bounds on the couplings of the Z' come from various experiments such as the lepton anomalous magnetic moment, atomic parity violation, polarized electron scattering, meson decays, fixed target experiments, beam dump experiments, and Higgs decays. The exact bounds depend on the $m_{Z'}$ and its decay branching ratio, but typically, it is set as $|\varepsilon| \lesssim 10^{-2}$ and $|\delta| \lesssim 10^{-2}$ (with $\varepsilon_Z \equiv \delta \frac{m_{Z'}}{m_Z}$) [12, 20].

For our interested Z' of roughly $\mathcal{O}(\text{GeV})$, the $\text{BR}(Z' \rightarrow \ell^+ \ell^-)$ for $\ell = e, \mu$ is expected to be large, typically $0.2 \sim 1$ depending on $m_{Z'}$ and other details. Such a light Z' gauge boson shows many distinguishable properties from heavy (electroweak or TeV scale) Z' gauge bosons in various contexts [21]. (Also see Refs. [22, 23] for some recent studies on invisible or partly invisible heavy Z' gauge bosons.)

Because the Z' can be easily boosted in the top decay processes we consider, it is expected to appear as highly collimated leptons or jets. Depending on its mass and coupling, it could be more identifiable as a lepton-jet or a simple pair of isolated leptons. (See the Appendix for some detailed discussions.) A lepton-jet is a final state consisting of collimated electrons or muons. Measuring properties of lepton-jets have been studied and experimental searches at the LHC experiments already started [24, 25].

B. New Higgs bosons

The dark force can be categorized into how the Z' gets a mass. We will consider the dark Z model based on the type-I two Higgs doublet model (2HDM) [12], with notations taken from Ref. [14], for scenarios (i) and (ii). In this kind of dark force model, $\tan\beta \equiv v_2/v_1 \gtrsim 1$ is required, where Φ_2 couples to the SM fermions and Φ_1 does not. (For a heavy Z' model in 2HDM frames, for example, see Ref. [26].)

A new neutral Higgs boson that can mix with the SM Higgs doublet is generically expected, and if an extra Higgs is a doublet, there are charged Higgs bosons too. The Higgs properties of such scenarios have been studied in many literatures [12, 14, 27]. A new neutral Higgs can be very light and it can dominantly decay as $h \rightarrow Z'Z'$. A charged Higgs can be also much lighter than typical experimental bounds as its dominant decay may be into rather elusive light Z' s [14].

For the $m_{H^\pm} \lesssim m_t$, the major decay modes of $H^\pm$ in the typical 2HDM are into $\nu\tau^+$ and $c\bar{s}$. Their decay widths are

$$\Gamma(H^+ \rightarrow \nu\tau^+) \simeq \frac{m_{H^\pm}}{8\pi v^2} \frac{m_\tau^2}{\tan^2\beta}, \quad (7)$$

and similarly for $c\bar{s}$ with a color factor. Despite the color factor, because of the small mass of charm quark (c) at the electroweak scale, the $c\bar{s}$ mode is subdominant to the $\tau\nu$ mode. With a recently discovered 125 GeV SM-like Higgs (H_{SM}), the off-shell decay $H^\pm \rightarrow W^*H_{\text{SM}} \rightarrow f\bar{f}'H_{\text{SM}}$ can be also quite sizable, even larger than $H^\pm \rightarrow \nu\tau^\pm$ for certain parameter space.

The scenario (i) is based on the assumption that the SM-like Higgs is the lighter Higgs doublet. The $H^\pm W^\mp Z'$ coupling is very small, but its decay branching ratio could be sizable [28, 29]. The tree-level decay width is given by

$$\Gamma(H^\pm \rightarrow WZ') \simeq \frac{m_{H^\pm}^3}{16\pi v^2} (\sin\beta \cos\beta_d)^2 \left(1 - \frac{m_W^2}{m_{H^\pm}^2}\right)^3 \quad (8)$$

where β_d is a parameter related to the dark sector Higgs singlet, introduced in Ref. [12].

Scenario (ii) is based on the assumption that there is a light Higgs h that a charged Higgs can decay into. For definiteness, let us take the Higgs mixing angle $\alpha \simeq \pm\pi/2$ limit, which is a decoupling limits of doublets where a heavier Higgs doublet is the SM-like Higgs (125 GeV) and a lighter one is the other doublet. The decay width [14] is

$$\Gamma(H^\pm \rightarrow Wh) \simeq \frac{\sin^2\beta}{16\pi v^2} \frac{1}{m_{H^\pm}^3} \lambda^{3/2}(m_{H^\pm}^2, m_W^2, m_h^2) \quad (9)$$

with $\lambda(x, y, z) \equiv x^2 + y^2 + z^2 - 2xy - 2yz - 2zx$. In this limit, we also get $\text{BR}(h \rightarrow Z'Z') \simeq 1$ as h does not couple to the SM fermions.

In both scenarios (i) and (ii), for most of the parameter space, a dominant decay of the charged Higgs is into Z' s. The dominance of the $H^\pm$ decay into the Z' particles in both scenarios originates from the enhancement of couplings for boosted gauge bosons, formally known as Goldstone boson equivalence theorem. Detailed discussions and illustrations are given in the aforementioned references [14, 28, 29]. We will use a parameter for the charged Higgs to Z' s decay branching ratio

$$Y \equiv \text{BR}(H^\pm \rightarrow W + Z'\text{s}), \quad (10)$$

which corresponds to $Y = \text{BR}(H^\pm \rightarrow WZ')$ with one Z' [for scenario (i)], and $Y = \text{BR}(H^\pm \rightarrow Wh) \text{BR}(h \rightarrow Z'Z')$ with two Z' s [for scenario (ii)]. In a large area of the parameter space, $Y \simeq 1$ is obtained. In our analysis, instead of using an exact value which depends on various model parameters, we will take a range of $Y = 0.5 - 1$ (the branching ratio of 50% or greater).

