

# Nucleon $g_2$ Structure Function and Quark-Gluon Correlations

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# Outline

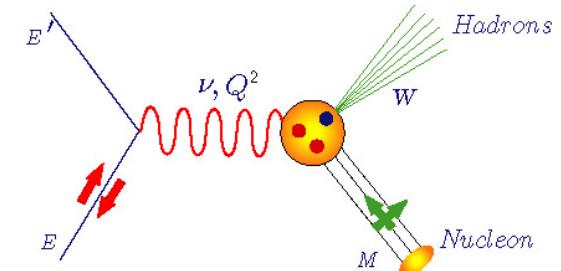
- Quark-gluon correlations: Average Color Lorentz force, Color polarizabilities
  - ➔ Nucleon  $g_2$  and  $g_1$  spin structure functions
  - ➔ Twist-3  $d_2$  and twist-4  $f_2$  matrix elements
  - ➔  $d_2^n$  (E06-114 in Hall A) and SANE (E07-003 in Hall C) experiments at Jefferson Lab
  - ➔ Future prospects

# Spin Structure Functions

- Unpolarized structure functions  $F_1(x, Q^2)$  and  $F_2(x, Q^2)$

U 
$$\frac{d^2\sigma}{dE'd\Omega}(\downarrow\uparrow + \uparrow\uparrow) = \frac{8\alpha^2 \cos^2(\theta/2)}{Q^4} \left[ \frac{F_2(x, Q^2)}{\nu} + \frac{2F_1(x, Q^2)}{M} \tan^2(\theta/2) \right]$$

- Polarized structure functions  $g_1(x, Q^2)$  and  $g_2(x, Q^2)$



$Q^2$  : Four-momentum transfer  
 $x$  : Bjorken variable  
 $\nu$  : Energy transfer  
 $M$  : Nucleon mass  
 $W$  : Final state hadrons mass

L 
$$\frac{d^2\sigma}{dE'd\Omega}(\downarrow\uparrow - \uparrow\uparrow) = \frac{4\alpha^2}{MQ^2} \frac{E'}{\nu E} \left[ (E + E' \cos \theta) g_1(x, Q^2) - \frac{Q^2}{\nu} g_2(x, Q^2) \right]$$

T 
$$\frac{d^2\sigma}{dE'd\Omega}(\downarrow\Rightarrow - \uparrow\Rightarrow) = \frac{4\alpha^2 \sin \theta}{MQ^2} \frac{E'^2}{\nu^2 E} \left[ \nu g_1(x, Q^2) + 2E g_2(x, Q^2) \right]$$

# Example of a standard setup in Hall A

## Polarized beam

Energy: 0.86-5.1 GeV

Polarization: > 70%

Average Current: 5 to 15  $\mu$ A

## Hall A polarized $^3\text{He}$ target

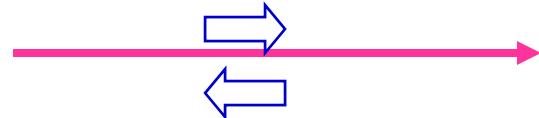
Pressure ~ 10 atm

Polarization average: 35%

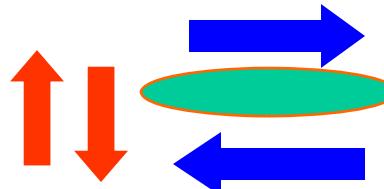
Length: 40 cm with 100  $\mu\text{m}$  thickness

Highest polarized luminosity  $\sim 10^{36} \text{cm}^{-2}\text{s}^{-1}$

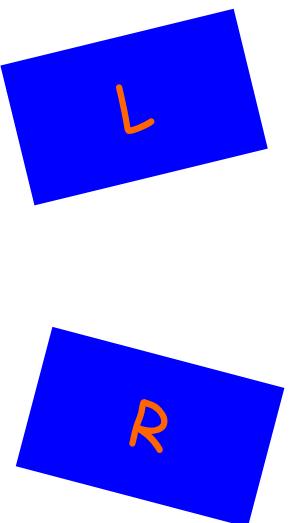
## Electron beam



## Hall A polarized $^3\text{He}$ target



Spectrometers  
set at  $15.5^\circ$



- Measurement of helicity dependent  $^3\text{He}$  cross sections
- Extract  $g_1$  and  $g_2$  spin structure functions of  $^3\text{He}$
- Extract moments of spin structure functions of  $^3\text{He}$  and Neutron

# $g_2$ and Quark-Gluon Correlations



$$g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$$

- a twist-2 term (Wandzura & Wilczek, 1977):

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 g_1(y, Q^2) \frac{dy}{y}$$

- a twist-3 term with a suppressed twist-2 piece (Cortes, Pire & Ralston, 1992):

$$\bar{g}_2(x, Q^2) = - \int_x^1 \frac{\partial}{\partial y} \left[ \frac{m_q}{M} h_T(y, Q^2) + \xi(y, Q^2) \right] \frac{dy}{y}$$

Transversity    q-g correlations

# Quark-Gluon Correlations

## ● How did we investigate them?

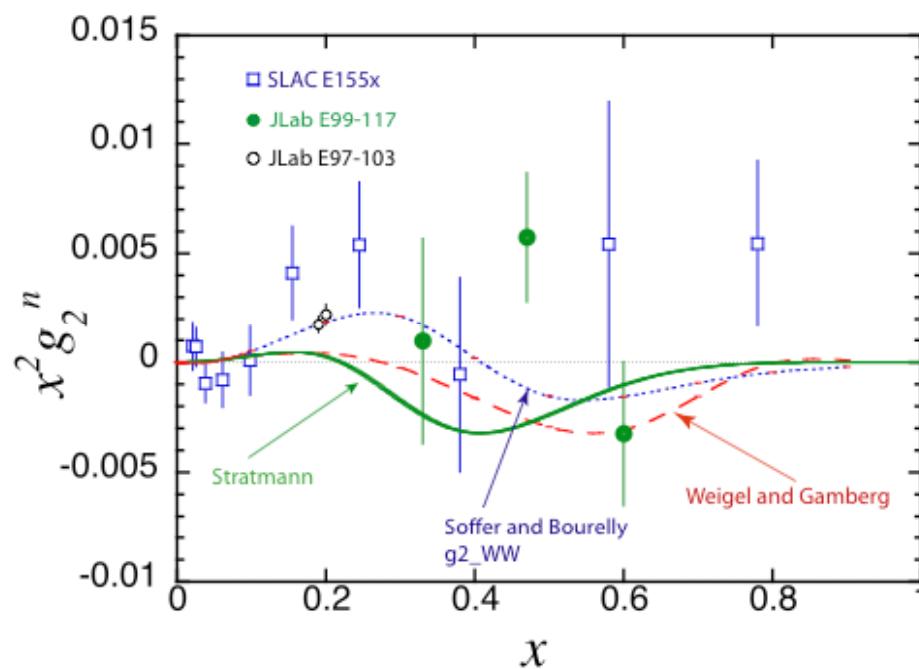
- By direct comparison of  $g_2$  to  $g_2^{\text{WW}}$  to observe deviations
- As for any other nucleon structure function it is hard to have ab-initio calculation of  $g_2$ .
- Quark models are can be useful to gain insight

## ● Second moment of $g_2$ offers another avenue of investigation

- Moments of  $\overline{g_2}$  can be calculated using lattice QCD since they correspond to specific matrix elements of quark and gluon field operators
- These matrix elements have a physical interpretation
  - Average Color Lorentz Force (M. Burkhardt)
  - "Color polarizabilities" (X. Ji, Stein et al.)

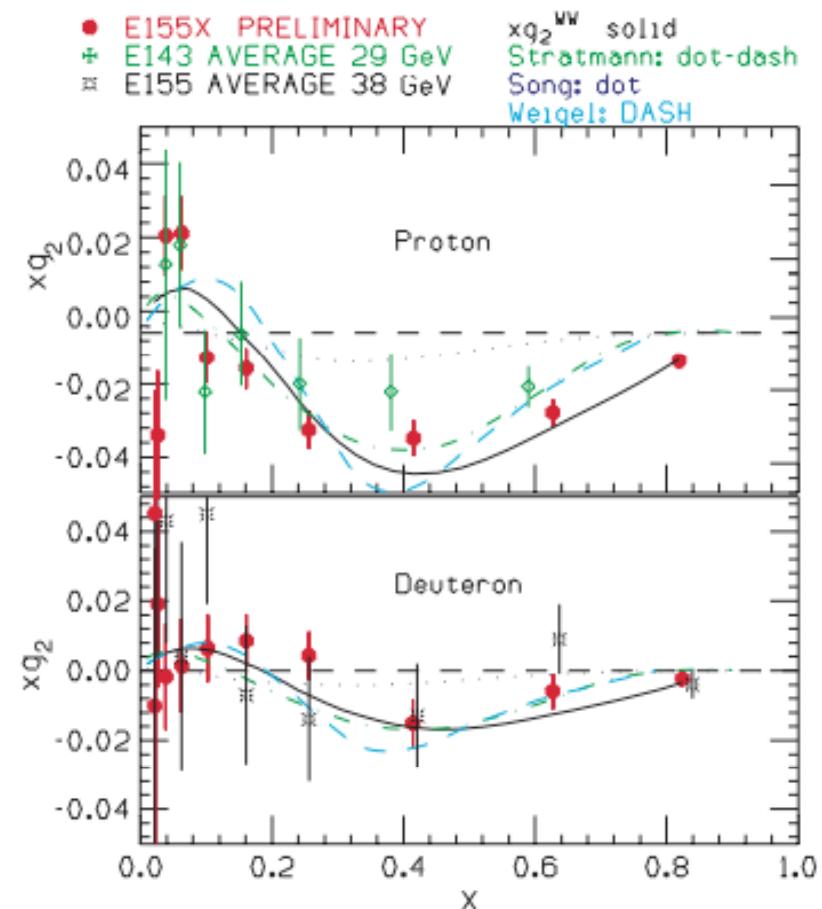
# Nucleon world results of $g_2$

## Neutron



- SLAC E155x (proton and deuteron)
- JLab E99-117(helium-3),  $A_1^n$  in DIS
- Jlab E97-103 (helium 3) DIS,  $Q^2$  dependence mainly below  $1.4 \text{ GeV}^2$

## Proton and Deuteron



SLAC E155x (proton and deuteron)

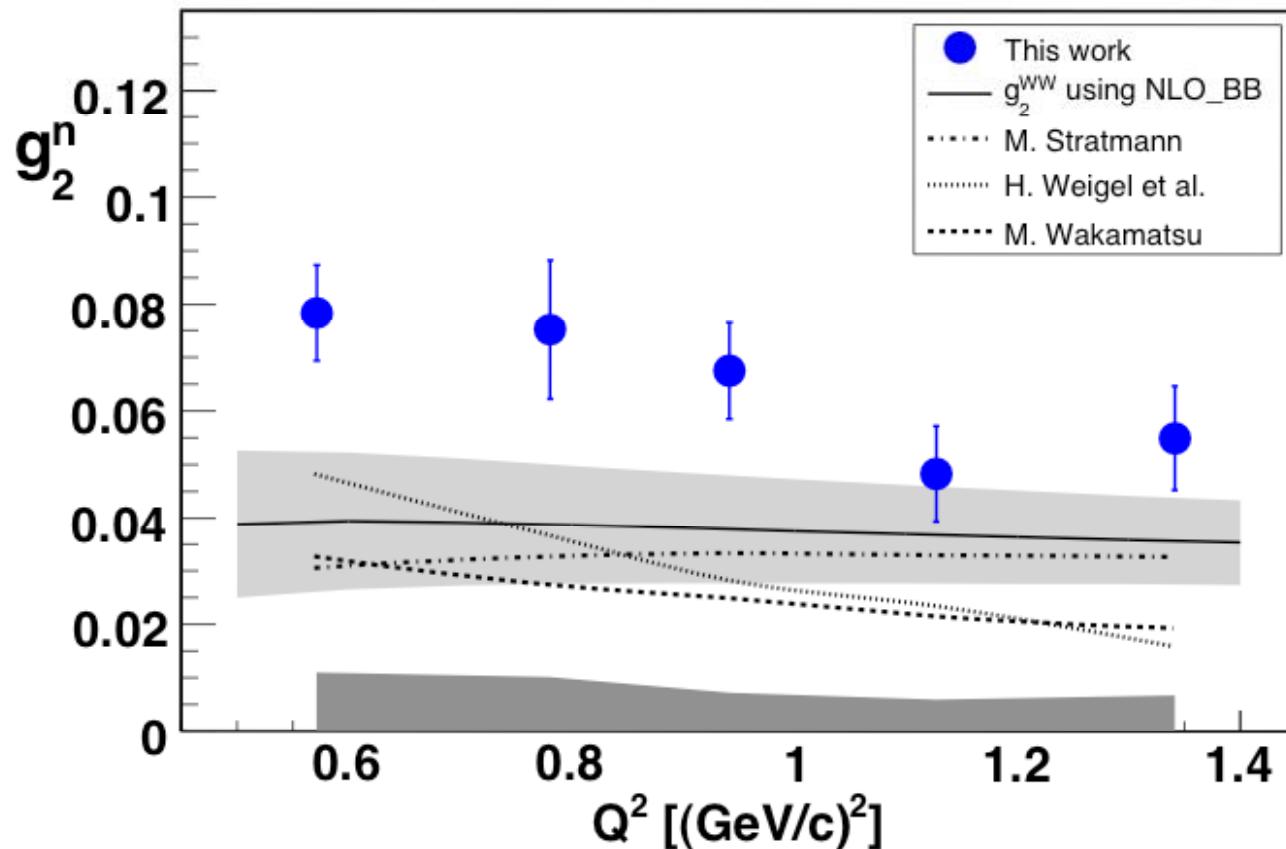
# $Q^2$ dependence below 1 $\text{GeV}^2$

JLab E97-103 (helium 3) DIS,  $Q^2$  dependence mainly below 1.4  $\text{GeV}^2$

Spokespersons: T. Averett and W. Korsch

Student: K. Kramer

Phys. Rev. Lett. 95:142002, 2005.



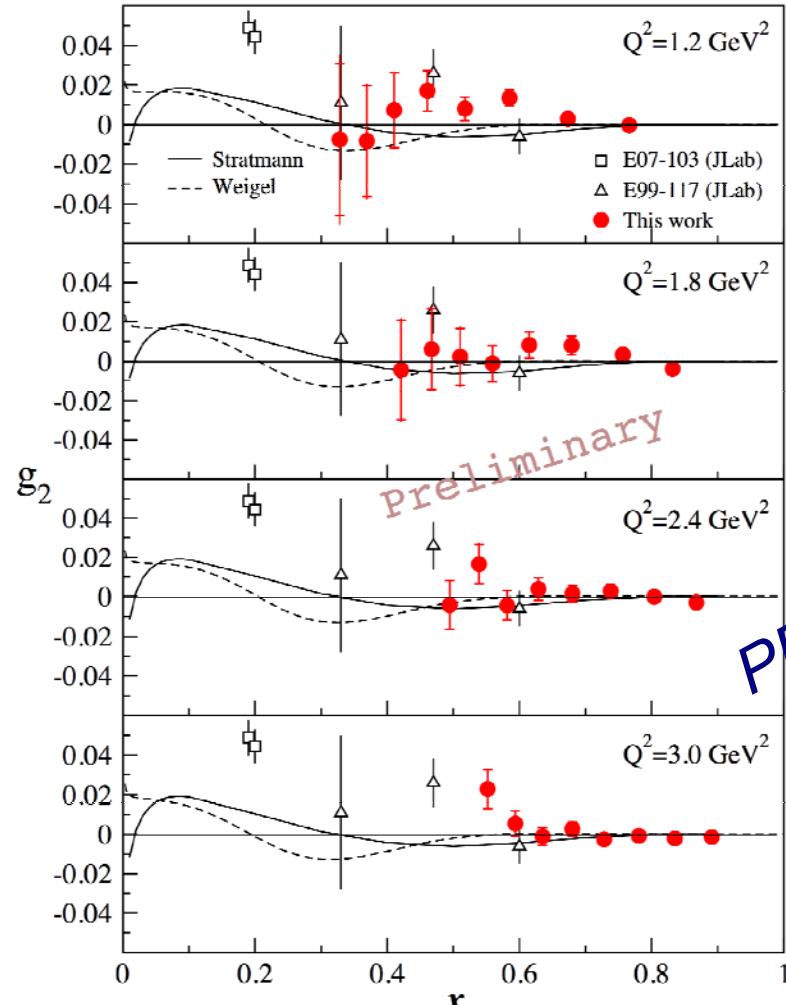
# $x^2 g_2 {}^{3\text{He}}$ at constant $Q^2$

JLab Experiment E01-012

Phys.Rev.Lett. 101:182502, 2008.

Spokespersons: J.P Chen,  
Seonho Choi and N. Liyanage

Thesis student: P. Solvignon



Statistical errors only

# Moments of Structure Functions

$$d_2(Q^2) = 3 \int_0^1 x^2 (g_2(x, Q^2) - g_2^{WW}(x, Q^2)) dx$$

$$d_2 S^{[\mu} P^{\{\nu} P^{\lambda\}} = \frac{1}{8} \sum_q \langle P, S | \bar{\psi}_q \, g \bar{F}^{\{\mu\nu} \gamma^{\lambda\}} \psi_q | P, S \rangle$$

$d_2(Q^2)$  → dynamical twist-3 matrix element

$$d_2(Q^2) = \int_0^1 dx \, x^2 [2\mathbf{g}_1(x, Q^2) + 3\mathbf{g}_2(x, Q^2)]$$

# "Color Polarizabilities"

X.Ji 95, E. Stein et al. 95

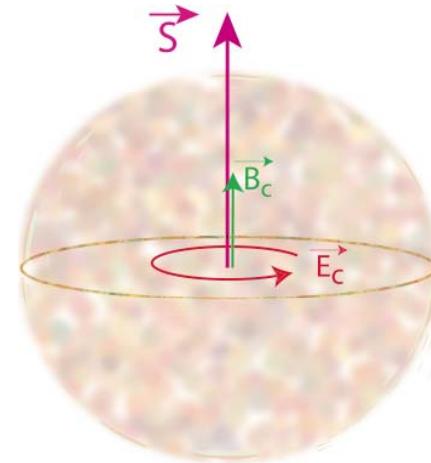
How does the gluon field respond when  
a nucleon is polarized ?

Define color magnetic and electric polarizabilities (in nucleon rest frame):

$$\chi_{B,E} 2M^2 \vec{S} = \langle PS | \vec{O}_{B,E} | PS \rangle$$

where  $\vec{O}_B = \psi^\dagger g \vec{\mathbf{B}} \psi$

$$\vec{O}_E = \psi^\dagger \vec{\alpha} \times g \vec{\mathbf{E}} \psi$$



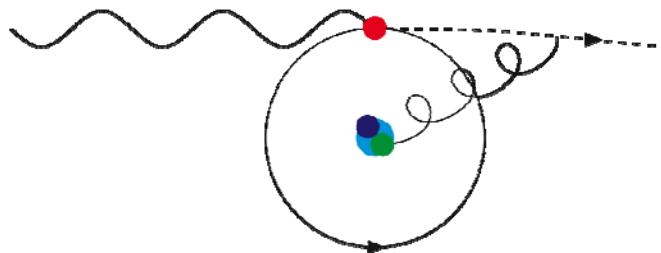
$$d_2 = (\chi_E + 2\chi_B)/8$$

$$f_2 = (\chi_E - \chi_B)/2$$

$d_2$  and  $f_2$  represent the response of the color  $\vec{\mathbf{B}}$  &  $\vec{\mathbf{E}}$  fields  
to the nucleon polarization

# Average Color Lorentz Force (M. Burkardt)

$$\int dx x^2 \bar{g}_2(x) = \frac{1}{3} d_2 = \frac{1}{6 M P^+{}^2 S^x} \langle P, S | \bar{q}(0) g G^{+y}(0) \gamma^+ q(0) | P, S \rangle$$



- $d_2$  a measure for the **color Lorentz force** acting on the struck quark in SIDIS in the instant **after being hit by the virtual photon**

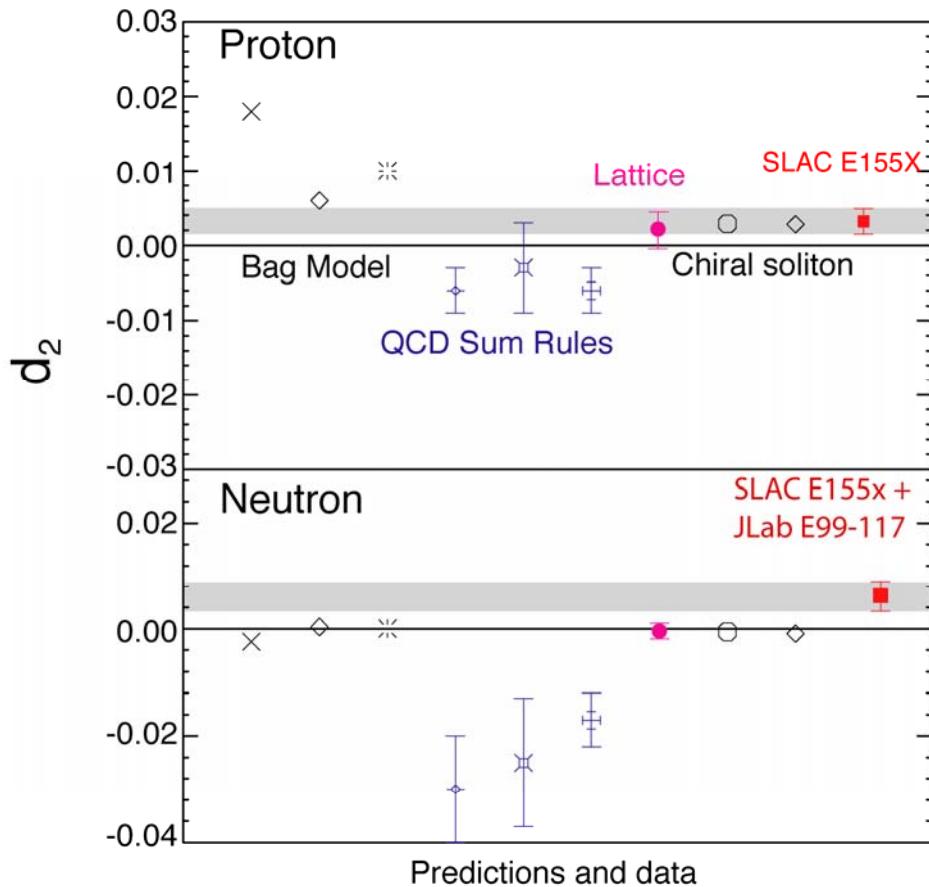
$$\langle F^y(0) \rangle = -M^2 d_2 \quad (\text{rest frame; } S^x = 1)$$

- Interpretation of  $d_2$  with the transverse FSI force in DIS also consistent with  $\langle k_\perp^y \rangle \equiv \int_0^1 dx \int d^2 k_\perp k_\perp^2 f_{1T}^\perp(x, k_\perp^2)$  in SIDIS (Qiu, Sterman)

$$\langle k_\perp^y \rangle = -\frac{1}{2p^+} \left\langle P, S \left| \bar{q}(0) \int_0^\infty dx^- g G^{+y}(x^-) \gamma^+ q(0) \right| P, S \right\rangle$$

semi-classical interpretation: average  $k_\perp$  in SIDIS obtained by correlating the quark density with the transverse impulse acquired from (color) Lorentz force acting on struck quark along its trajectory to (light-cone) infinity

# Models and Lattice evaluations of $d_2$



## Quark Bag Models

M.Stratmann, Z.Phys.C60,763(1993).