IV. PRODUCTION AND DECAYS OF TOP QUARK AT THE LHC

A. Top pair production

Top quarks can be produced in pair by dominant QCD process ($q\bar{q}'$, gg) or singly by electroweak process with a W boson at the Tevatron and the LHC. At the LHC, the $t\bar{t}$ can be produced abundantly via dominant gluon-gluon fusion. The gluon fusion makes up 90% of the total $t\bar{t}$ for the center-of-mass energy $\sqrt{s} = 14$ TeV (about 80% for $\sqrt{s} = 7$ TeV).

The total $t\bar{t}$ pair production cross section at the LHC (at next-to-next-to-leading order QCD corrections) is predicted to be $\sigma_{t\bar{t}} \simeq 167$ pb (for 7 TeV), 239 pb (for 8 TeV), and 933 pb (for 14 TeV) [30]. Currently, at the LHC, integrated luminosity (L) is about 5 fb^{-1} for 7 TeV, and about 20 fb^{-1} for 8 TeV [31]. The 14 TeV LHC is scheduled to operate soon, and is expected to reach the luminosity of several hundreds of fb^{-1} .

B. Top decay into dark gauge bosons through $H^\pm$

A top quark can decay into a charged Higgs through $t \rightarrow bH^+$ for a relatively light $H^\pm$. While there are searches for light charged Higgs in $t \rightarrow bH^+ \rightarrow b\nu\tau^+$ and $t \rightarrow bH^+ \rightarrow bc\bar{s}$ based on typical 2HDMs, the results are negative [32]. These searches, however, would have missed the light charged Higgs of $t \rightarrow bH^+ \rightarrow bW + Z'$ s that would dominate in our scenario. As described earlier, the $H^\pm$ can decay into the Z' s dominantly in the presence of the dark force.

Neglecting m_b/m_t and higher order corrections, the

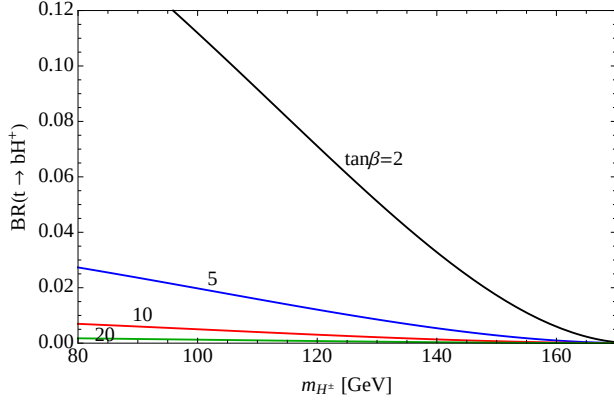


FIG. 2: $\text{BR}(t \rightarrow bH^+)$ for $\tan\beta = 2$ (black), 5 (blue), 10 (red), 20 (green). The t decay into $H^\pm$ is larger for smaller $m_{H^\pm}$ and smaller $\tan\beta$.

relevant top decay widths are

$$\Gamma_{t \rightarrow bW} = \frac{\sqrt{2}G_F|V_{tb}|^2}{16\pi} m_t^3 \left(1 - \frac{m_W^2}{m_t^2}\right)^2 \left(1 + \frac{2m_W^2}{m_t^2}\right), \quad (11)$$

$$\Gamma_{t \rightarrow bH^\pm} = \frac{\sqrt{2}G_F|V_{tb}|^2}{16\pi} m_t^3 \left(1 - \frac{m_{H^\pm}^2}{m_t^2}\right)^2 \frac{1}{\tan^2\beta} \quad (12)$$

with $\tan\beta \gtrsim 1$ in the dark force model we consider. (The $t \rightarrow bW$ decay itself shows the enhancement from the Goldstone boson equivalence theorem with a boosted W boson [33].) As both decays have the same dependence on the Cabibbo-Kobayashi-Maskawa (CKM) matrix element $|V_{tb}|^2$, even quite sizable $\Gamma(t \rightarrow bH^+)$ may not alter an effective value of V_{tb} significantly when it is measured from the top quark decays.

In our study, we still take $t \rightarrow bW$ as the dominant top decay and consider $t \rightarrow bH^+$ as the important subdominant one. Then the branching ratio of the on-shell $t \rightarrow bH^+$ decay, which is dependent on unknown $m_{H^\pm}$ and $\tan\beta$, is

$$\text{BR}(t \rightarrow bH^+) \simeq \frac{\Gamma_{t \rightarrow bH^+}}{\Gamma_{t \rightarrow bW} + \Gamma_{t \rightarrow bH^+}} \quad (13)$$

$$\simeq \left(\frac{m_t^2 - m_{H^\pm}^2}{m_t^2 - m_W^2}\right)^2 \frac{1/\tan^2\beta}{1 + 2m_W^2/m_t^2}, \quad (14)$$

which is plotted in Fig. 2. We can see that a few % level of the top decay can be easily accommodated for $m_{H^\pm} < m_t$. For $m_{H^\pm} = 140$ GeV, for instance, we have $\text{BR}(t \rightarrow bH^+) \simeq 0.03 - 0.0003$, with the $\tan\beta = 2 - 20$ range (higher BR corresponds to lower $\tan\beta$).