X.Song,Phys.Rev.D54,1955(1996).

X.Ji and P.Unrau, Phys.Lett.B333,228(1994).

## Chiral Soliton Model

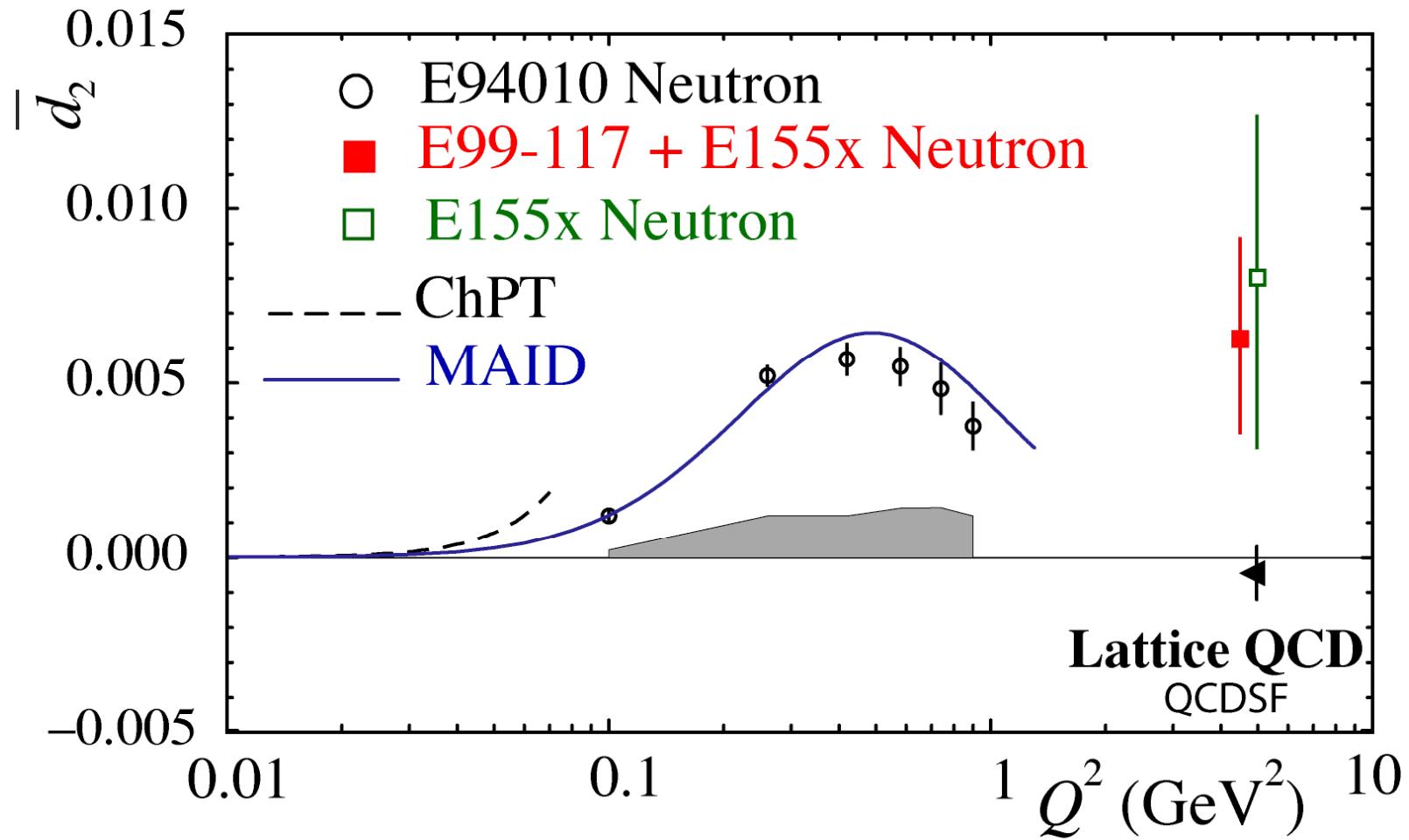
H.Weigel and L.Gamberg,  
Nucl. Phys. A680, 48 (2000).

M.Wakamatsu, Phys. Lett. B487,118(2000).

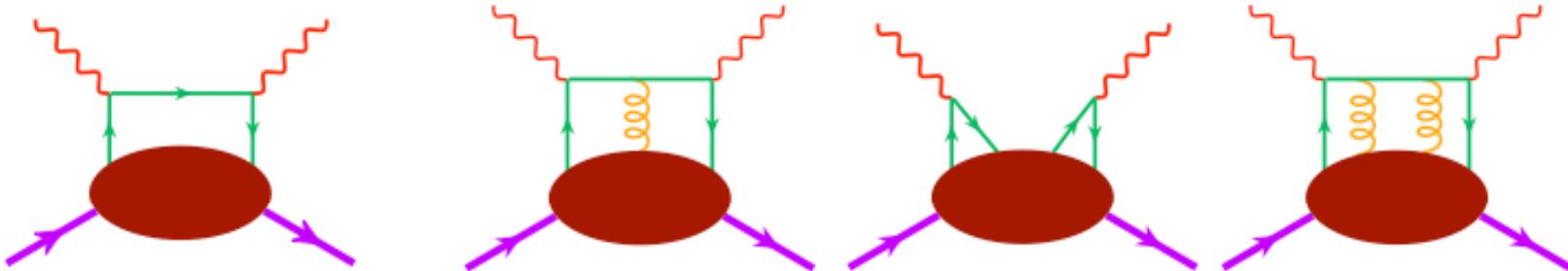
## Lattice QCD

M.Gockeler et al.,  
Phys.Rev.D72:054507,(2005)

## *$Q^2$ evolution of the neutron "d<sub>2</sub>"*



# Moments of Structure Functions (continued)



$$\tau = 2$$

single quark  
scattering

$$\tau > 2$$

*qq* and *qg*  
correlations

$$\begin{aligned} \rightarrow \Gamma_1(Q^2) &\equiv \int_0^1 dx g_1(x, Q^2) \\ &= \Gamma_1^{\text{twist-2}}(Q^2) + \frac{M_N^2}{9Q^2} [a_2(Q^2) + 4d_2(Q^2) + 4f_2(Q^2)] + \mathcal{O}\left(\frac{M_N^4}{Q^4}\right) \end{aligned}$$

# Moments of Structure Functions (continued)

$$\rightarrow a_2(Q^2) \equiv 2 \int_0^1 dx x^2 g_1^{\text{twist-2}}(x, Q^2) \rightarrow \text{target mass correction term}$$

$\rightarrow d_2(Q^2) \rightarrow$  dynamical twist-3 matrix element

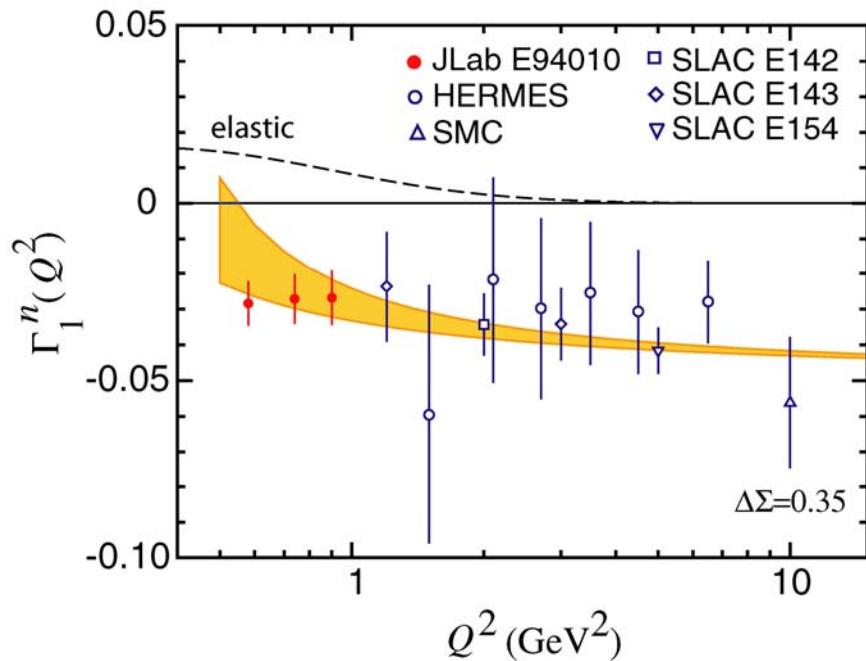
$$d_2(Q^2) = \int_0^1 dx x^2 [2g_1(x, Q^2) + 3g_2(x, Q^2)]$$

$\rightarrow f_2(Q^2) \rightarrow$  dynamical twist-4 matrix element

$$f_2(Q^2) = \frac{1}{2} \int_0^1 dx x^2 [7g_1(x, Q^2) + 12g_2(x, Q^2) - 9g_3(x, Q^2)]$$

$$f_2 M^2 S^\mu = \frac{1}{2} \sum_q e_q^2 \langle N | \bar{\psi}_q g \tilde{F}^{\mu\nu} \gamma_\nu \psi_q | N \rangle$$

# Twist-4 neutron matrix element $f_2$



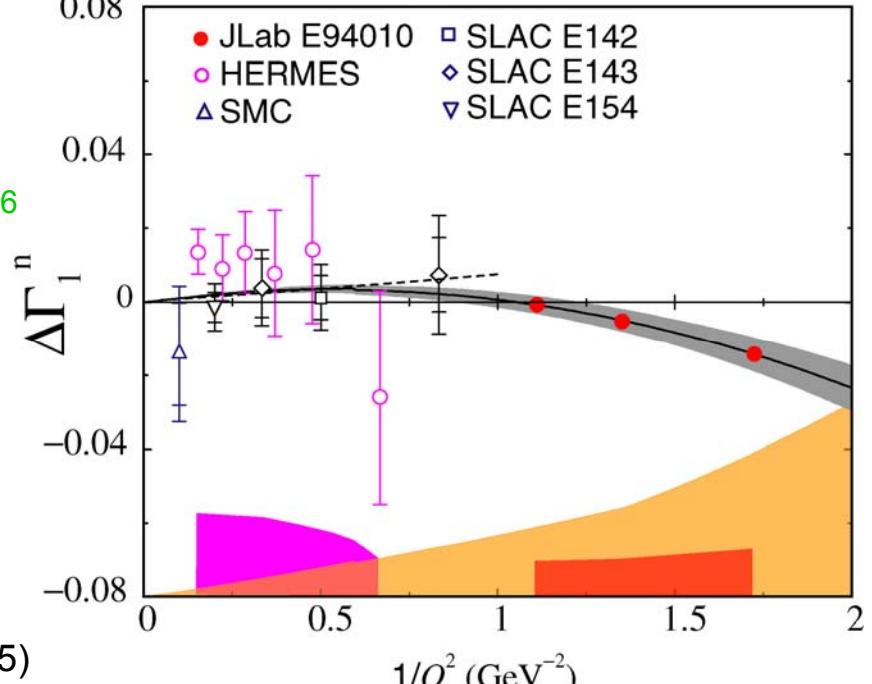
Adding  $1/Q^6$  term gives the same  $f_2$  and  $\mu_6$   
with  $\mu_8 = (0.00 \pm 0.03)M^2$

$$\begin{aligned}\Delta\Gamma_1^n(Q^2) &\equiv \Gamma_1^n(Q^2) - \mu_2^n(Q^2) \\ &= \frac{\mu_4^n(Q^2)}{Q^2} + \frac{\mu_6^n(Q^2)}{Q^4} + \mathcal{O}\left(\frac{1}{Q^6}\right)\end{aligned}$$

$$\mu_4^n = \frac{1}{9}M^2(a_2^n + 4d_2^n + 4f_2^n)$$

$$f_2^n = 0.033 \pm 0.005, \quad \mu_6^n = (-0.019 \pm 0.002)M^4$$

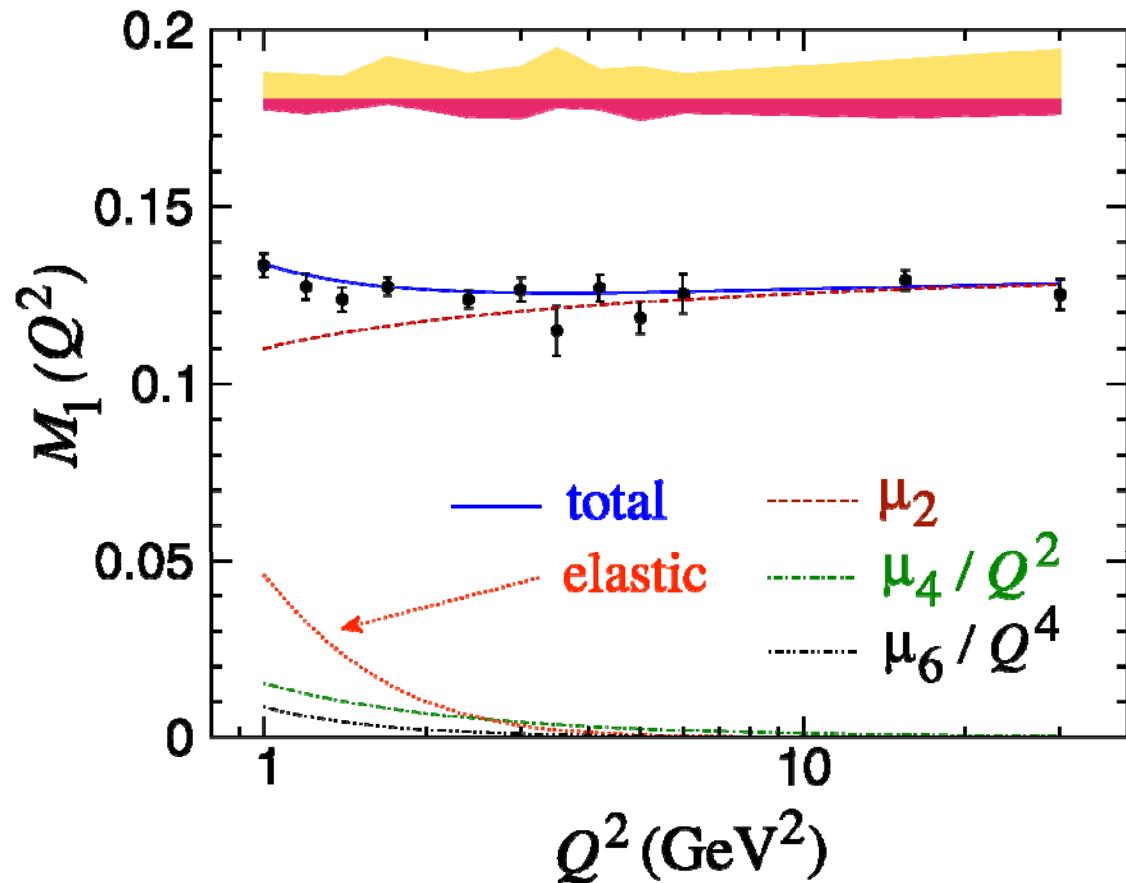
$$f_2^n = 0.034 \pm 0.043, \quad \mu_6^n = (-0.019 \pm 0.017)M^4$$



# Determination of $f_2$ for the proton

World data + EG1a data: R. Fatemi et al., PRL, 91 22200 (2003)

Osipenko et al. Phys. Lett. B 609, 258 (2005)



$$f_2 = 0.039^{+0.037}_{-0.043}$$

$$\mu_6/M^4 = 0.011^{+0.017}_{-0.013}$$

# Hall A $d_2^n$ and Hall C SANE experiments

## Neutron and Proton

Spokespeople:

B. Sawatzky, S. Choi, X. Jiang and Z.-E.M

Students:

D. Flay, D. Parno, M. Posik

and the Hall A collaboration

Spokespeople:

O. Rondon, S. Choi, M. Jones,, Z.-E. M

Students:

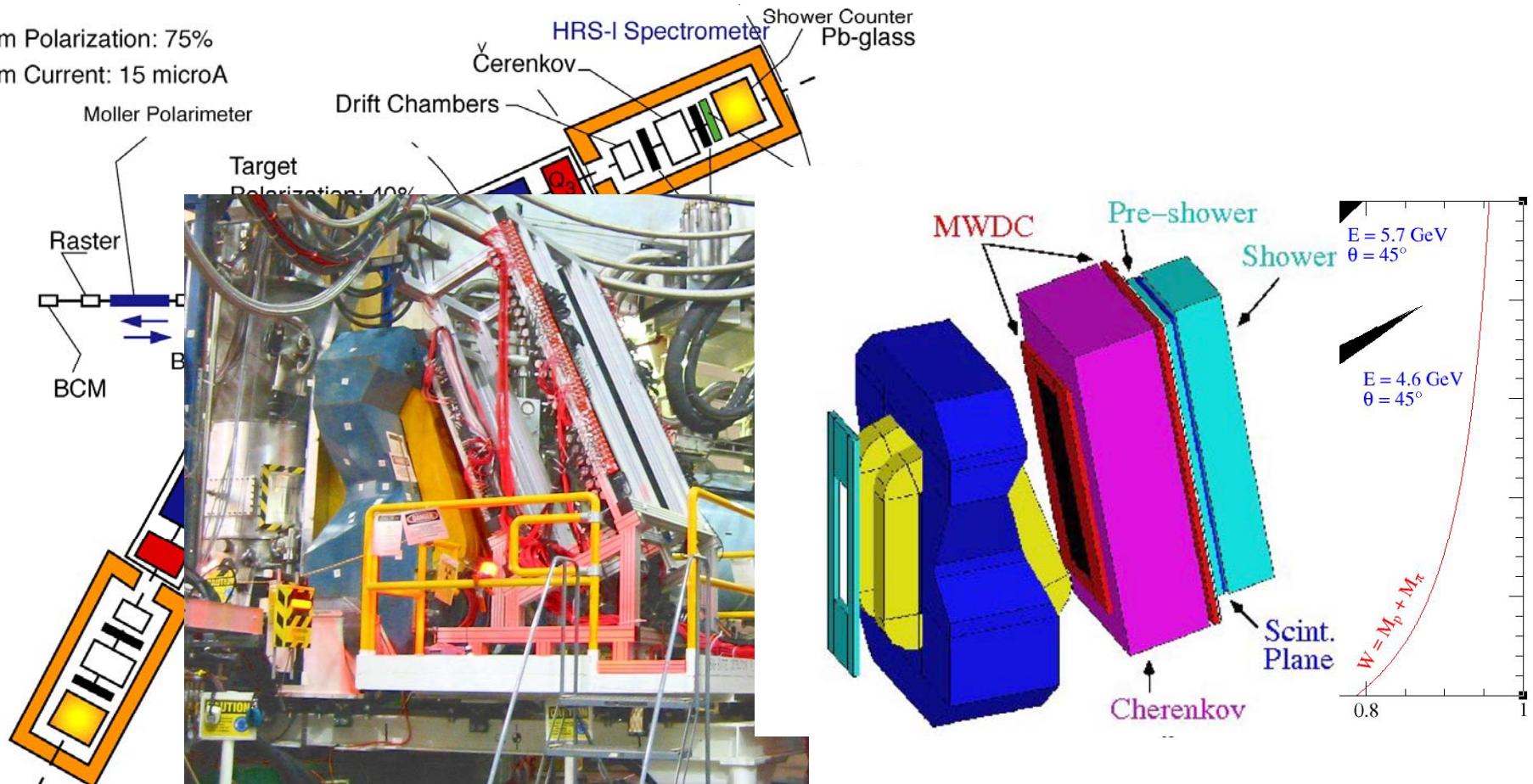
W. Armstrong, H. Kang, A. Liyanage, J. Maxwell,  
J. Mulholland

and the Hall C collaboration

# Experiment E06-114 ( $d_2^n$ ) in Hall A

Beam Polarization: 75%

Beam Current: 15 microA



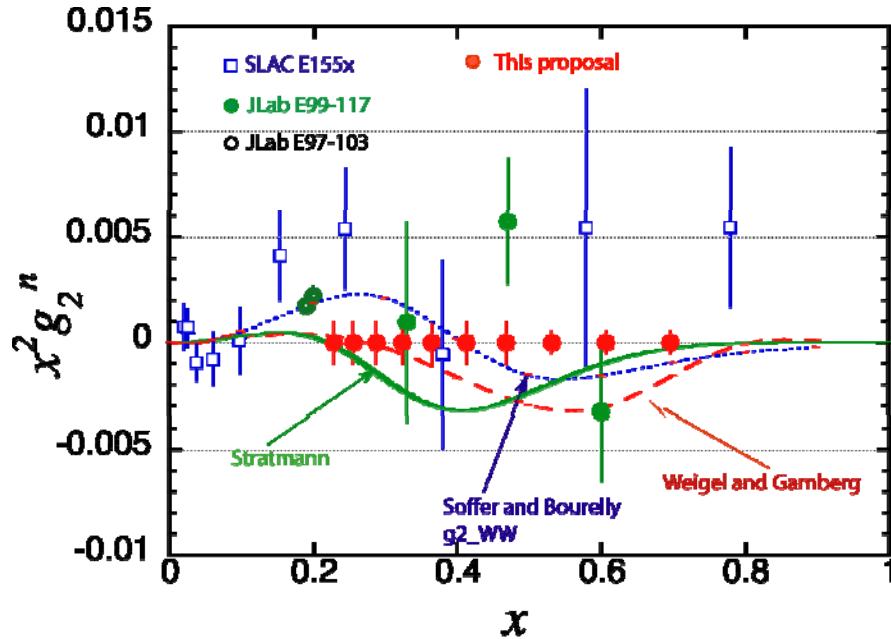
Two beam energies **4.6** and **5.7 GeV**  
(4 pass, 5 pass)