V. SETUP FOR NUMERICAL ANALYSIS

We will consider the $t\bar{t}$ production followed by one of the top quark pair decaying into Z' 's. We will also consider only the $Z' \rightarrow \ell^+\ell^-$ channel. The cross section at

the LHC to produce Z' is given by

$$\sigma(pp \rightarrow bW\bar{b}W + Z'\text{'s}) \simeq \sigma_{t\bar{t}} 2X \quad (15)$$

using $\text{BR}(t \rightarrow bW) \simeq 1$ and a new parameter X for the top to Z' decay branching ratio

$$X \equiv \text{BR}(t \rightarrow bW + Z'\text{'s}), \quad (16)$$

whose detail depends on the specific scenario.

In scenarios (i) and (ii), using the on-shell $H^\pm$ decays, we have

$$X = \text{BR}(t \rightarrow bH^+) Y \quad (17)$$

with $\text{BR}(t \rightarrow bH^+)$ given in Fig. 2. In the numerical analysis of this paper, we consider only the scenario (i). [The application for the scenario (ii) would be straightforward.] This process is

$$\bullet \text{ top pair: } pp \rightarrow t\bar{t} \rightarrow bW\bar{b}H^\pm \rightarrow bW\bar{b}W + Z', \quad (18)$$

which is similar to the dominant $t\bar{t}$ process except that Z' is accompanied in the decay products. We consider only $m_W \lesssim m_{H^\pm} \lesssim m_t$ to avoid additional constraints from $W \rightarrow bH^\pm$ decays, etc.

Figure 3 shows the production cross sections of the Z' with $m_{H^\pm}$ in the $t\bar{t}$ channel ($pp \rightarrow t\bar{t} \rightarrow bW\bar{b}W + Z'$) at the (a) 8 TeV LHC and (b) 14 TeV LHC, using the high order calculation of $\sigma(pp \rightarrow t\bar{t})$. The band indicates $Y = \text{BR}(H^\pm \rightarrow WZ') = 0.5 - 1$ range.

We will take a rather conservative value of $X = 0.001$ and assume $\text{BR}(Z' \rightarrow \ell^+\ell^-) = 0.2$, for our illustration, meaning 0.02% of top quark decay is into the lepton pairs. [Only the product $X \text{BR}(Z' \rightarrow \ell^+\ell^-)$ has the real meaning for the final lepton pair production rate.]

The value $X = 0.001$ can be obtained, for example, for $m_{H^\pm} = 100$ GeV (with $\tan\beta \simeq 20$, $Y \simeq 0.8$), $m_{H^\pm} = 140$ GeV (with $\tan\beta \simeq 10$, $Y \simeq 0.9$), and $m_{H^\pm} = 160$ GeV (with $\tan\beta \simeq 5$, $Y \simeq 1$).

We use a rather intuitive parameter X for our presentation instead of model-specific parameters. The exact value of Y , for example, can be more constrained for a specific $m_{H^\pm}$, $\tan\beta$, $m_{Z'}$. There are many unknown parameters such as $\text{BR}(Z' \rightarrow \ell^+\ell^-)$ and other dark sector related parameters anyway, and our treatment using X (with a rather conservative values) allows us more controllable analysis.

VI. COMPARISON TO THE CHARGED HIGGS PAIR PRODUCTION

The charged Higgs boson can be typically produced in the Drell-Yan process. Charged Higgs pair production through Drell-Yan (γ^* , Z^*) is model independent except for the mass.

The Drell-Yan production of $H^\pm$ pair, for scenario (i), is

$$\bullet \text{ Drell-Yan: } pp \rightarrow H^+H^- \rightarrow WW + Z'Z'. \quad (19)$$