**BigBite** fixed at single scattering angle ( $\approx 45^\circ$ )  
(data divided into 10 bins during analysis)

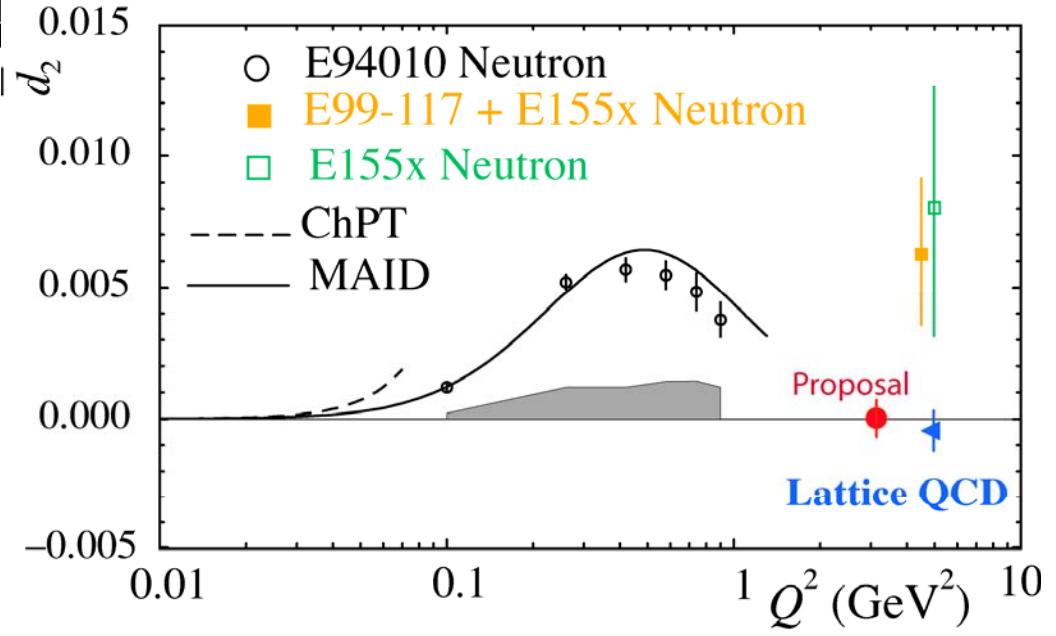
Experiment ran Jan.-Mar. 09  
May-30, 2009

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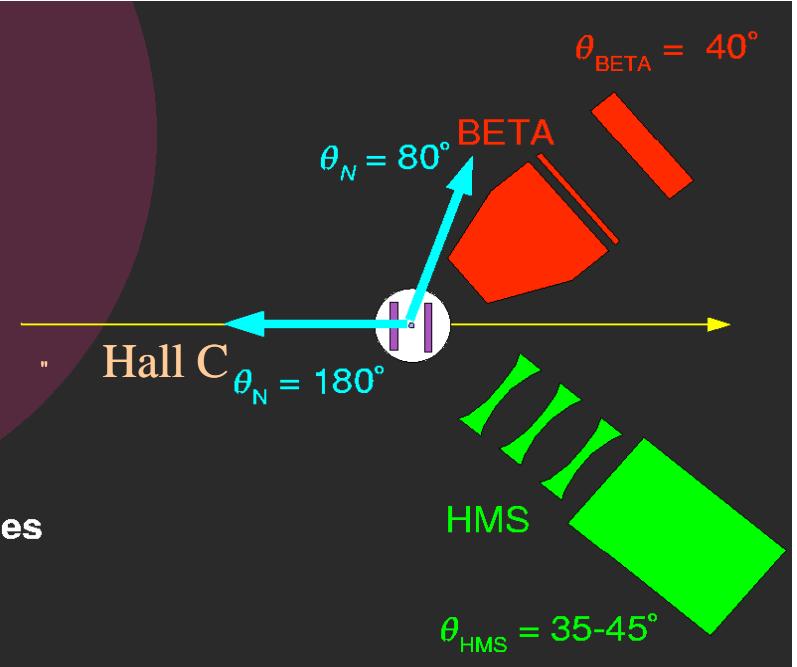
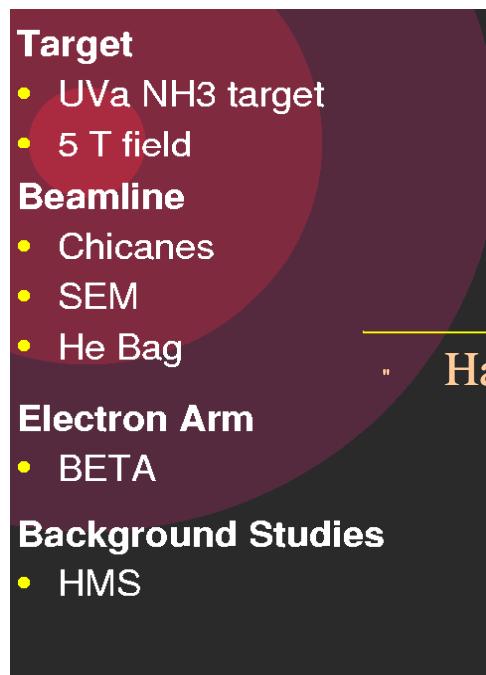
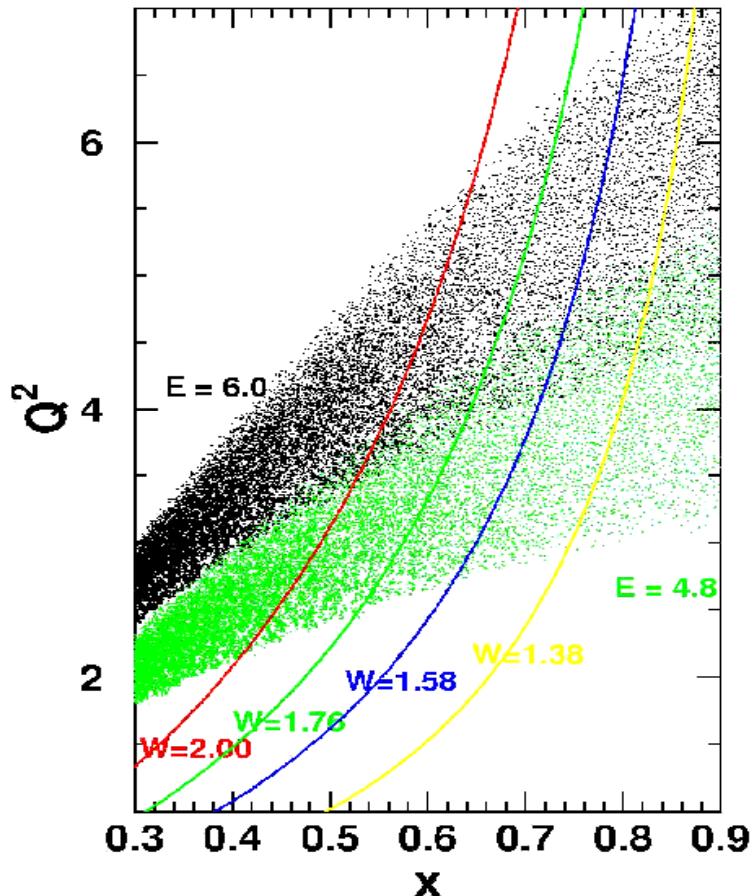
# Expected precision in Experiment E06-114



- At large  $Q^2$ ,  $d_2$  coincides with the reduced twist-3 matrix element of gluon and quark operators
- At low  $Q^2$ ,  $d_2$  is related to the spin polarizabilities



# SANE experiment in Hall C



- ➊ Two beam energies:
  - 6.0 GeV (black)
  - 4.8 GeV (green)

CEBAF polarized beam

- 85 nA
- 75% beam polarization

Experiment Ran January-March 09

# BETA detector

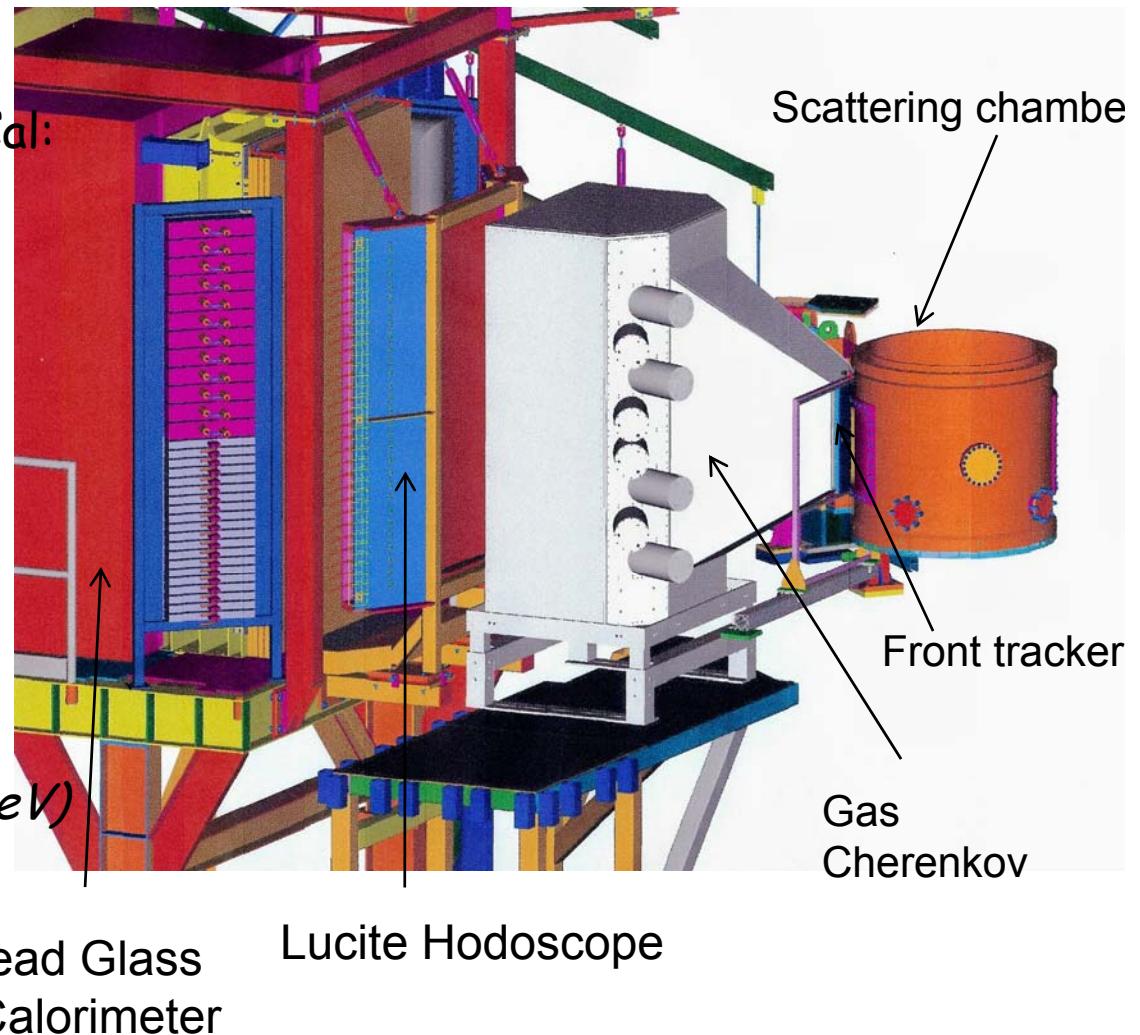
- Three subsystems:

- Lead glass calorimeter BigCal: Energy Measurement
- Gas Cherenkov:  $e^-$  identification
- Lucite hodoscope: tracking
- Front tracker: tracking

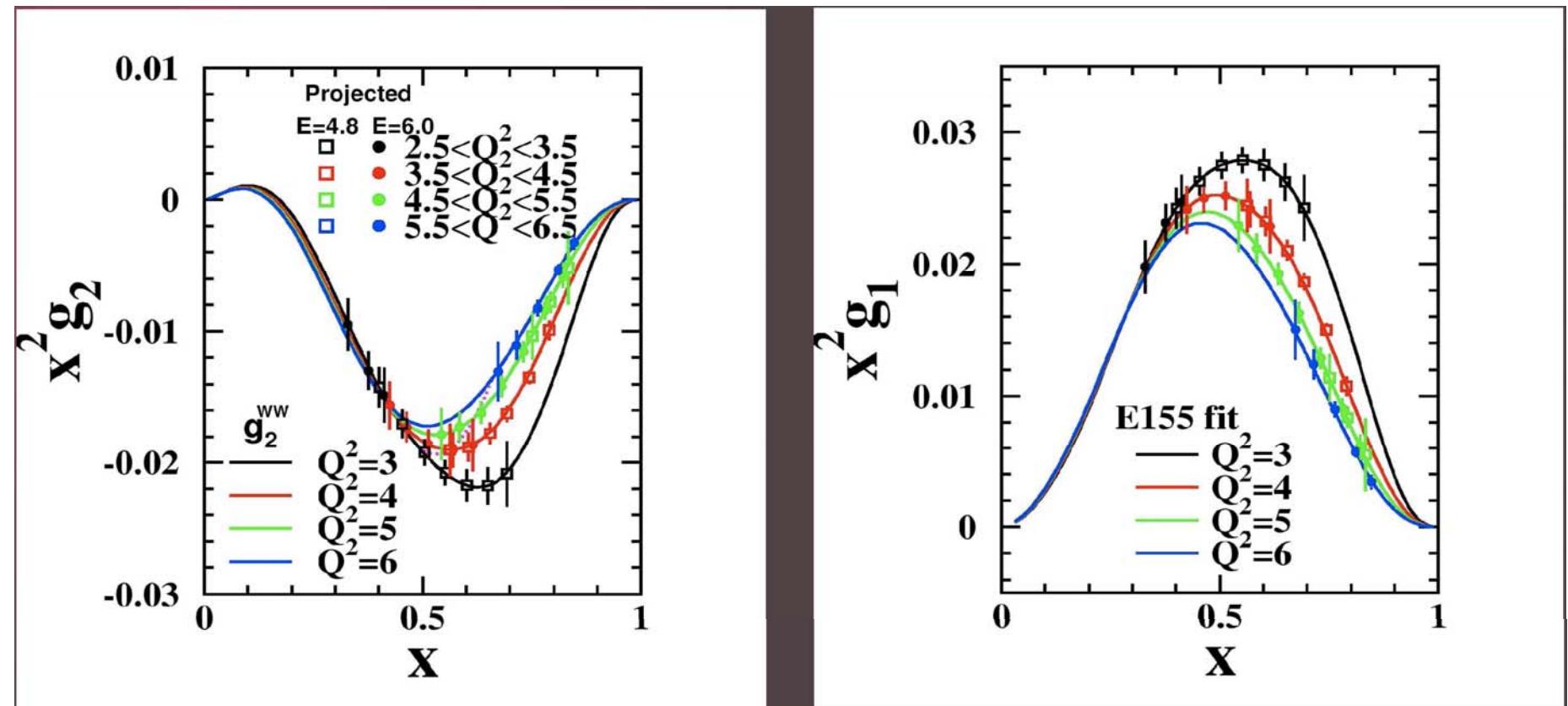
- Target field sweeps low  $E$  background

- Characteristics

- Effective solid angle (with cuts) = 0.194 sr
- Energy resolution  $5\%/\sqrt{E(\text{GeV})}$
- angular resolution =  $2^\circ$
- 1000:1 pion rejection



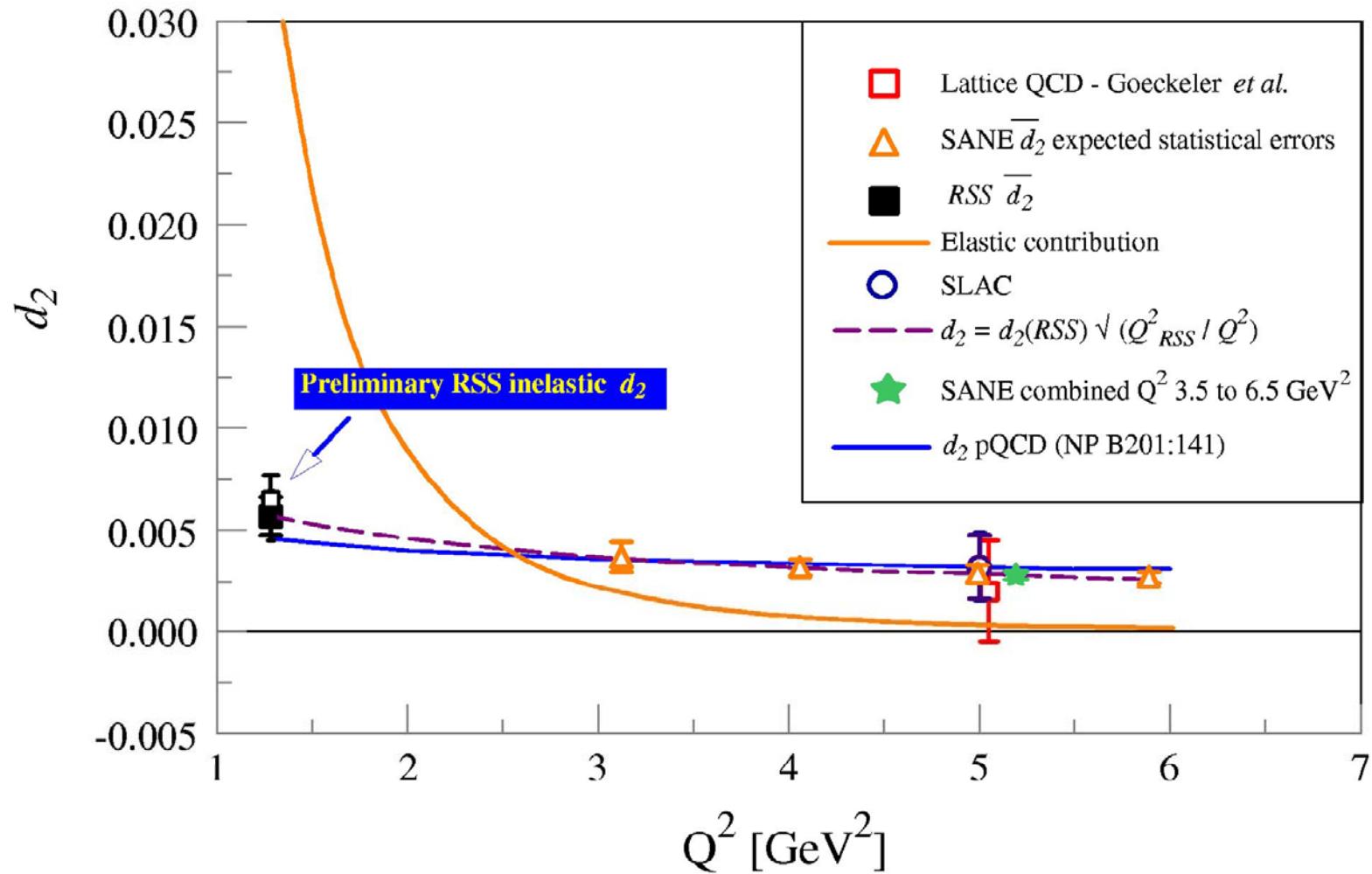
# SANE experiment $g_2, g_1$ projected errors