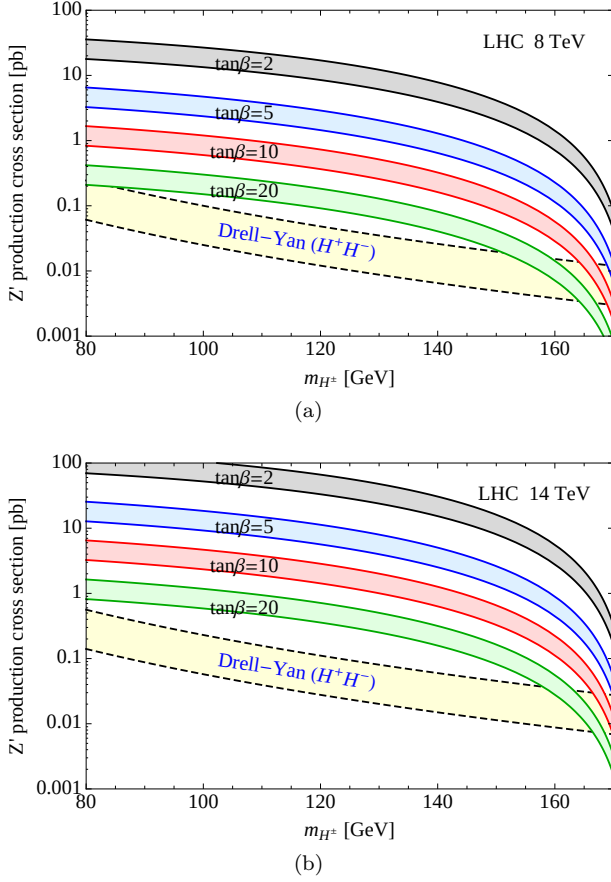


FIG. 3: Production cross sections of the Z' with $m_{H^\pm}$ in the $t\bar{t}$ channel ($pp \rightarrow t\bar{t} \rightarrow bW\bar{b}W + Z'$) at the (a) 8 TeV LHC and (b) 14 TeV LHC. Cross section at the 14 TeV is about 4 times larger than that at the 8 TeV. In the $m_W \lesssim m_{H^\pm} \lesssim m_t$ range, the results for $\tan\beta = 2$ (black), 5 (blue), 10 (red), 20 (green) are shown. Drell-Yan channel ($pp \rightarrow H^+H^- \rightarrow WW + Z'Z'$) (Dashed) is also shown for comparison. The band indicates $\text{BR}(H^\pm \rightarrow WZ') = 0.5 - 1$ range.

In Fig. 3, we can see the difference of the production cross sections of the Z' through the $t\bar{t}$ channel and Drell-Yan channel. In both cases, the cross section decreases with $m_{H^\pm}$ because of the phase space. We use the on-shell decays only using branching ratio of Fig. 2.

The Drell-Yan and the $t\bar{t}$ processes have a few differences. First, the $t\bar{t}$ production cross section is much larger than the Drell-Yan case, except for the very large $\tan\beta$ ($\tan\beta \gtrsim 20$) or large $m_{H^\pm}$. Second, $t\bar{t}$ produces only one charged Higgs while the Drell-Yan produces a pair of charged Higgs. Third, tagging is different (bW pair for $t\bar{t}$, W pair for Drell-Yan). With different tagging and a small production cross section, we neglect the Drell-Yan process in our study.

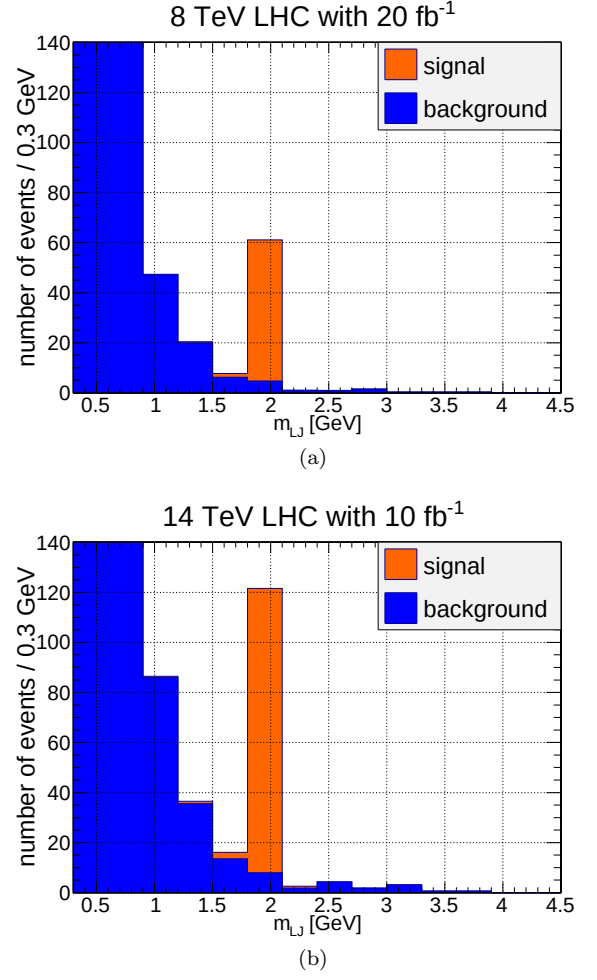


FIG. 4: Distributions of lepton-jet mass (m_{LJ}) in the $t\bar{t} + LJ$ mode at the LHC for (a) 8 TeV LHC with $L = 20 \text{ fb}^{-1}$ and (b) 14 TeV LHC with $L = 10 \text{ fb}^{-1}$. $m_{H^\pm} = 140 \text{ GeV}$, $m_{Z'} = 2 \text{ GeV}$ with $X = 0.001$ and $\text{BR}(Z' \rightarrow \ell^+\ell^-) = 0.2$ are used.

VII. DISCOVERY POTENTIAL AT THE LHC

We discuss the discovery potential of the Z' from the $t\bar{t}$ process at the LHC. For definiteness, we assume $\text{BR}(Z' \rightarrow \ell^+\ell^-) = 0.2$. For the background events, we take only the irreducible processes $t\bar{t} + \ell^+\ell^-$ from the off-shell photon and Z boson, although there may be more sources of backgrounds such as $t\bar{t} + \text{jets}$ with the jets faking leptons. In this section, we require two b -tagged jets to limit backgrounds to $t\bar{t}$ events. The Appendix describes more details of our Monte Carlo study including the tagging efficiencies. The efficiency depends on $m_{H^\pm}$ and $m_{Z'}$, as well as the LHC energy. We assume a K -factor for the background events $K_{\text{bkg}} \simeq 2$ and apply it to our background events generated by tree-level Monte

$m_{Z'}$ [GeV]	$m_{H^\pm}$			BKG
	100 GeV	140 GeV	160 GeV	
1	40.0	86.2	58.1	69.6
2	8.2	59.9	47.8	5.0
5	0.1	5.0	9.1	0.3

TABLE I: Expected number of events in each lepton-jet bin (20% window of the Z' mass) with two b -tagging in 8 TeV LHC 20 fb^{-1} . We set $X = 0.001$ and $\text{BR}(Z' \rightarrow \ell^+ \ell^-) = 0.2$. Signal events were obtained with high order $\sigma_{t\bar{t}}$ with the branching ratio, and the background events were obtained with tree-level simulation with $K_{\text{bkg}} = 2$.