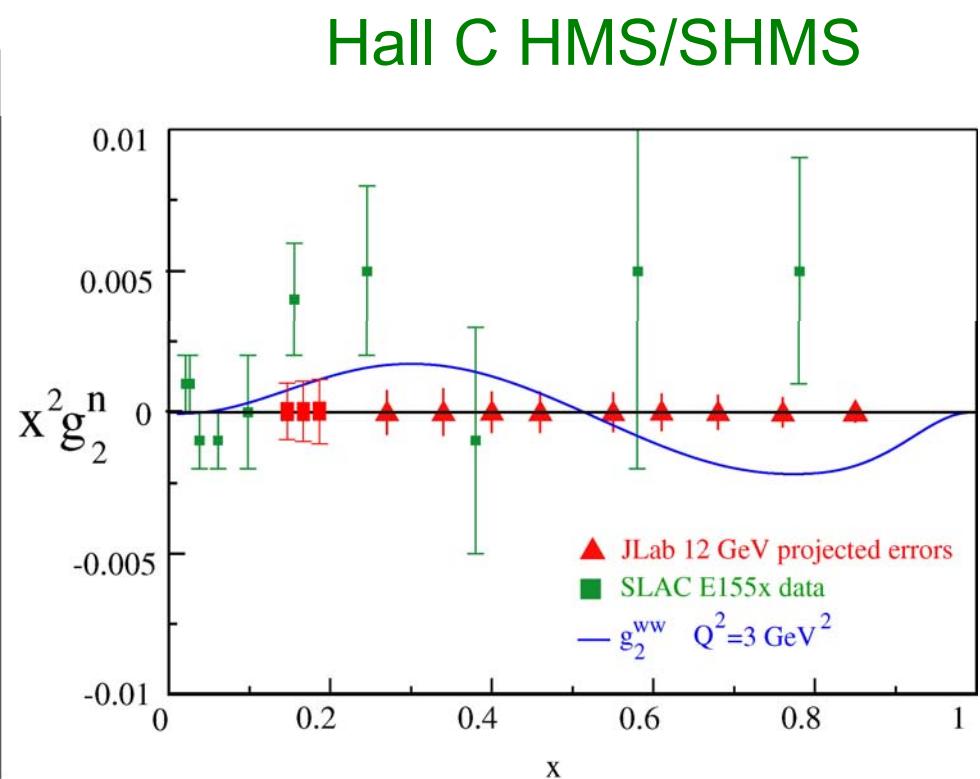
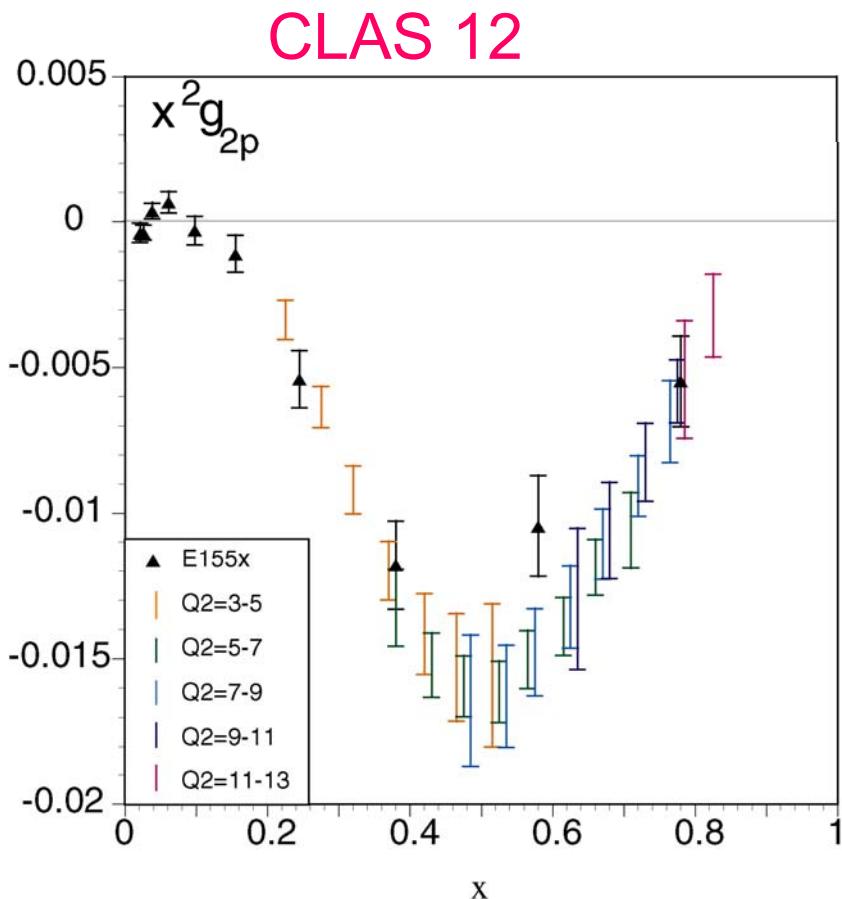
# $d_2^p$ RSS and SANE $d_2^p$ projection in Hall C

RSS spokespersons: M. Jones, O. Rondon

SANE spokespersons: S. Choi, M. Jones, O. Rondon, Z.-E. M



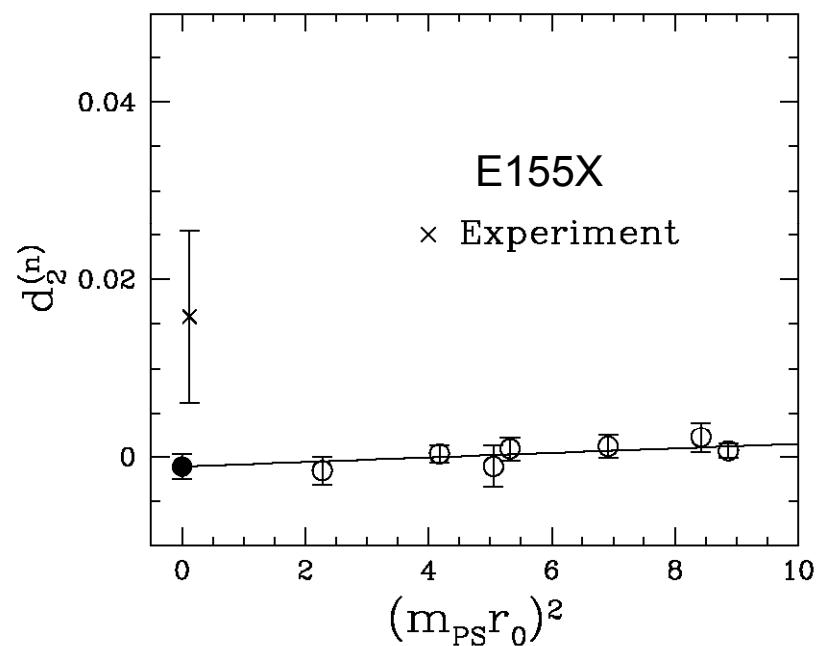
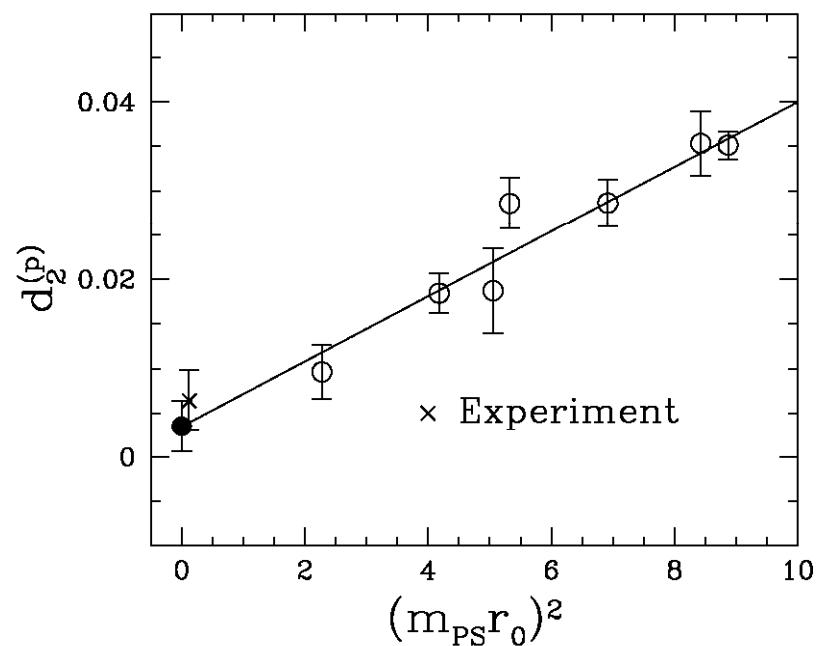
# $g_2$ at JLab with 11 GeV



# Summary

- Past experiments on the neutron and proton suggest that the twist-3 and twist-4 are small but finite.
- Precision measurements of  $g_1$  and  $g_2$  in the range  $1 < Q^2 < 4 \text{ GeV}^2$  are crucial for an improved extraction of the
  - ➔ Average color Lorentz force
  - ➔ "Color polarizabilities"
- In the next year or two we will have results from two recently ran experiments at Jefferson Lab, SANE in Hall C (proton) and E06-14 in Hall A (neutron).
- The non-singlet combination ( $d_2^p - d_2^n$ ) should provide a benchmark test for present lattice QCD calculations since no disconnected diagrams are needed.
- This program will be pursued at JLab 11 GeV for higher precision and greater  $Q^2$  and  $x$  coverage.

# QCDSF Collaboration Lattice Calculations

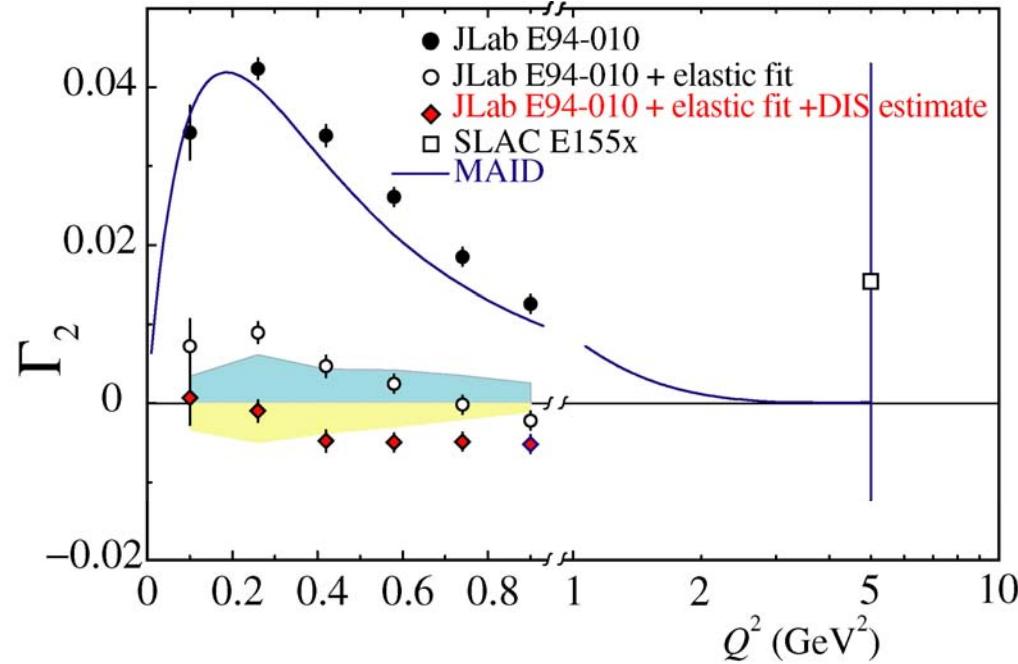


hep-lat/0506017

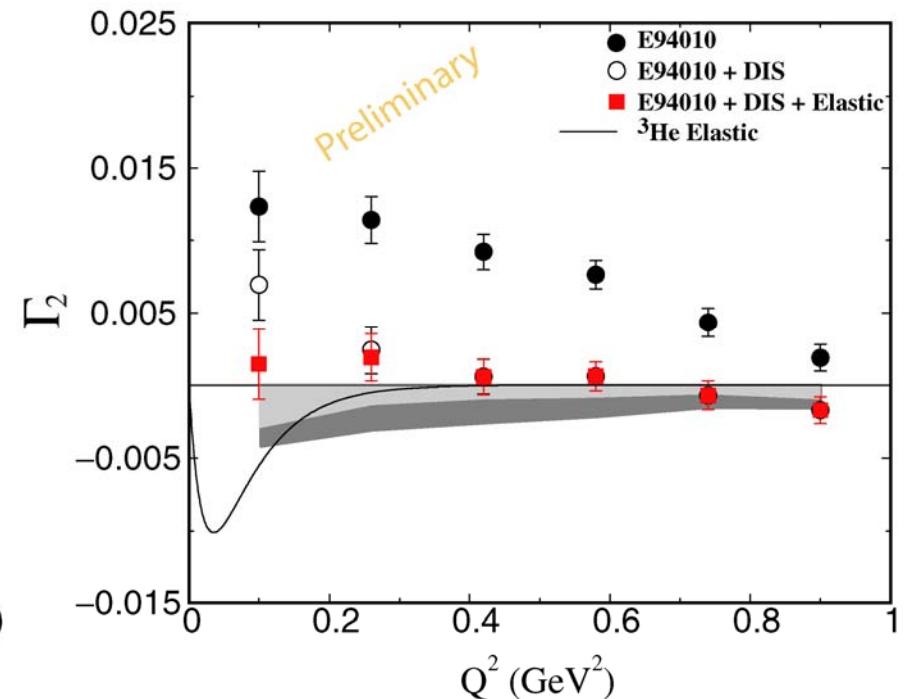
M. G\"ockeler, R. Horsley, D. Pleiter, P.E.L. Rakow, A. Sch\"afer, G. Schierholz, H. St\"uben, J.M. Zanotti