Carlo simulation.¹

First, we consider the $\sqrt{s} = 8 \text{ TeV}$ case ($\sigma_{t\bar{t}} \sim 239 \text{ pb}$), with integrated luminosity of about $L = 20 \text{ fb}^{-1}$. Table I shows the number of signal events and background events for various choices of $m_{H^\pm}$ and $m_{Z'}$, with $X = 0.001$ and $\text{BR}(Z' \rightarrow \ell^+ \ell^-) = 0.2$. The numbers are for each lepton-jet bin (20% window of a given $m_{Z'}$) with two b -tagging. (See the Appendix for details including the tagging efficiencies for signal and background events.)

For a specific example, we consider $m_{H^\pm} = 140 \text{ GeV}$ and $m_{Z'} = 2 \text{ GeV}$. We expect the number of signal events (after the tagging efficiency), for $L = 20 \text{ fb}^{-1}$,

$$N_{\text{sig}} = \sigma_{t\bar{t}} 2X \text{BR}(Z' \rightarrow \ell^+ \ell^-) \epsilon_{\text{sig}} L \approx 60, \quad (20)$$

and the SM background events

$$N_{\text{bkg}} = \sigma_{\text{bkg}} \epsilon_{\text{bkg}} L \approx 5, \quad (21)$$

which would give a very large number of signal events compared to the backgrounds (resulting the likelihood ratio $S_{\text{cL}} \simeq 14.6$). The likelihood ratio, which is defined as

$$S_{\text{cL}} = \sqrt{2N_{\text{obs}} \log(1 + N_{\text{sig}}/N_{\text{bkg}}) - 2N_{\text{sig}}} \quad (22)$$

with $N_{\text{obs}} = N_{\text{sig}} + N_{\text{bkg}}$, is a good method even when there are relatively small background events.

Even this kind of large signal can be still missed in conventional analysis. For example, in the CMS $t\bar{t}$ dilepton analysis (see the Appendix) with 5.3 fb^{-1} luminosity at 8 TeV LHC [34], signals can be lost by invariant mass requirements for the lepton pair ($m_{\ell\ell} > 20 \text{ GeV}$). The contribution of signals to dileptons in the $t\bar{t}$ channels are very small with CMS analysis cuts (one b -tagged jet). For the above sample point, we estimate the expected number of signal, $N_{\text{sig}} \simeq 4$ ($\epsilon_{\text{sig}} \simeq 0.71\%$) can be buried under the uncertainties of $t\bar{t}$ dilepton events (Expected uncertainty in $t\bar{t}$ dilepton samples, $\Delta N_{\text{bkg}} \simeq 591$ with observed data $N_{\text{bkg}} \simeq 1.7 \times 10^4$), resulting in only $S_{\text{cL}} \simeq 0.03$.

$m_{Z'}$ [GeV]	$m_{H^\pm}$		
	100 GeV	140 GeV	160 GeV
1	7.8 fb^{-1}	1.9 fb^{-1}	3.4 fb^{-1}
2	14.5 fb^{-1}	0.7 fb^{-1}	1.0 fb^{-1}
5	-	7.3 fb^{-1}	3.5 fb^{-1}

TABLE II: Required luminosity for 14 TeV LHC to see the likelihood ratio $S_{\text{cL}} = 5$ (corresponding to 5σ discovery). Basically the same method as Table I is used.

Thus, re-analysis of existing 8 TeV data with $t\bar{t} + \text{lepton-jet}$ can potentially bring a discovery of the light Z' .

For the $\sqrt{s} = 14 \text{ TeV}$ case ($\sigma_{t\bar{t}} \sim 933 \text{ pb}$), we show the required luminosity for $S_{\text{cL}} = 5$ (corresponding to 5σ discovery) in Table II. Basically the same method as the 8 TeV case (Table I) is used. It shows the dark force search at the very early stage of the 14 TeV LHC will be a very interesting program. Both Table I and Table II, for given X and $\text{BR}(Z' \rightarrow \ell^+ \ell^-)$, can be obtained from Table III in the Appendix up to the precision.

Figure 4 shows the signals and backgrounds for the above sample point ($m_{H^\pm} = 140 \text{ GeV}$, $m_{Z'} = 2 \text{ GeV}$, $X = 0.001$) with $\text{BR}(Z' \rightarrow \ell^+ \ell^-) = 0.2$. For cuts, we require the CMS-like analysis cuts [Sec. A 2] with two b -tagged jets and construct lepton-jets with $m_{\text{LJ}} > 0.2 \text{ GeV}$. For backgrounds, the leading order cross section is 3.73 pb at 8 TeV and 15.33 pb at 14 TeV LHC with parton level cuts for the rapidity of quark and leptons as $|\eta_q| < 5$, $|\eta_\ell| < 3$ and a dilepton invariant mass cut for the same flavor, an opposite-sign lepton pair greater than 0.2 GeV . Corresponding efficiencies are about 1.4% for both collision energies. We take $K_{\text{bkg}} = 2$ for the K -factor of the background. We can see that the signal shows up as a clear spike over the SM background.

The $t \rightarrow bW + Z'$ decay (via $H^\pm$) can be compared to the dominant top decay mode $t \rightarrow bW$. The top decay into the charged Higgs might look similar to the dominant top decay accompanied by a Z' that can decay into a pair of collimated leptons or others that are hard to identify. It has important implication as the current experimental measurements might have counted the $t \rightarrow bW + Z'$ as $t \rightarrow bW$ depending on the analysis methods. Z' may also have sizable decay branching ratio into neutrinos or invisible particles. As mentioned earlier, since both decays have the same dependence on the CKM matrix element $|V_{tb}|^2$, [Eqs. (11) and (12)], even quite sizable $\Gamma(t \rightarrow bH^+)$ may not alter the effective value of V_{tb} significantly when it is measured from the top quark decays.

VIII. SUMMARY

We discussed the production of light Z' gauge boson through a top quark at the LHC. A light Z' of roughly $\mathcal{O}(1) \text{ GeV}$ with small coupling is a very well motivated

¹ The assumed $K_{\text{bkg}} \simeq 2$ can be compared to K factors for signals $K_{\text{sig}} = 1.74$ (1.84) for 8 TeV (14 TeV) LHC, obtained from the estimation with our leading order Monte Carlo simulation and Ref. [30].

new physics candidate as it can address some astrophysical anomalies as well as the muon $g - 2$ anomaly. While its search is very active at the low energy experimental facilities, its search at the LHC is relatively limited so far.

The LHC can produce the top quark pair abundantly through the gluon fusion. We considered the scenario the top quark decays through a charged Higgs $t \rightarrow bH^+$, where the charged Higgs can decay into one Z' or multiple Z' s dominantly. The top decay into the dark gauge boson is very close to its dominant decay mode accompanied by one or two illusive Z' s ($t \rightarrow bW + Z'$ s). Even a small $\text{BR}(t \rightarrow bH^+)$ can be enough to produce the Z' at the observable level at the LHC experiments. The Z' production through a top can be larger than the typical Drell-Yan mechanism to produce a pair of charged Higgs and produce one Z' when the Drell-Yan produces a pair of Z' .

We considered the process $pp \rightarrow t\bar{t} \rightarrow bW\bar{b}W + Z'$ with Z' decaying into a lepton pair. Because of lightness of the Z' , the lepton pairs are highly collimated forming lepton-jets. For some parameter space, even the existing 8 TeV LHC data may give enough signals for a discovery. It also guarantees a huge discovery potential even at the very early stage of the 14 TeV LHC experiments.

As the top quark decaying into the dark sector mode can be easily mistaken with its dominant bW mode, a reanalysis of the top data at the hadron collider can possibly reveal an interesting hint of the Z' even if the Z' is very elusive or decays invisibly. It calls for attention in both the experimental and theoretical sides of the top quark study.

Note: Around the time this work was submitted, Ref. [29] preprint (version 2), which overlaps with some aspect of this paper, appeared.

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Appendix A: Some details on numerical analysis

1. Lepton pair from Z' decay

Light Z' cannot be reconstructed with the usual lepton tagging because of the following simple kinematical reason. The invariant mass of a lepton pair can be expressed

as

$$m_{\ell^+\ell^-}^2 = 2P_{T_1}P_{T_2}(\cosh\Delta\eta - 1) \quad (\text{A1})$$

$$\simeq 2P_{T_1}P_{T_2}(\cosh\Delta R - 1), \quad (\text{A2})$$

with observation $\Delta R \simeq \Delta\eta$ since $\Delta\phi$ distribution is peaked at 0. For a moderate lepton tagging efficiency, most analyses require $P_{T(\ell)}^{\min}$ as a P_T cut of leptons

$$P_{T(e)}^{\min} = 10 \text{ GeV}, \quad P_{T(\mu)}^{\min} = 5 \text{ GeV}. \quad (\text{A3})$$

Now with an isolation requirement of $\Delta R > 0.3$, the corresponding minimum invariant mass of an electron pair and muon pair from Z' would be

$$m_{ee} > \sqrt{2P_{T(e)}^{\min}P_{T(e)}^{\min}(\cosh(0.3) - 1)} \simeq 3 \text{ GeV}, \quad (\text{A4})$$

$$m_{\mu\mu} > \sqrt{2P_{T(\mu)}^{\min}P_{T(\mu)}^{\min}(\cosh(0.3) - 1)} \simeq 1.5 \text{ GeV}. \quad (\text{A5})$$

Therefore conventional analyses would miss Z' lighter than 3 (1.5) GeV in the dielectron (dimuon) channel. We adopt an analysis method with lepton-jet proposed in Ref. [11]. A variation of the LJ definition can be found in Ref. [24]. Since $t\bar{t} + \ell^+\ell^-$ is a major background in our study, we follow the LJ definition in Ref. [35] with a modification to the muon P_T requirement.

1. At least two same flavor leptons with $P_T > 10$ GeV (electron), 5 GeV (muon) and in a cone of $\Delta R < 0.1$.
2. Isolation: Hadronic and leptonic isolation of $\sum P_T < 3$ GeV in $0.1 < \Delta R < 0.4$.