# E94-010 B-C sum rule; results

Neutron



$^3\text{He}$



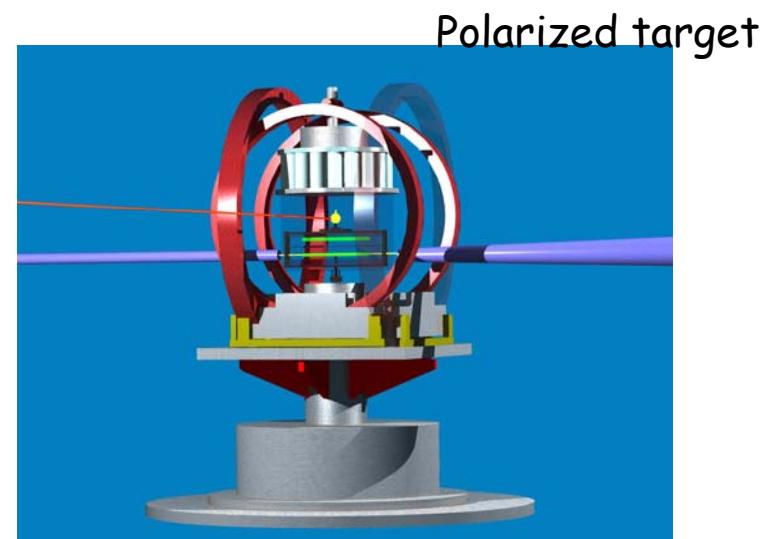
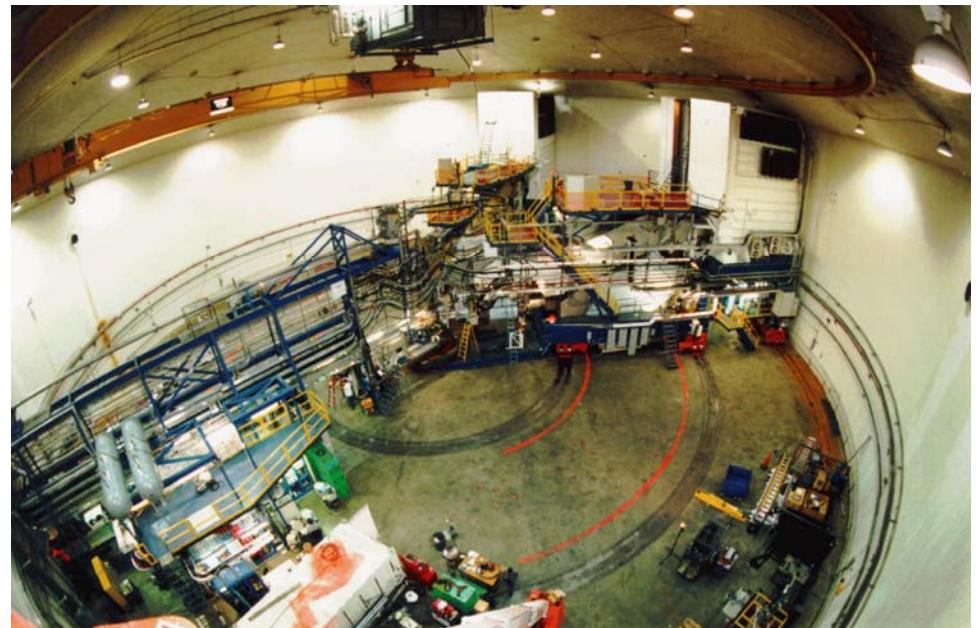
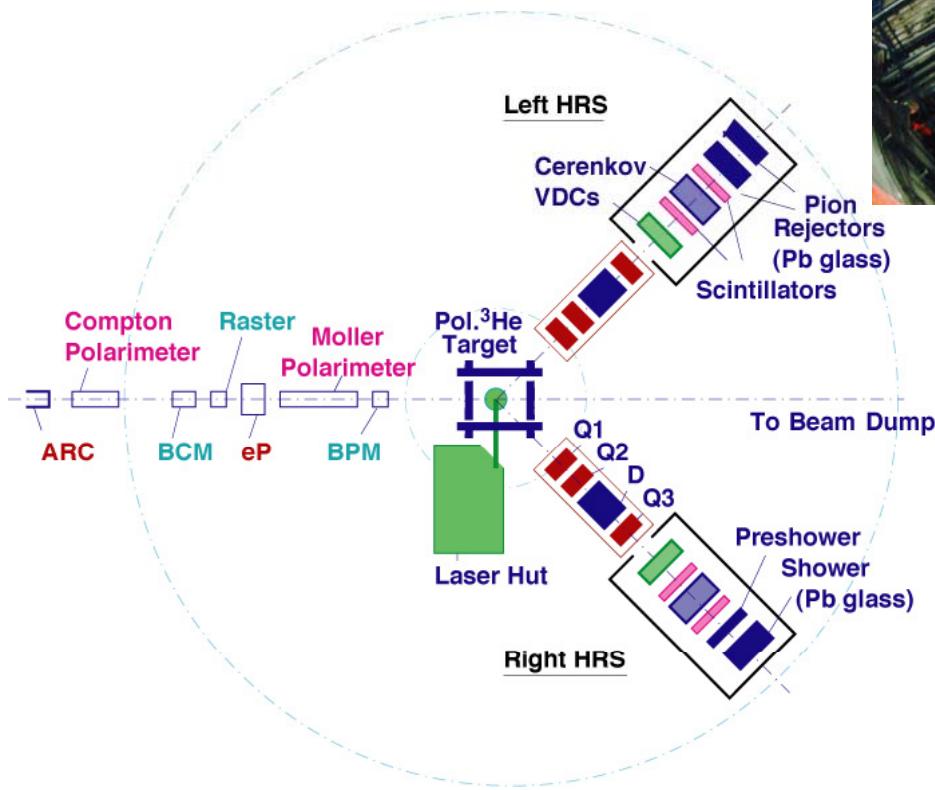
M. Amarian et al., Phys. Rev. Lett. 92, 022301 (2004)

M. Amarian et al., in preparation

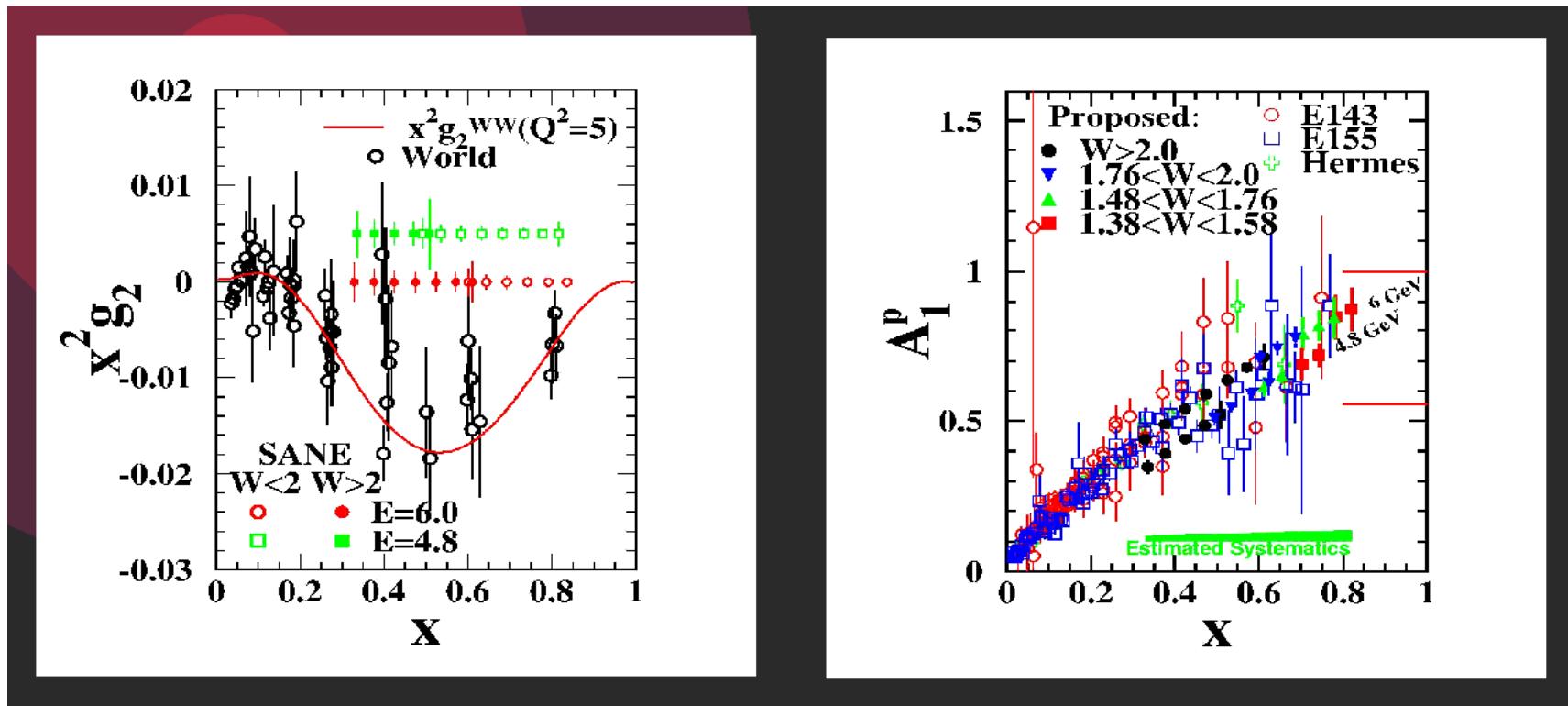
# Jlab Hall A Experimental Setup

75-80% polarized beam at  $15\mu\text{A}$

35-40% polarized target in beam



# Proton $g_2$ and $A_1$



- DIS data up to  $x = 0.6$ ; Resonances measured down to  $W = 1.38 \text{ GeV}$ 
  - $g_2$  measured in region of most sensitivity for  $d_2$