In addition, to reduce the background events, we require 20% window of the expected Z' mass for an invariant mass of lepton-jet.

3. Invariant mass cut on the lepton-jet: $|m_{\text{LJ}} - m_{Z'}| < 0.2 \times m_{Z'}$.

For a Monte Carlo simulation, we add Z' and $H^\pm$ to the SM using FeynRules v2 [36] and simulate events with Madgraph v5.14 [37], Pythia 6 [38] and Delphes 3.0.11 [39]. We modify b -jet tagging/mistagging efficiency (tagging efficiency is around 60% – 75% depending on P_T and η) according to CMS CSVM tagging [40, 41]. We make a change in the Delphes module for a smearing muon P_T to reflect the nonzero muon mass in the muon's four vector. For the lepton-jet analysis, we add the lepton-jet class to the Delphes detector simulation.

2. Signal boxes

To consider all $t\bar{t}$ decay modes, we consider three signal boxes with a slight modification of CMS analyses according to the number of triggered leptons. Jets are reconstructed with an anti- k_T algorithm with $\Delta R < 0.5$. We require one b -tagged jet (or two b -tagged jets) and the aforementioned lepton-jet mass window. Other event selection criteria will depend on signal boxes as following.

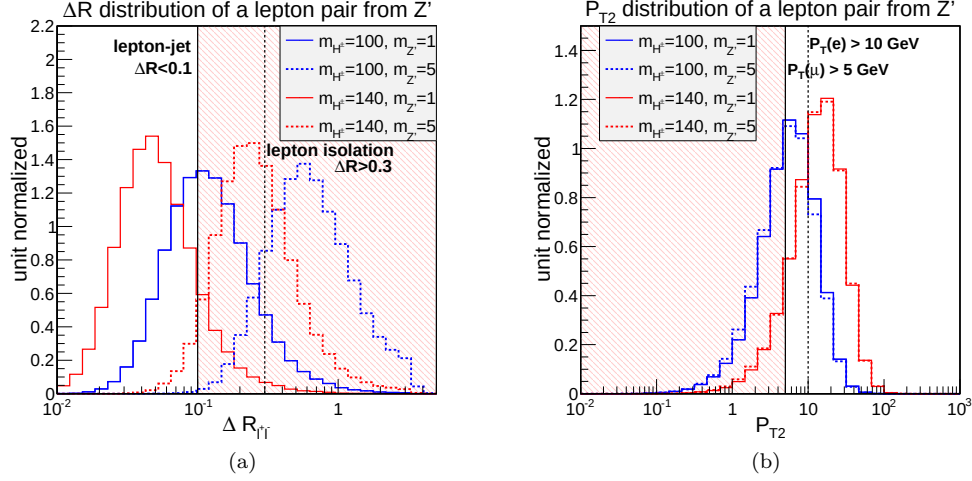


FIG. 5: We show (a) ΔR and (b) $P_{T2} = \min[P_{T(\ell)}, P_{T(\bar{\ell})}]$ of a lepton pair from the Z' decay at the parton level for the 14 TeV LHC, which are useful to understand lepton-jet tagging efficiency.

a. Dilepton box

For event selections, we require the following criteria [34].

1. Electrons with $P_T > 20$ GeV, $|\eta| < 2.5$, muons with $P_T > 20$ GeV, $|\eta| < 2.1$ are taken.
2. For the same flavor opposite-sign leptons, we veto events with the following invariant mass window: $m_{\ell+\ell^-} < 20$ GeV and $|m_Z - m_{\ell+\ell^-}| < 15$ GeV.
3. For the same flavor lepton pairing, we require $\cancel{E}_T > 40$ GeV.
4. We require at least two jets with $P_T > 30$ GeV, $|\eta| < 2.5$.

b. Semilepton box

If events can not be put in the dilepton box, we pass them to the semilepton box with the following triggers. We collect leptons of $P_T > 17$ GeV if the lepton is a muon and of $P_T > 25$ GeV for electrons as a lepton pool, then we require events to have exactly one lepton with the following selection criteria [42].

$$\begin{aligned} \text{muon : } & P_T > 26 \text{ GeV}, |\eta| < 2.1, \\ \text{electron : } & P_T > 30 \text{ GeV}, |\eta| < 2.5. \end{aligned} \quad (\text{A6})$$

For jets, we require at least four jets with $P_{T1}, P_{T2} > 45$ GeV and $P_{T3}, P_{T4} > 35$ GeV.

c. Hadronic top box

If events are not included in the dilepton or semilepton boxes, we pass events to a hadronic top box where we give

conditions only to jets. Since we tag a lepton-jet, we relax the P_T conditions of jets compared to the CMS analysis [43]. We require at least six jets with $P_{Tj} > 30$ GeV with $|\eta| < 2.4$. The CMS requires $P_{T1}, P_{T2}, P_{T3}, P_{T4} > 60$ GeV, $P_{T5} > 50$ GeV, $P_{T4} > 30$ GeV, and additional constraints for the distance between two b -tagged jets and a kinematic fit for the mass reconstruction of $t, \bar{t}$, and W .

d. Backgrounds

We consider only the irreducible background of $(t\bar{t} + \ell^+\ell^-)$ from the virtual photon and virtual Z boson radiations and we do not consider possible reducible backgrounds from the mistagged lepton-jet. For example, jets can be misidentified as electrons and overlapped leptons as discussed in Ref. [25].

3. Simple explanation of a lepton-jet tagging efficiency for signal events

With a good approximation, most $t\bar{t}$ pairs will be produced near the energy threshold. At the $t(\bar{t})$ rest frame, the energy distribution of a lepton from Z' will drop logarithmically (from flat distribution) [44] after

$$E_\ell^{(\text{cusp})} \equiv \frac{m_{Z'}}{2} e^{|\eta_{Z'} - \eta_{H^\pm}|}, \quad (\text{A7})$$

until

$$E_\ell^{(\text{max})} = \frac{m_{Z'}}{2} e^{(\eta_{Z'} + \eta_{H^\pm})}, \quad (\text{A8})$$

LHC [TeV]	$m_{Z'}$ [GeV]	$\epsilon_{LJ}(\epsilon_{(LJ+CMS)})$ [%] for signal			Mass range of $m_{\ell+\ell^-}$ [GeV]	σ_{bkg}^{LO} [pb]	$\epsilon_{LJ}(\epsilon_{(LJ+CMS)})$ [%] for background
		$m_{H^\pm} = 100$ GeV	$m_{H^\pm} = 140$ GeV	$m_{H^\pm} = 160$ GeV			
8	1	16.37 (4.18/2.07)	46.77 (10.96/4.51)	52.04 (9.40/3.04)	0.5 – 1.5	0.617	2.05 (0.61/0.28)
	2	3.07 (0.92/0.43)	31.01 (7.64/3.13)	40.74 (7.57/2.50)	1.0 – 3.0	0.157	0.53 (0.19/0.08)
	5	0.02 (0.00/0.00)	2.24 (0.64/0.26)	5.55 (1.25/0.48)	3.0 – 5.0	0.0175	0.32 (0.10/0.04)
14	1	16.38 (4.28/2.02)	44.28 (10.73/4.37)	50.54 (9.44/3.13)	0.5 – 1.5	2.536	2.18 (0.60/0.30)
	2	3.33 (1.11/0.49)	29.73 (7.52/3.13)	39.31 (7.64/2.51)	1.0 – 3.0	0.640	0.57 (0.23/0.11)
	5	0.03 (0.01/0.00)	2.57 (0.76/0.28)	5.90 (1.40/0.47)	3.0 – 5.0	0.0706	0.34 (0.15/0.08)

TABLE III: Lepton-jet tagging efficiency ϵ_{LJ} (%) in $pp \rightarrow bW\bar{b}W + \ell^+\ell^-$ for signal (for given $m_{H^\pm}$ and $m_{Z'}$) and background (from virtual photon and virtual Z boson) at the 8 and 14 TeV LHC. The numbers in parentheses ($\epsilon_{(LJ+CMS[1b])}/\epsilon_{(LJ+CMS[2b])}$) are the efficiencies when we require additional selection cuts, requiring one b -tagged or two b -tagged jets as described in Appendix A 2. Coupling structure of Z' to the lepton does not give a significant effect on the tagging efficiency. In the above table, we take axial coupling as an example. For backgrounds, we set the trigger of a $m_{\ell+\ell^-}$ mass window as in the table to enlarge statistics.

with boost factors (rapidity) of $H^\pm$ and Z' as

$$\eta_{H^\pm} = \cosh^{-1} \left(\frac{m_t^2 + m_{H^\pm}^2 - m_b^2}{2m_t m_{H^\pm}} \right), \quad (A9)$$

$$\eta_{Z'} = \cosh^{-1} \left(\frac{m_{H^\pm}^2 + m_{Z'}^2 - m_W^2}{2m_{Z'} m_{H^\pm}} \right). \quad (A10)$$

Thus if we assume that a distribution of the geometric average of leptons' P_T is localized around $P_T^{\text{peak}} \equiv \frac{1}{2}E_\ell^{\text{(cusp)}}$, we can estimate the peak of $\Delta R (= \Delta R^{\text{(peak)}})$ between two leptons from Z' decays with Eq. (A2) by

$$\Delta R^{\text{(peak)}} \sim \cosh^{-1} \left(\frac{2m_{Z'}^2}{(E_\ell^{\text{(cusp)}})^2} + 1 \right). \quad (A11)$$

With this simple kinematical study, we can explain why ΔR will be the major criteria for a lepton-jet tagging. For example, with $m_{H^\pm} = 140$ GeV, P_T of the

second hardest lepton (P_{T2}) does not change much from $m_{Z'} = 1$ to 5 GeV (Fig. 5). This can be understood since P_T^{peak} does not change much from 18.96 to 18.95 GeV with Eq. (A7). But the corresponding $\Delta R^{\text{(peak)}}$ will change significantly to the point to change lepton-jet tagging efficiency from $\Delta R^{\text{(peak)}} \sim 0.05$ to 0.26 estimated by Eq. (A11). The observed peak is similar to this estimation as in Fig. 5. (For $m_{H^\pm} = 100$ GeV, estimated $\Delta R^{\text{(peak)}}$ is over estimated by a factor of 2 since the actual P_T of leptons is not very well localized.) Thus, for a large $m_{Z'}$, lepton-jet tagging efficiency is low due to large ΔR between leptons from Z' .

Now we consider the effect from the mass of charged Higgs. The P_T of leptons increases with $m_{H^\pm}$. At the same time, due to the dilepton mass relation, Eq. (A2), ΔR decreases with $m_{H^\pm}$. This effect from ΔR is greater than the effect from P_T , and the lepton-jet tagging efficiency increases with $m_{H^\pm}$.

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